

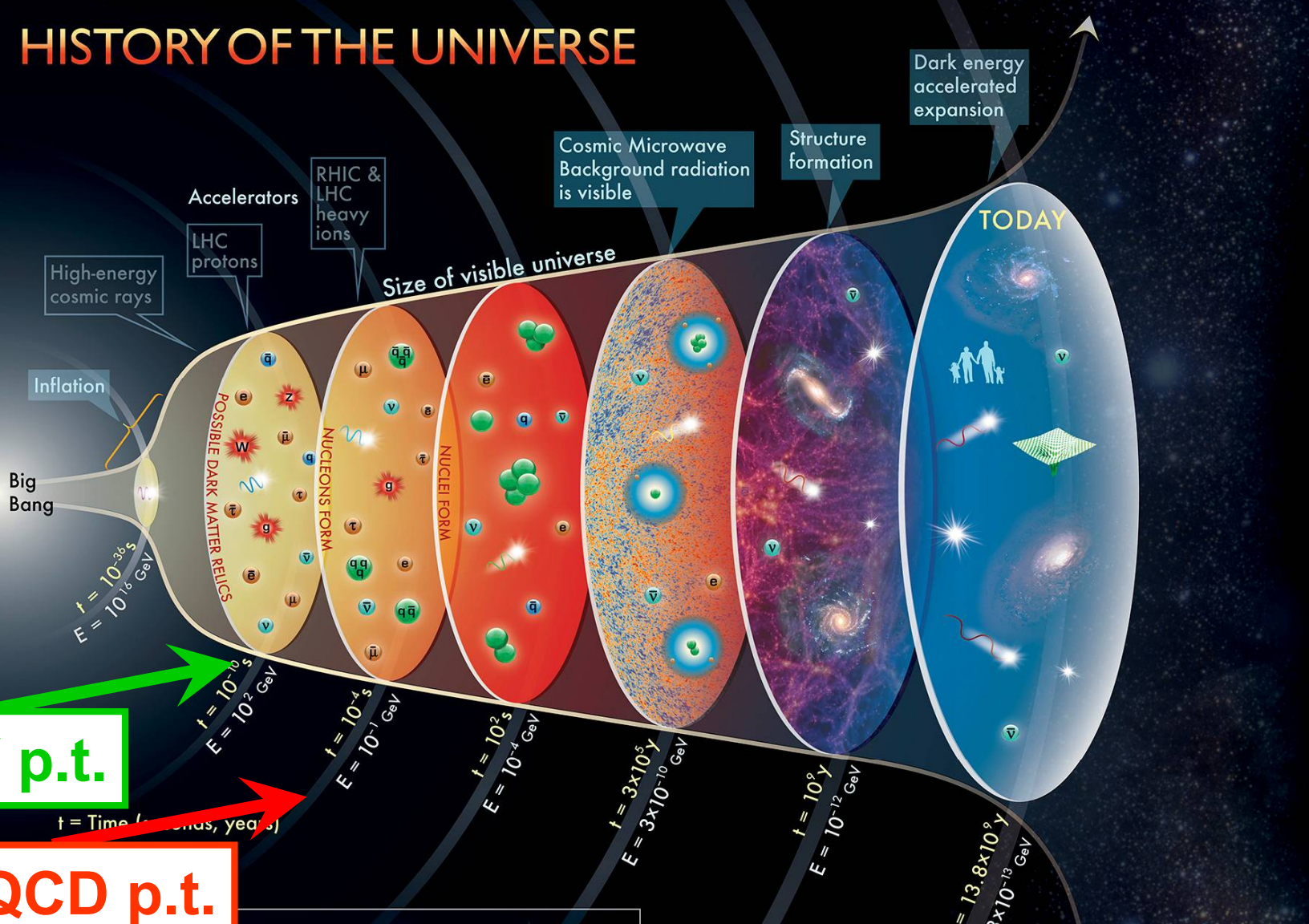
# Phases of Quantum Chromodynamics at Extremes

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# HISTORY OF THE UNIVERSE



**EW p.t.**

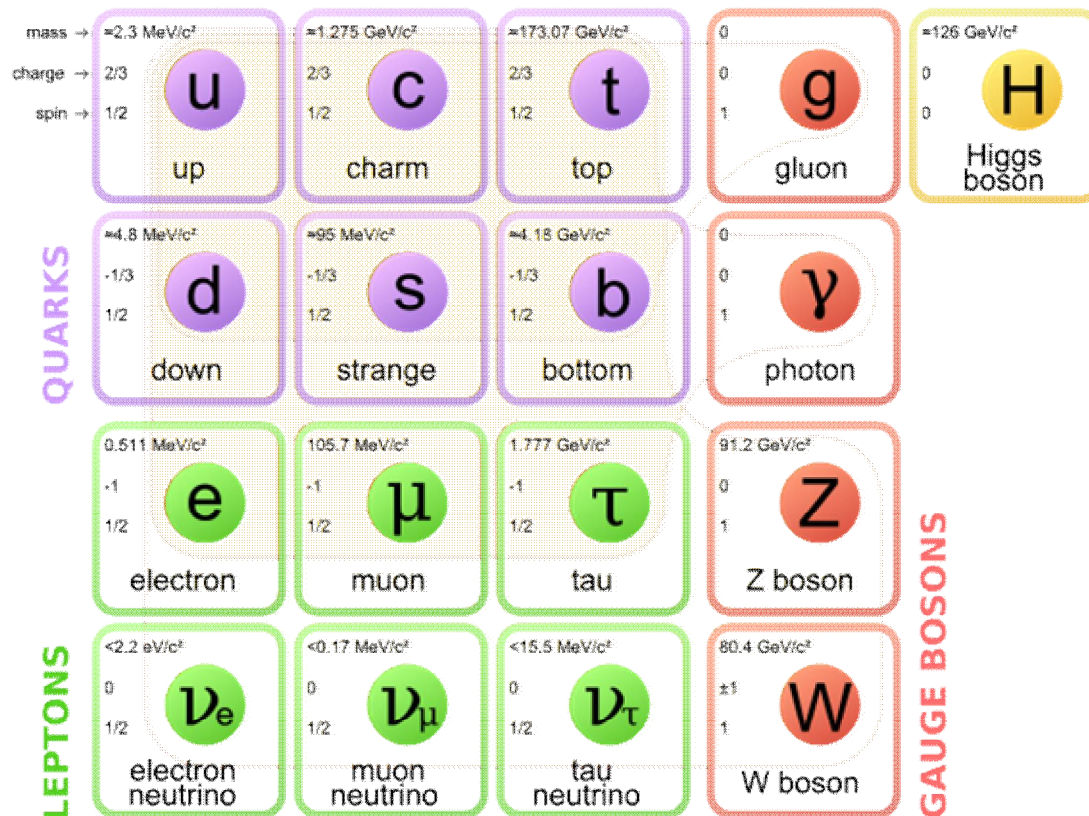
**QCD p.t.**

**What is the origin of matter?**

- gluon
- electron
- muon
- tau
- neutrino
- bosons
- meson
- baryon
- ion
- atom
- photon
- black hole

# EM, Weak & Strong: Standard Model

- What is an **elementary** particle?
  - Minimal composition of ordinary matter
  - No substructure, or substructure unknown



