

# Jets Escaping From Quark Soup

Ben-Wei Zhang

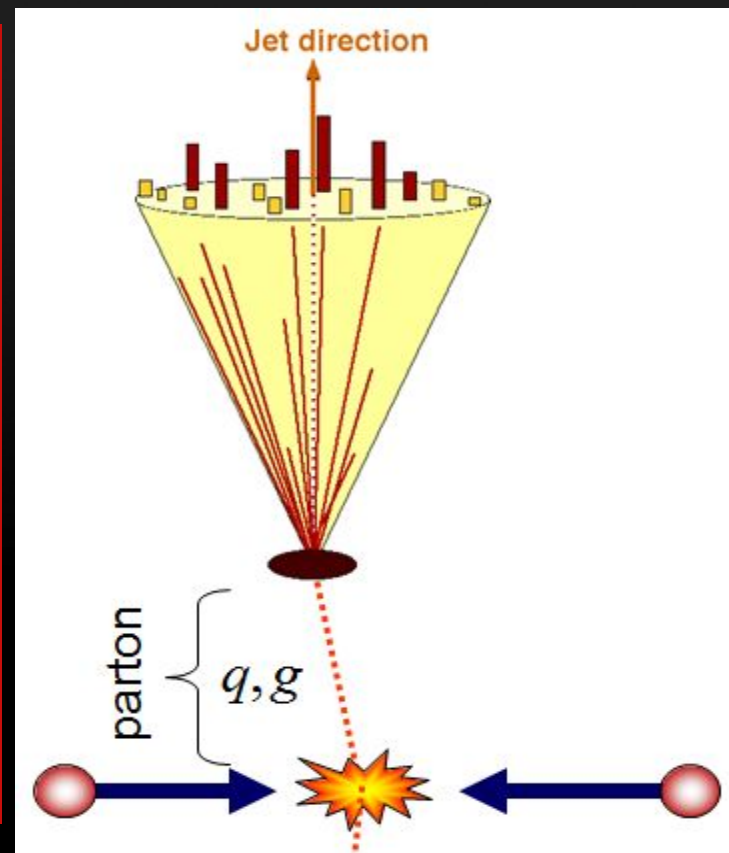
(张本威)

Institute of Particle Physics (IOPP),  
Central China Normal University



# What is a jet?

- At LO pQCD, jet  $\approx$  parton.
- A jet is a spray of final-state particles roughly moving in the same direction and defined by jet finding algorithms.
- In pQCD local-parton-hadron duality (LPHD) is used
- Jet: more precise and powerful



$$E_T = \sum_{i \in \text{jet}} E_{T,i}$$

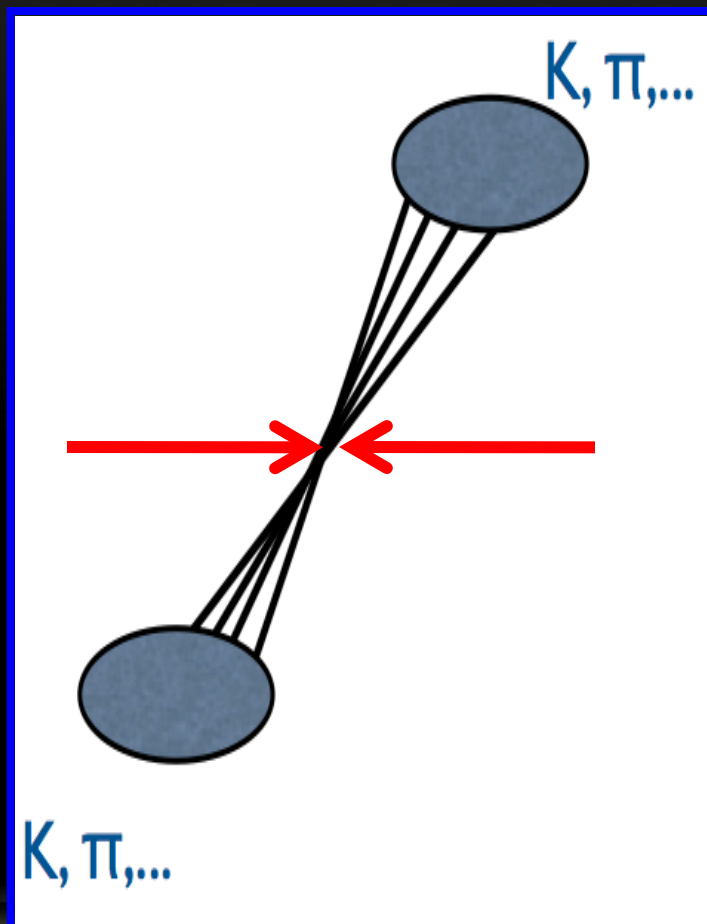
$$y = \sum_{i \in \text{jet}} y_i E_{T,i} / E_T$$

$$\phi = \sum_{i \in \text{jet}} \phi_i E_{T,i} / E_T$$

$$R_{ij} = \sqrt{(y_i - y_j)^2 + (\phi_i - \phi_j)^2}$$

# Briefing: jets at HEP

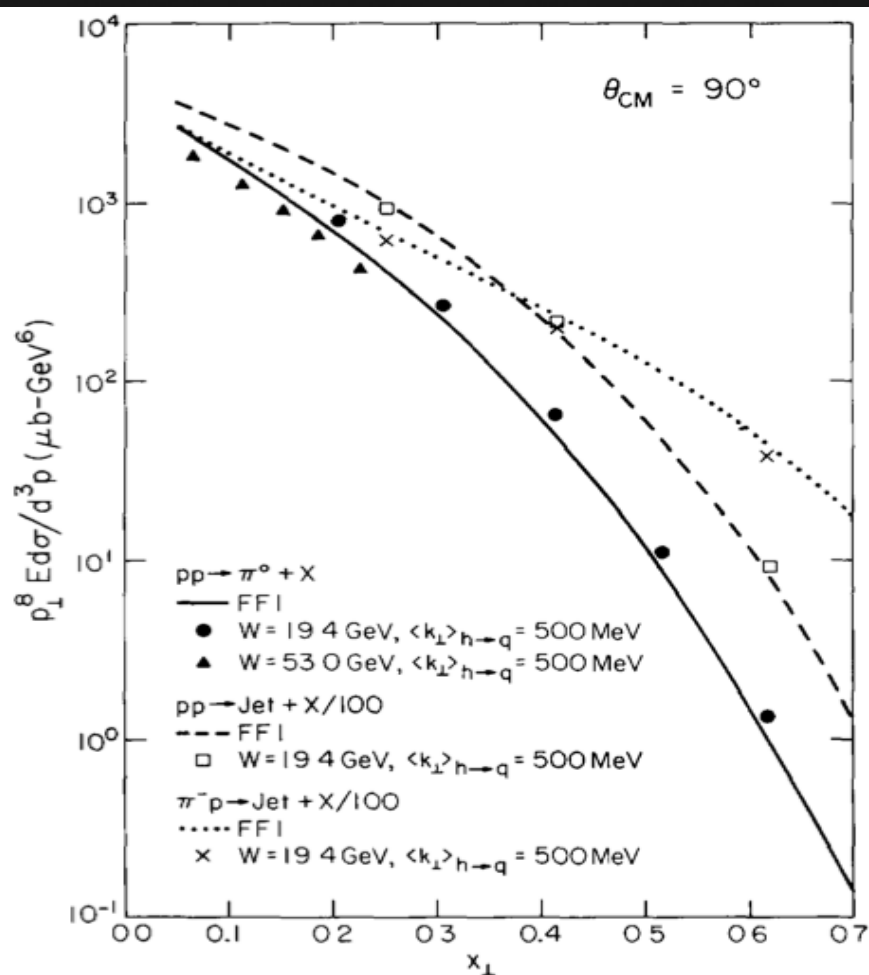
- Stermann & Weinberg ('77) defined a two-jet event and made an analytic calculation.



Stermann, Weinberg (1977)