# Gauge principle

- Known elementary particles – 37  
18 quarks/6 leptons/12 gauge bosons/1 Higgs
- What is the guiding principle?  
→ **Symmetry dictates interactions uniquely!**
- Gauge structure of SM  
→  $SU(2) \times U(1) \times SU(3)/U(1)_{em} \times SU(3)$   

Weak & EM      Strong

# What is QCD?

Quantum Chromodynamics (QCD): strong force

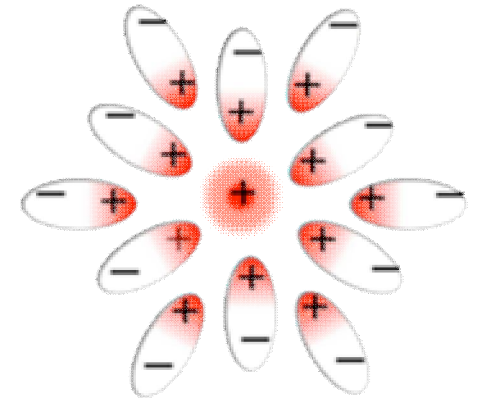
→ SU(3) gauge theory: rot. inv. in color space

- Quarks and gluons carry color charges.

- Gluon self-interactions

- Anti-screening of color charges

cf. QED: electric charges screened



increasing resolution → smaller color charges

higher energy → weaker QCD interaction

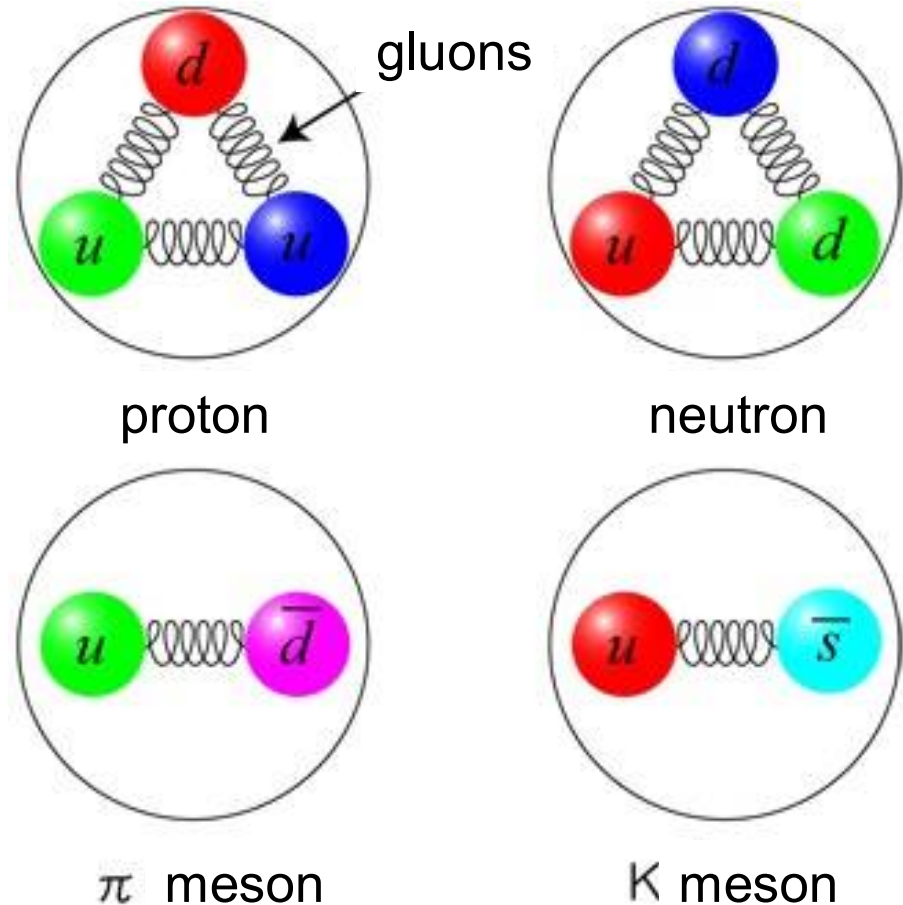
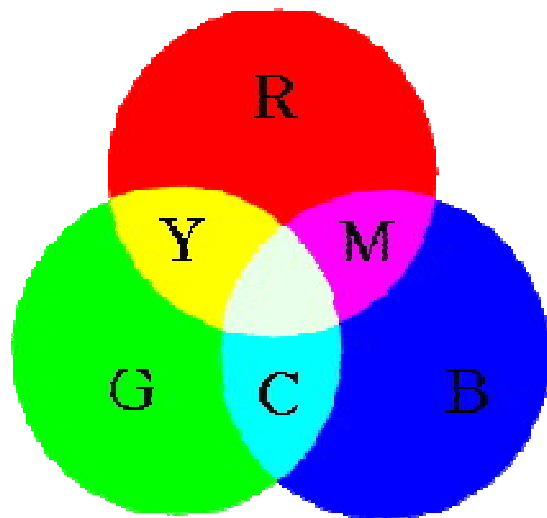
**Asymptotic freedom**

# Isolated single quark?

Quarks are confined! → composite states

Hadrons: white/singlet under SU(3) rot.

- Baryons (3 quarks)
- Mesons (2 quarks)
- Exotic hadrons

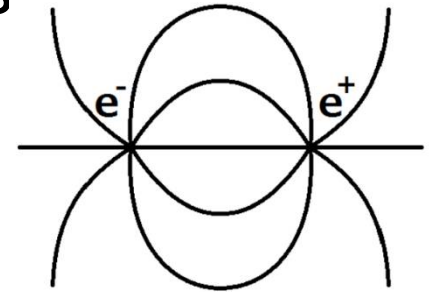
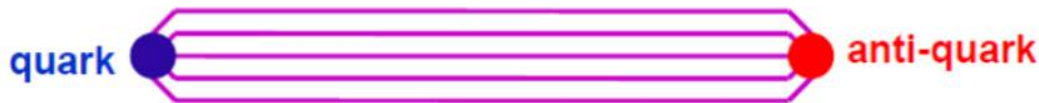


# Quark confinement

Phenomenology well described by

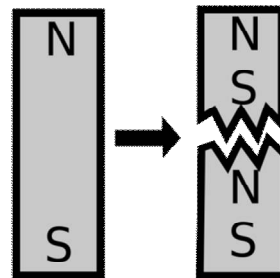
Coulomb ( $1/r$ ) + linear ( $r$ ) potential.

- separate 2 quarks  $\rightarrow$  color flux tubes



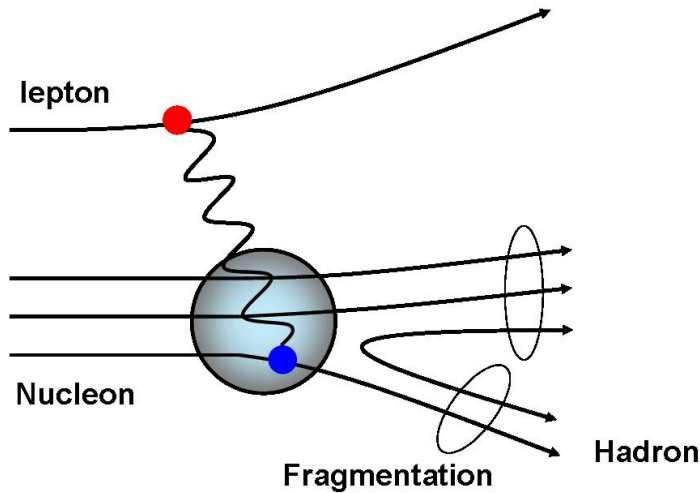
- separate them further  $\rightarrow$  exceed threshold energy of  $q\bar{q}$  pair creation  $\rightarrow$  tubes broken and a meson created.