# Briefing: jets at HEP

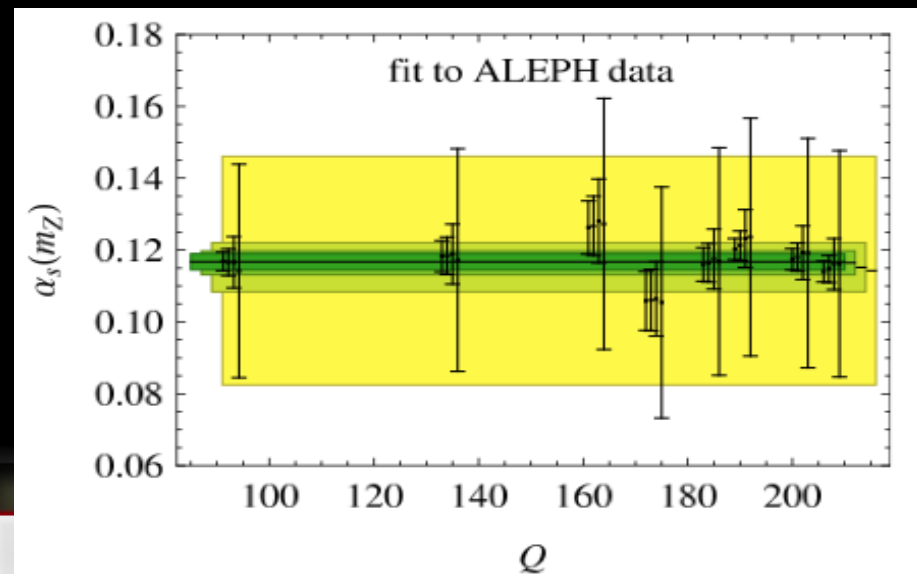
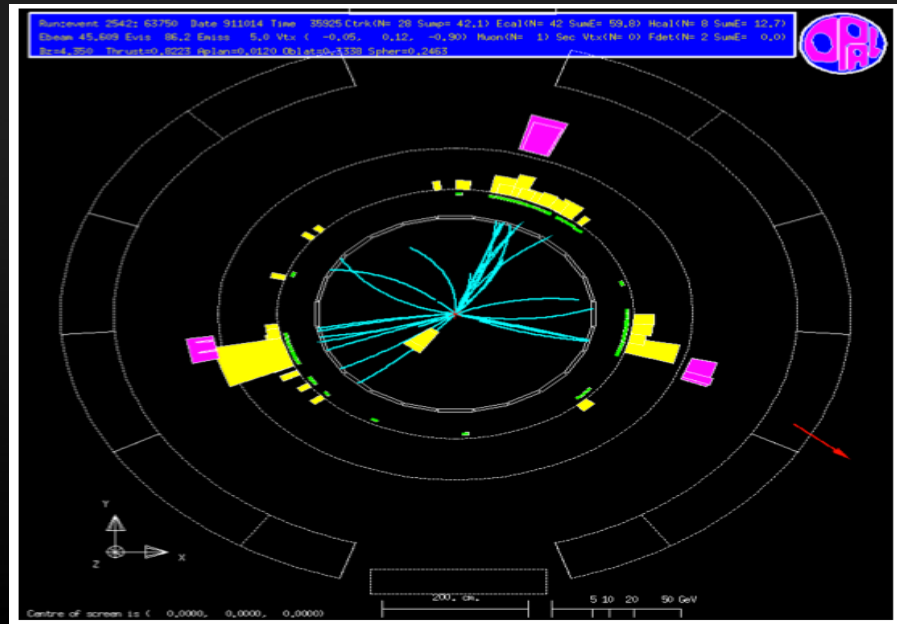
- Feynman, Field, Fox ('77) made a numerical calculation of the inclusive jet production.



Feynman, Field, Fox (1977)