- cf. a bar magnet



# How to “see” quarks?

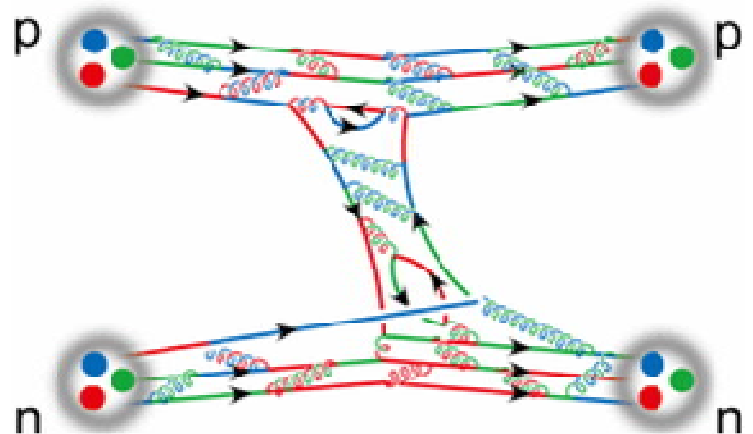
- High-energy particle collisions



Internal structure of a proton:  
a jet of hadrons

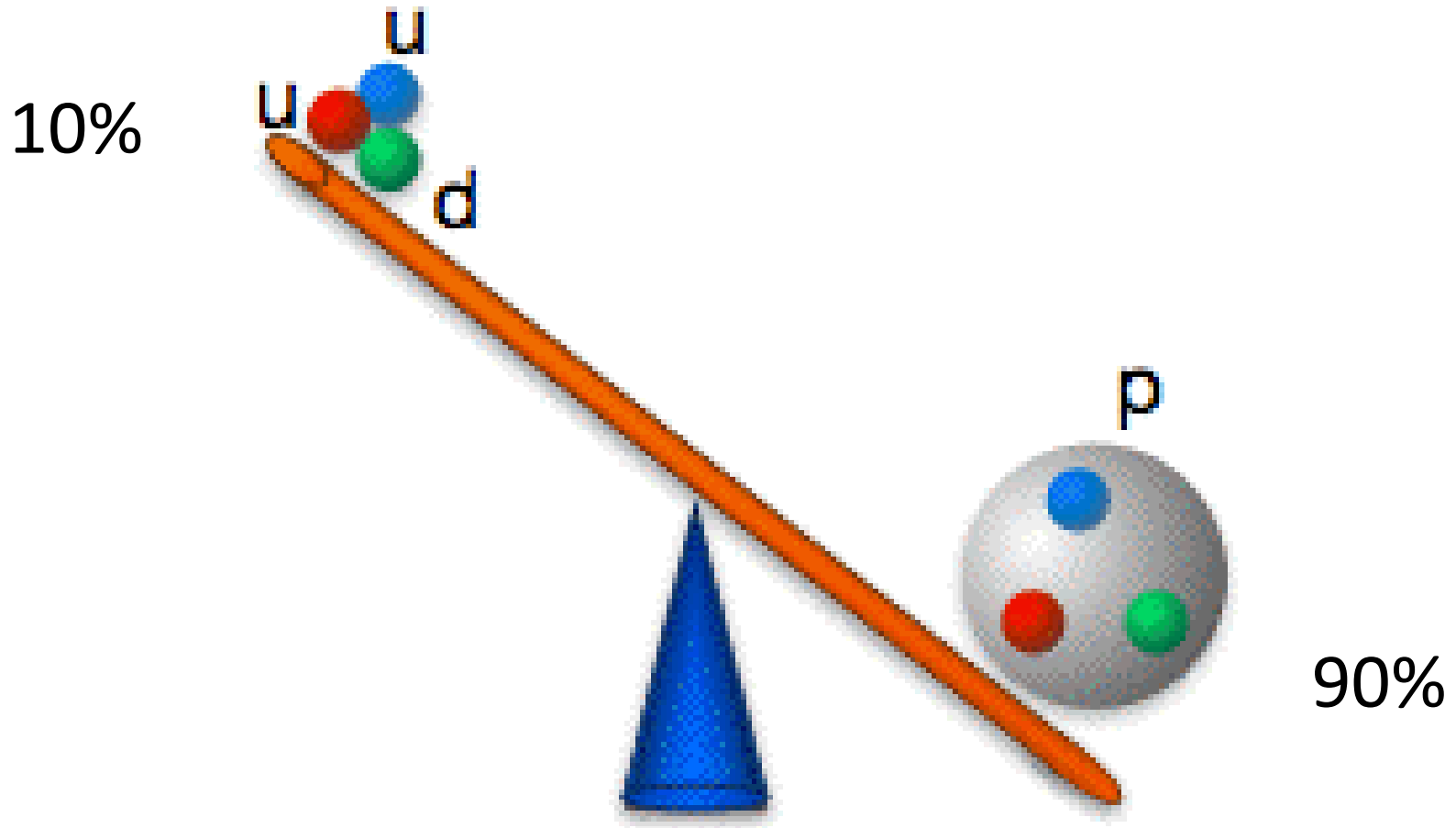
- Microscopic picture of nuclear forces

Quark-gluon reactions,  
nonlinear quantum effects



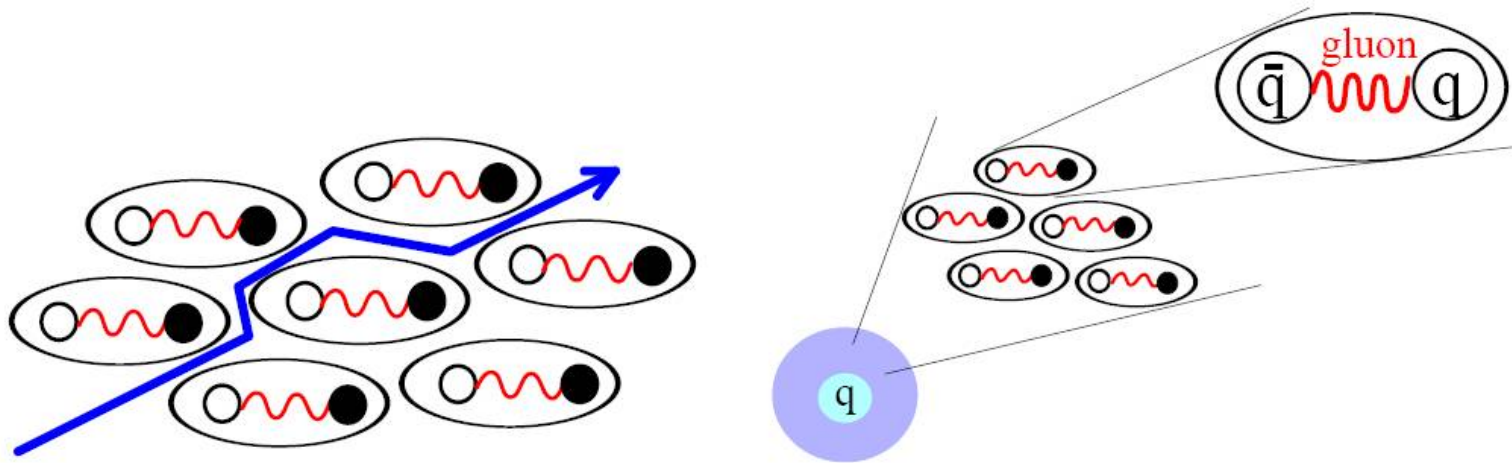


# The proton mass



# The ground state is not empty!

- Strong int.  $\rightarrow$  quark-antiquark pair formed

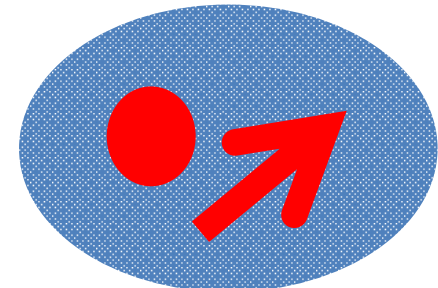
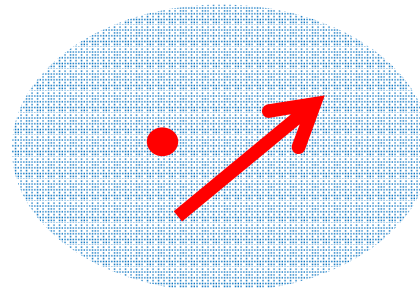


- “bare” quark  $\rightarrow$  “dressed” (massive) quark

- VEV  $q\bar{q}$ : order parameter

$\rightarrow$  Spontaneous breaking  
of chiral symmetry

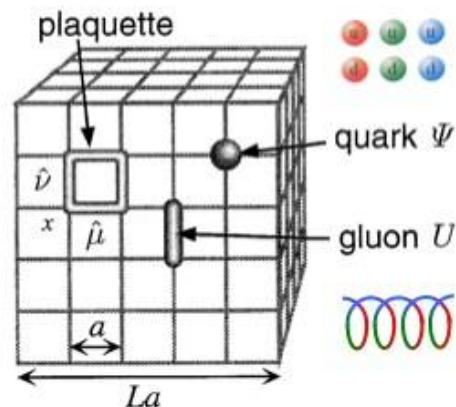
$$LL + RR + LR + RL$$



# QCD in low energy

Asymptotic freedom  $\rightarrow$  pQCD not valid!

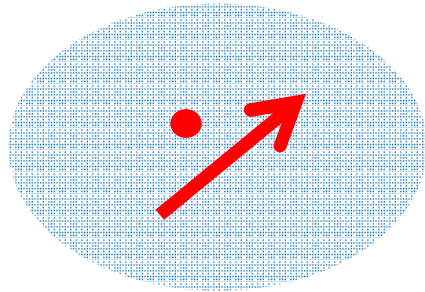
- Lattice gauge theory: MC simulations on a discretized space – first principles calc.
- Integral equations: e.g. Schwinger-Dyson eq.
- Effective theory: relevant d.o.f. & symmetries



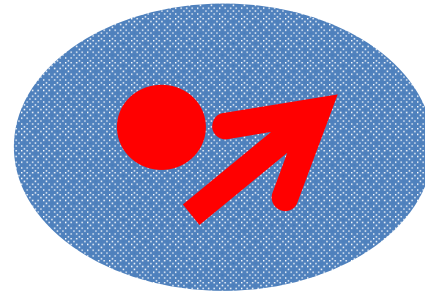
$$\left( \text{---} \bullet \text{---} \right)^{-1} = \left( \text{---} \text{---} \right)^{-1} + \text{---} \bullet \text{---} + \text{---} \bullet \text{---} + \text{---} \bullet \text{---}$$

full quark propagator
full gluon propagator  
full vertex

$t \approx 10^{-10}$  sec



today

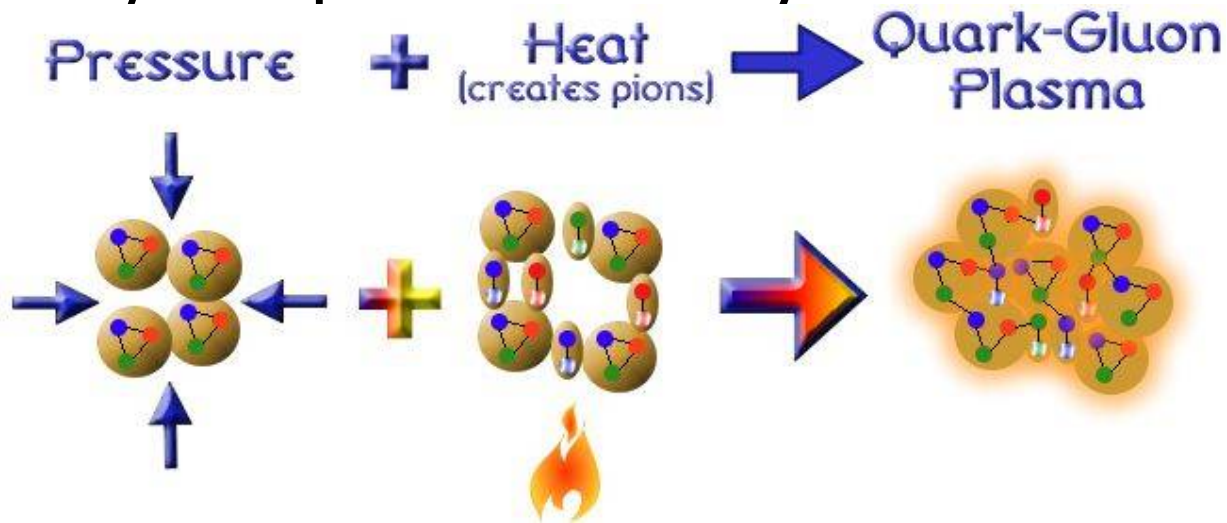


**HOW TO PROBE THE QCD PHASE  
TRANSITION?**

# QCD at high temp./density

- Early Universe:  $T \approx 2 \times 10^{12} K$   
cf. the core of the Sun:  $T \approx 10^7 K$
- Neutron stars:  $\rho \approx (5 - 10)\rho_0$

- Let's heat/compress ordinary matter!