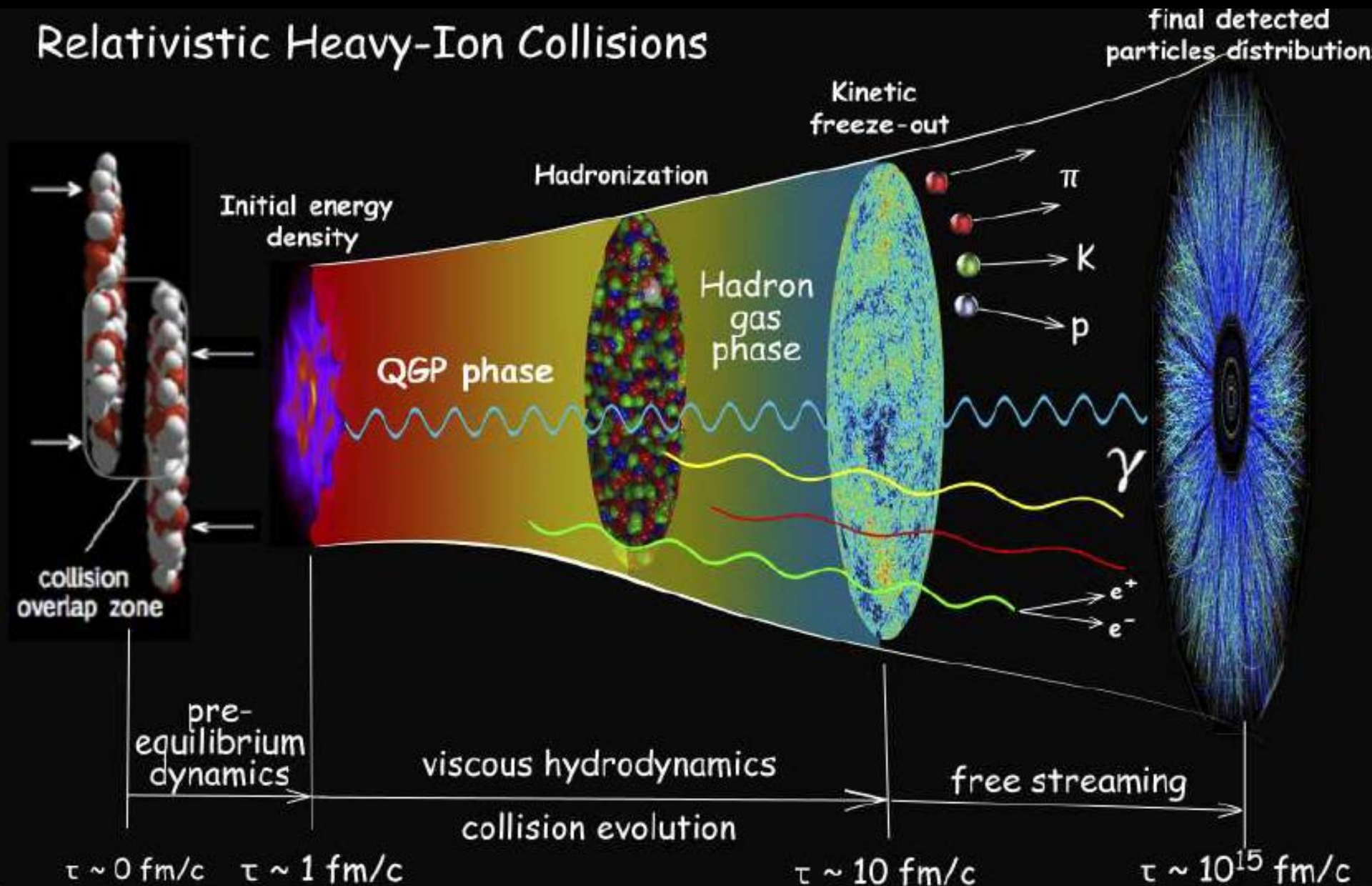
# Briefing: jets at HEP

- Discovery of three-jet events in  $e^+e^-$  gave a first evidence of gluons.
- Precise extraction of  $\alpha_s$  is made by measuring jet event shapes.
- New physics beyond Standard Model by studying jets.