- via QGP formation, “dressed”  $\rightarrow$  “undressed” quark
- Main goal in heavy-ion collision experiments

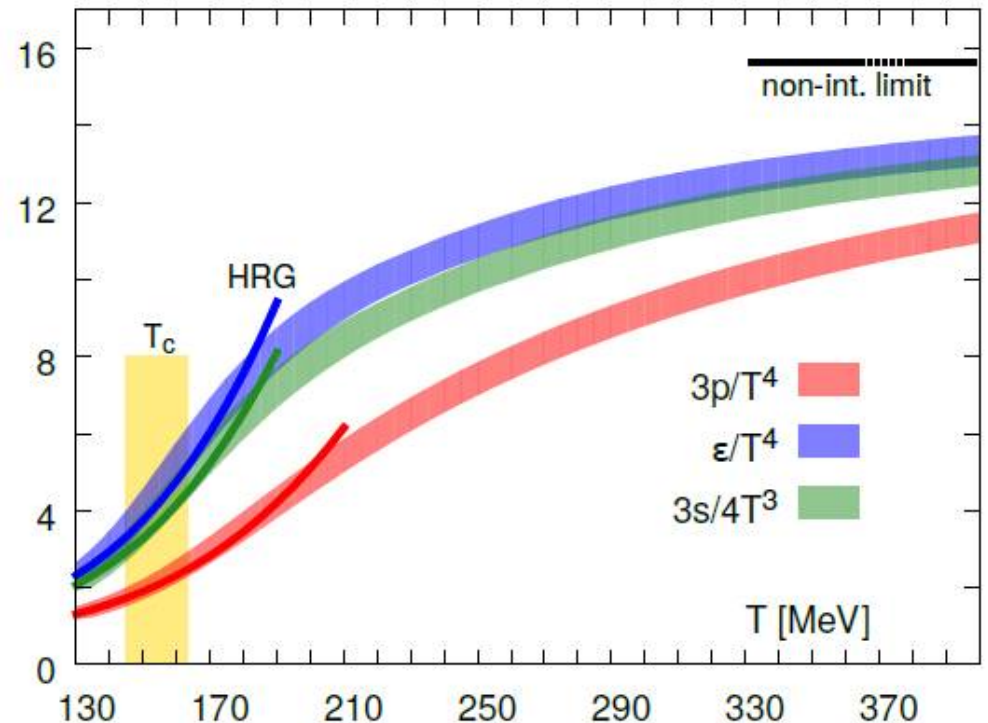
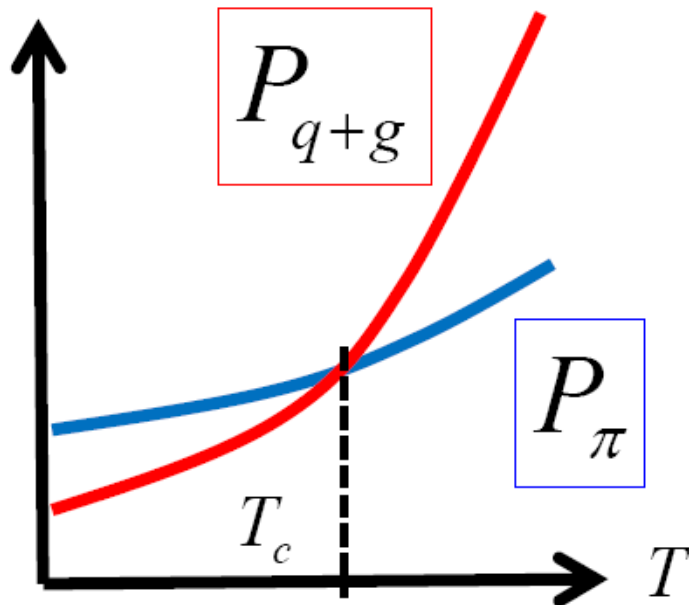
# Quark-Hadron phase transition

- Illustration in a simple model

  - Liberation of d.o.f.  $d_\pi = 3 \rightarrow d_q + d_g = 40$

- EoS from Lattice QCD: a crossover

$$\chi_{\bar{q}q} = \partial^2 P / \partial m_q^2 \approx V^0 \quad (V^1 : 1st, V^{2/3} : 2nd)$$



# Hot QCD at $\mu \approx 0$

❑ Restoration of chiral sym.

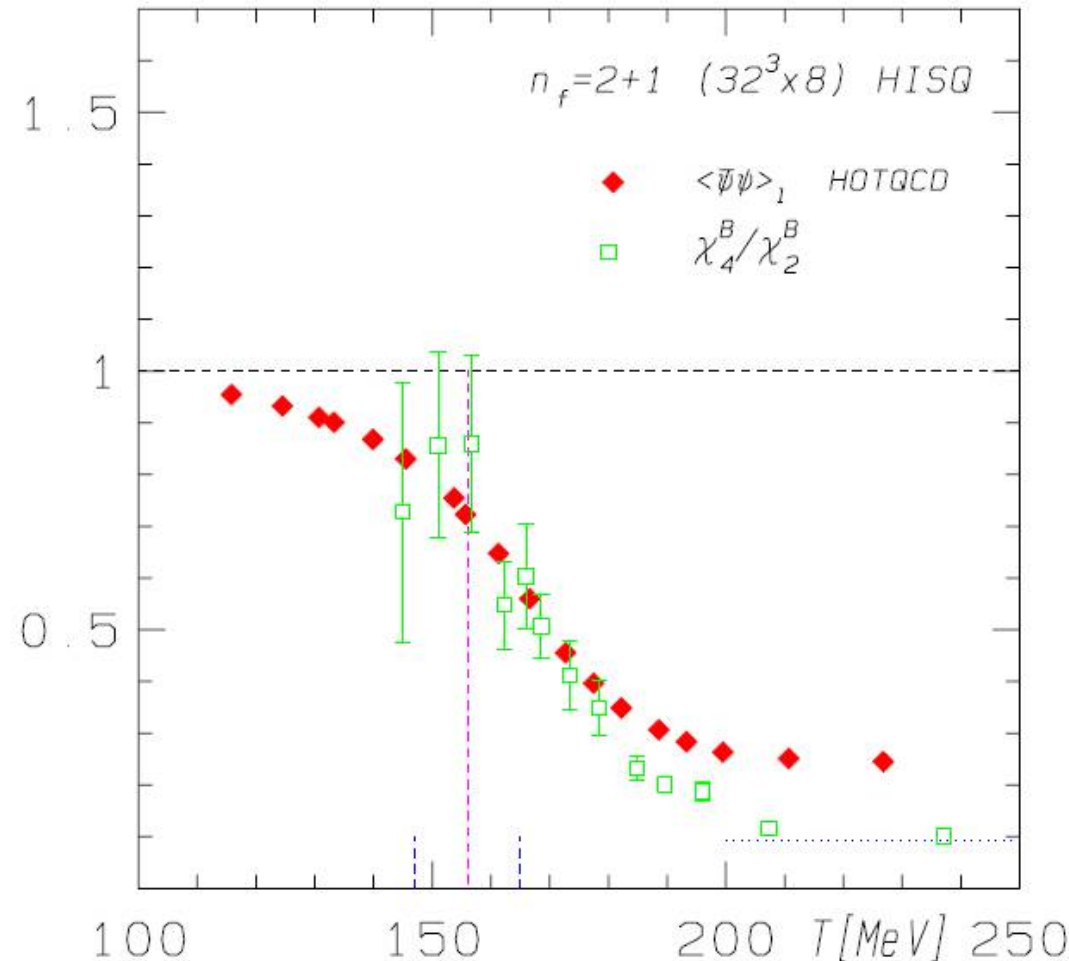
at  $T_c=154$  MeV

❑ Deconfinement

✓ Conserved charges

✓ Comprehensive comparison to Hadronic scenario

❑  $T_{dec} \approx T_c$



# **Chiral-confinement interplay in cold dense QCD**



# How to model dense QCD?

❑ Lattice simulations invalid → model analyses

❑ **Good** model must possess

- **Correct properties of nuclear ground state**

- ✓ Saturation density, binding energy, compressibility

- ✓ Rather big chiral-inv. mass  $m_0 \approx 500\text{-}800$  MeV favored

[Zschiesche et al. (07), Gallas et al. (11)]

- **Correct degrees of freedom**

- ✓ Nucleons at low density/quarks at high density

→ How to realize the 2<sup>nd</sup> property?

# Quark-nucleon hybrid model

□ How to suppress quarks at low density?

➤ IR/UV cutoff “b” in Fermi dist. functions

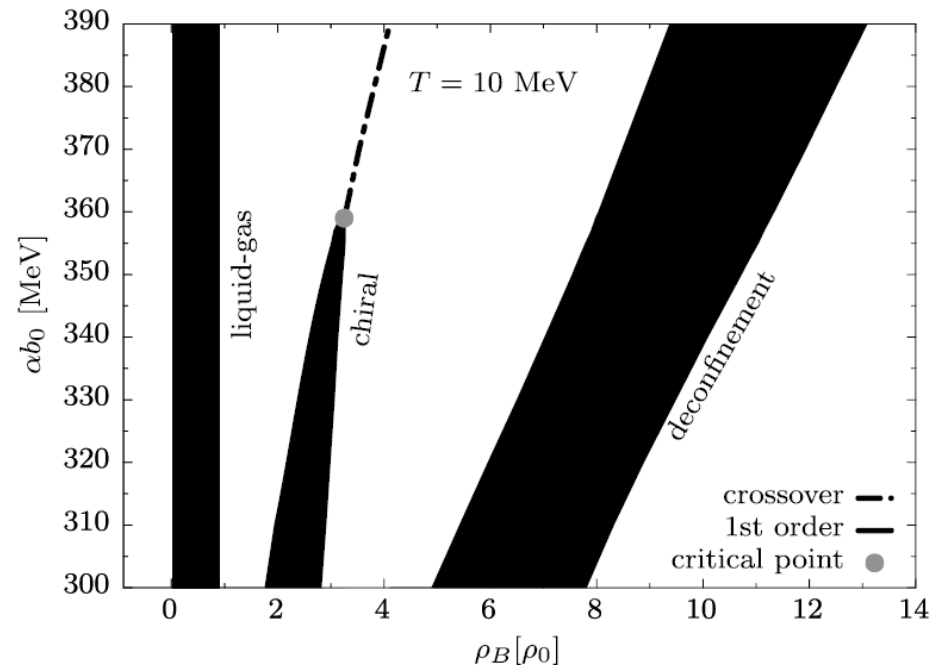
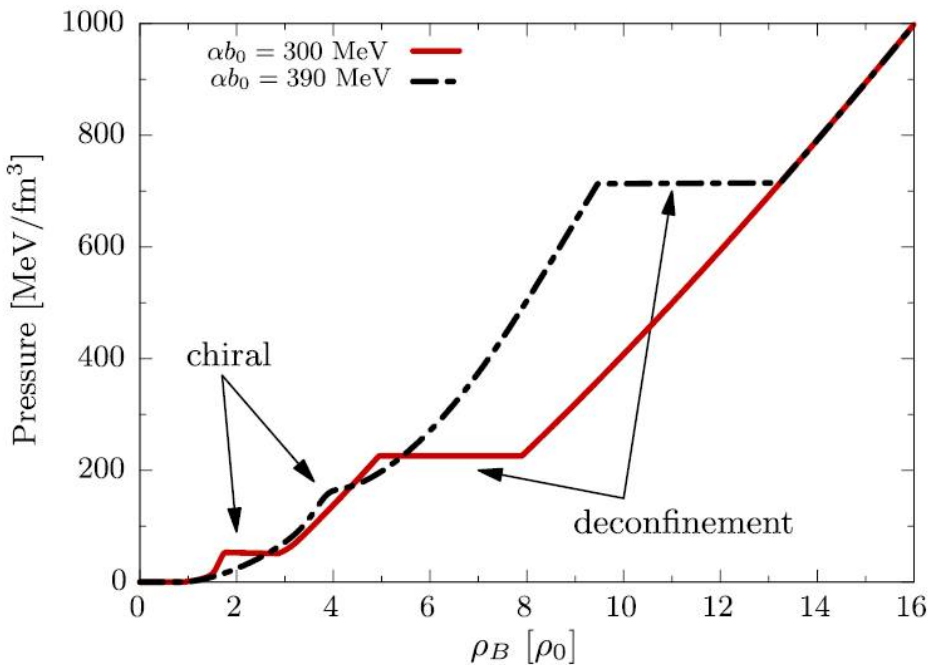
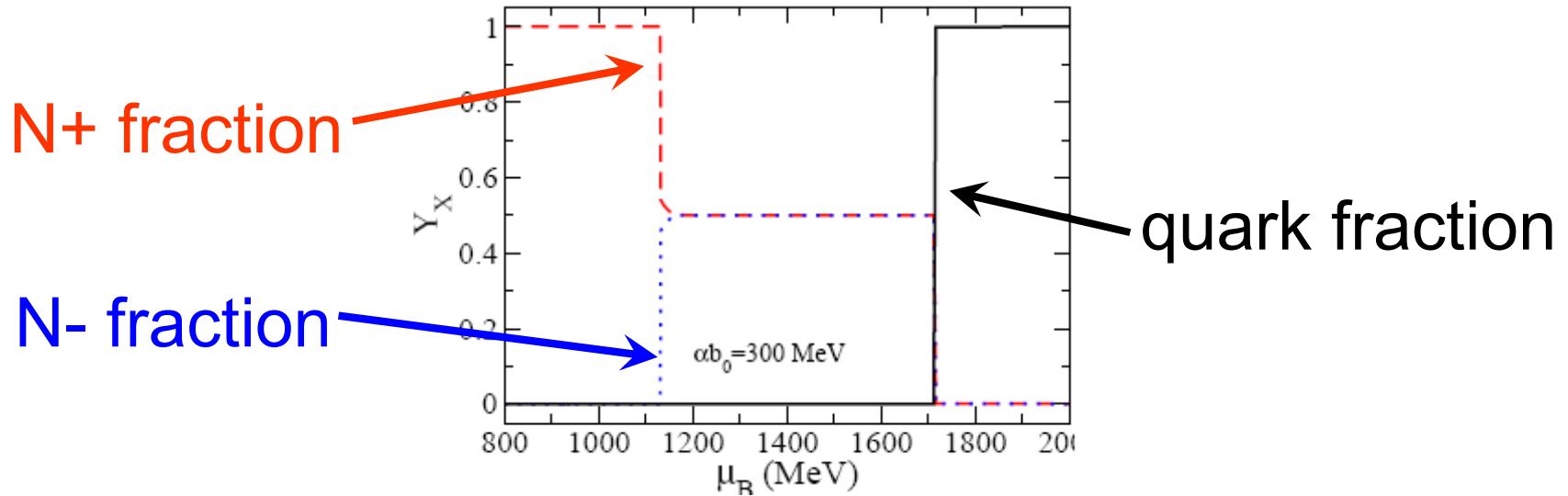
➤ from const. “b” to a VEV of a scalar field b

□ Chiral & deconf. p.t. in a single framework

$$\int_0^{\langle b \rangle} dp f_N(p; T, \mu) \rightarrow \int_0^0 dp f_N(p; T, \mu) = 0$$

$$\int_{\langle b \rangle}^{\infty} dp f_Q(p; T, \mu) \rightarrow \int_0^{\infty} dp f_Q(p; T, \mu)$$

# Onset of different fermions

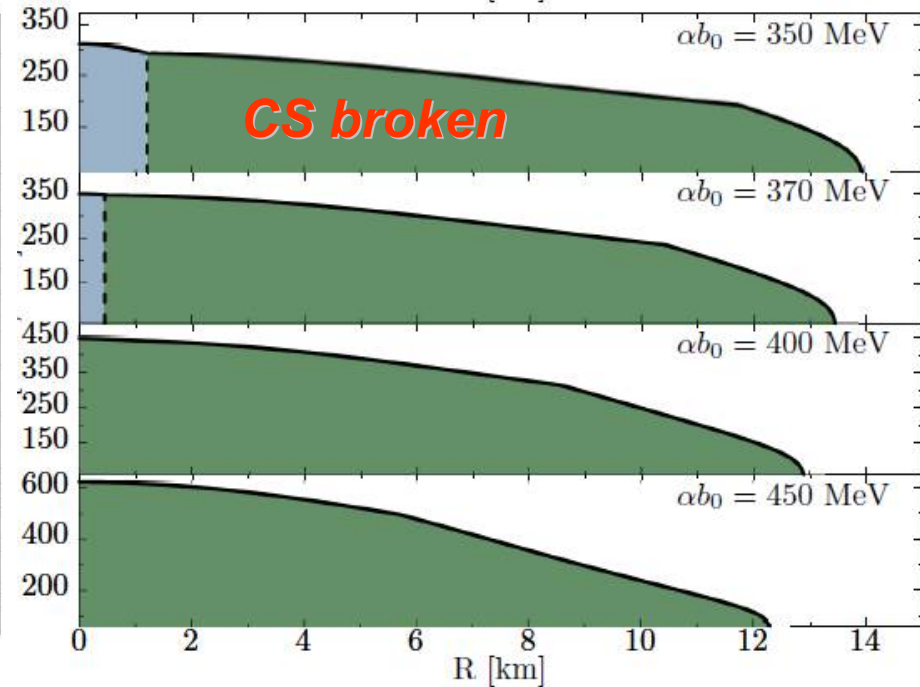
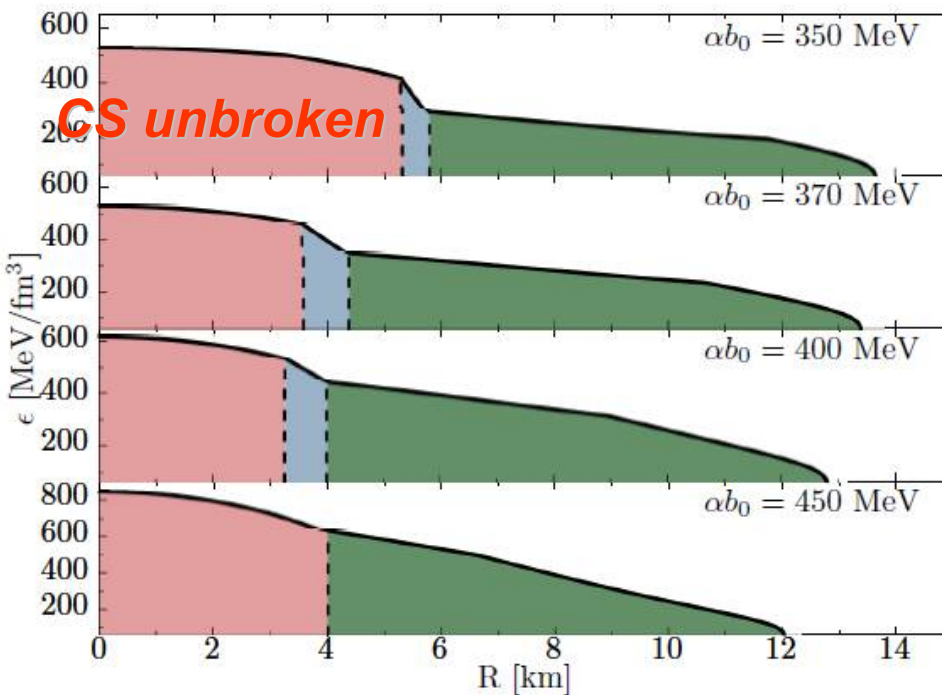


# Neutron stars

- $\beta$  -equilibrium and charge neutrality
- Constraints on the mass and compactness of a star  $\rightarrow$  **hadronic scenario w/o deconf. quarks**

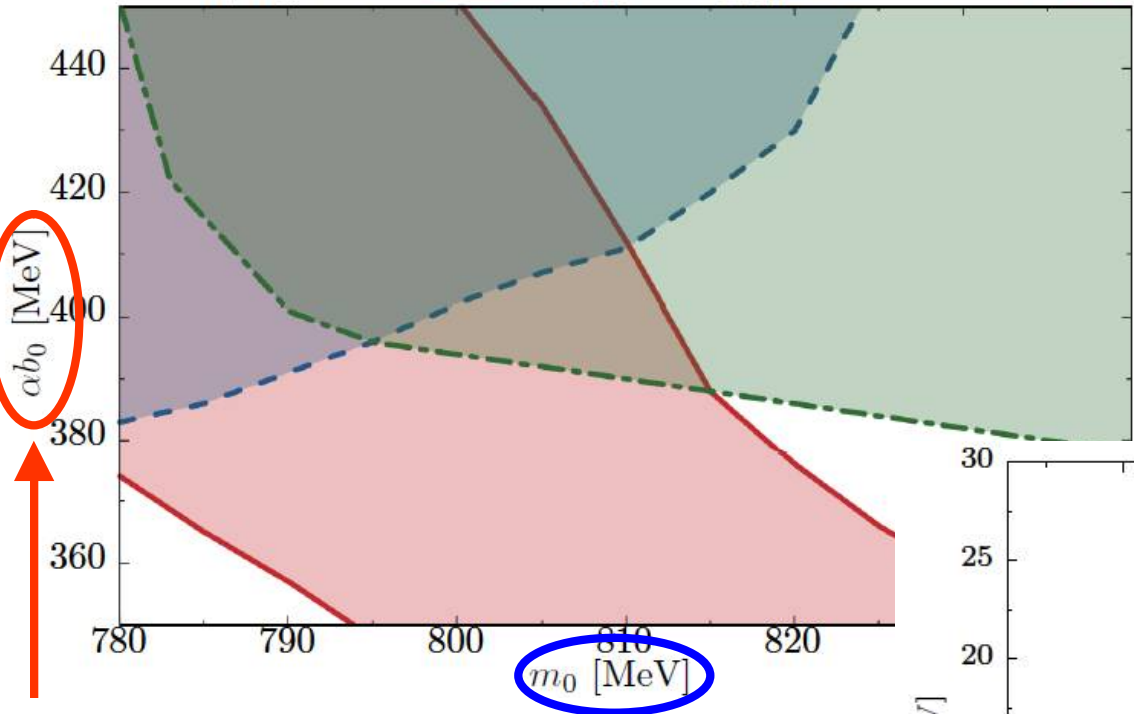
2.05\*SM NS

1.97\*SM NS



# Toward QCD phase diagram

$2 < M/M_{\odot} < 2.16$  ———  $M_{\text{DU}} > M_{\text{BRP}}$  - - -  $\Lambda < 800$  - - -

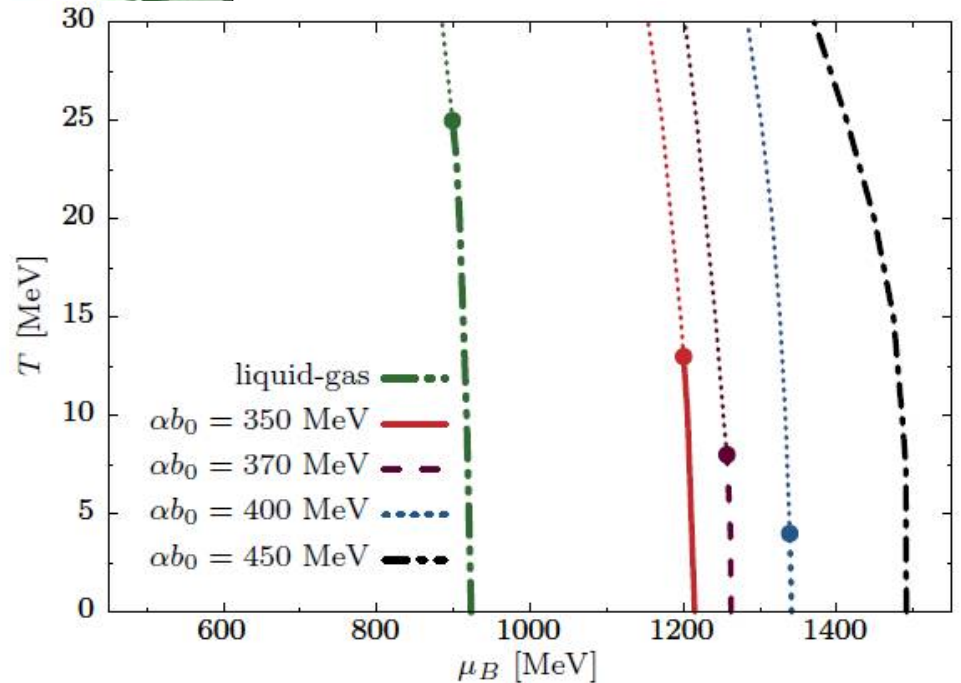


- ✓ Mass
- ✓ Cooling
- ✓ Tidal deformability in the binary merger

IR cutoff

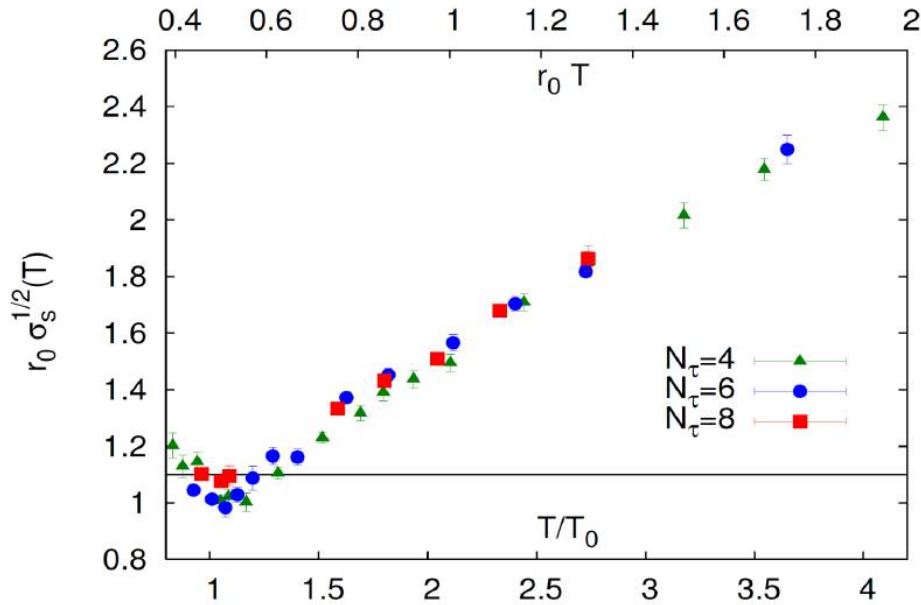
Chiral-inv. mass

CP disfavored?



# Fate of confinement: hot vs. dense

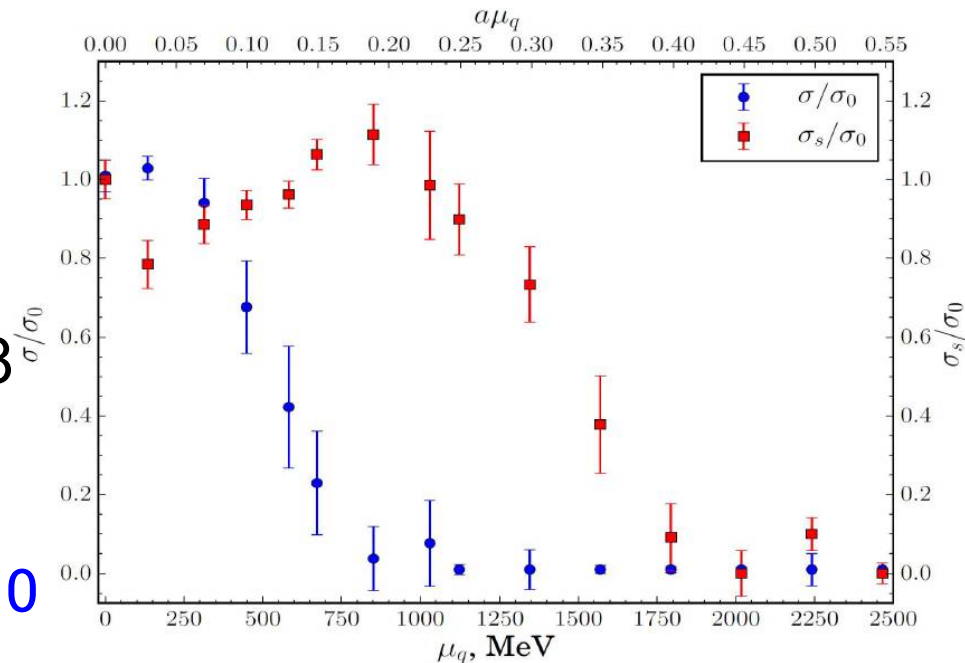
□ Non-pert. color-mag. sector  $\rightarrow$  perturbative!



$\leftarrow SU(3)_c, T > 0, \mu = 0;$   
 Cheng et al., PRD 2008  
 [mpi = 220 MeV].

$\rightarrow SU(2)_c, T = 0, \mu > 0;$   
 Bornyakov et al., JHEP 2018  
 [mpi = 740 MeV].

- ✓  $m_0(\mu = 0)$  vs.  $m_0(\mu \neq 0)$
- ✓ Color-mag.monopoles at  $\mu \neq 0$



# Summary

# Phase diagram: all science fiction?

❑ What we know is very limited:

- ✓ Crossover at  $\mu \approx 0$ ,  $T_c \approx 154$  MeV, remnant of  $O(4)$
- ✓ Nuclear liquid-gas phase transition, CP

❑ Interplay between CSB and confinement

❑ Modifications of hadrons: mass & width

❑ Toward more realistic description of QCD