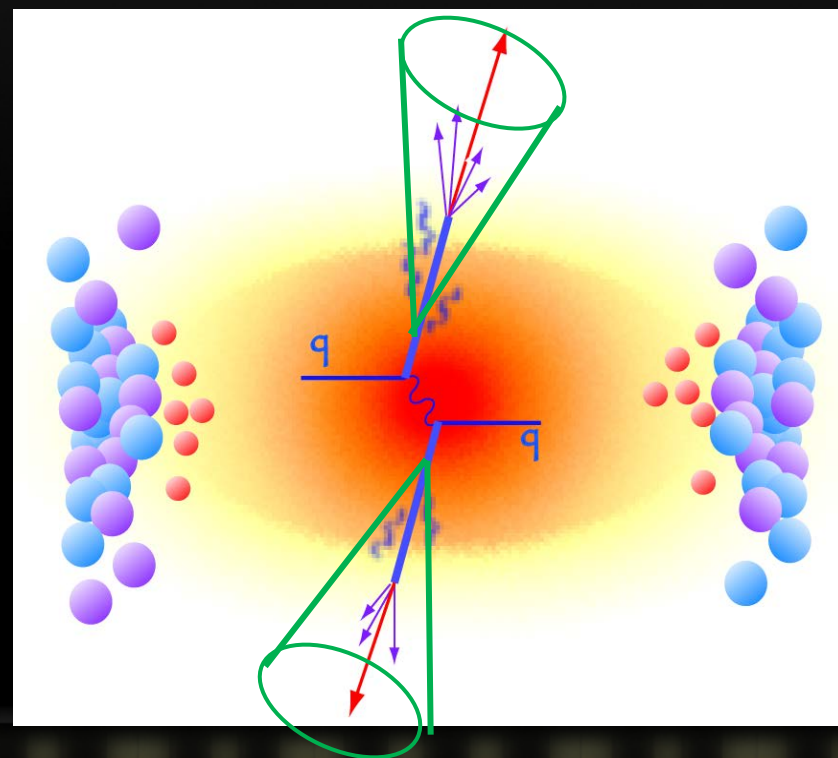


# The Little Bang

## Relativistic Heavy-Ion Collisions



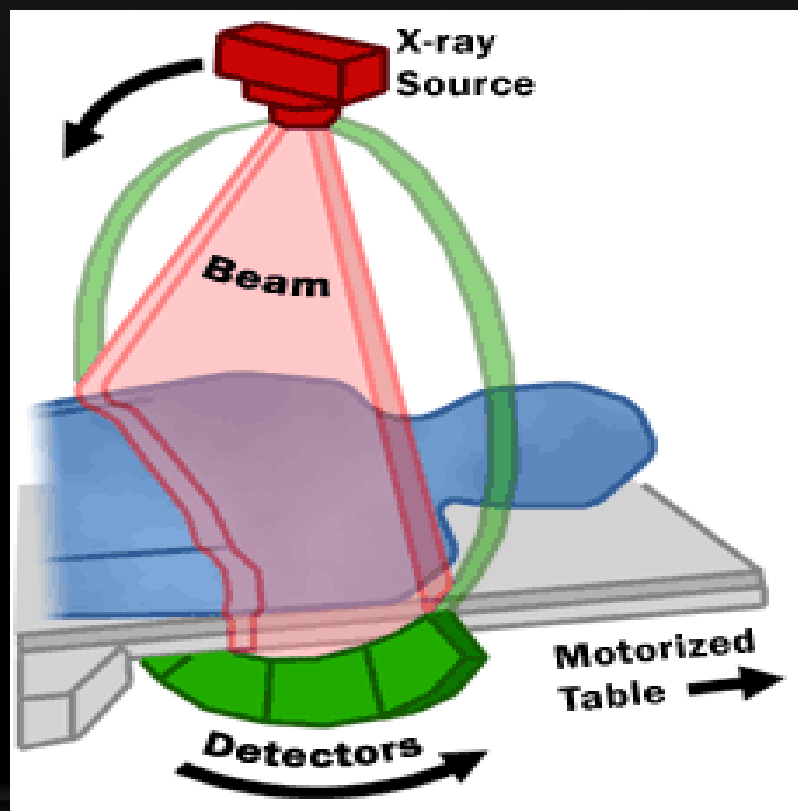
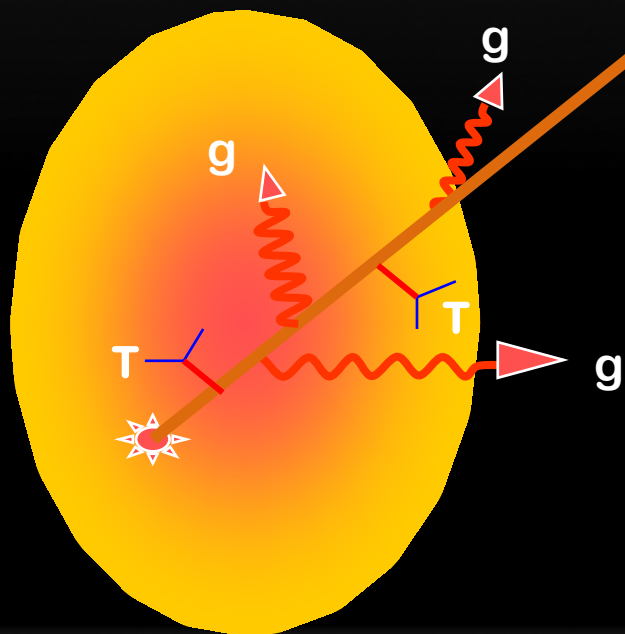
How will jets be modified in the existence of QGP ?



# Parton Energy loss as a hard probe

Parton energy has been proposed as an excellent probe of the hot/dense matter created at HIC.

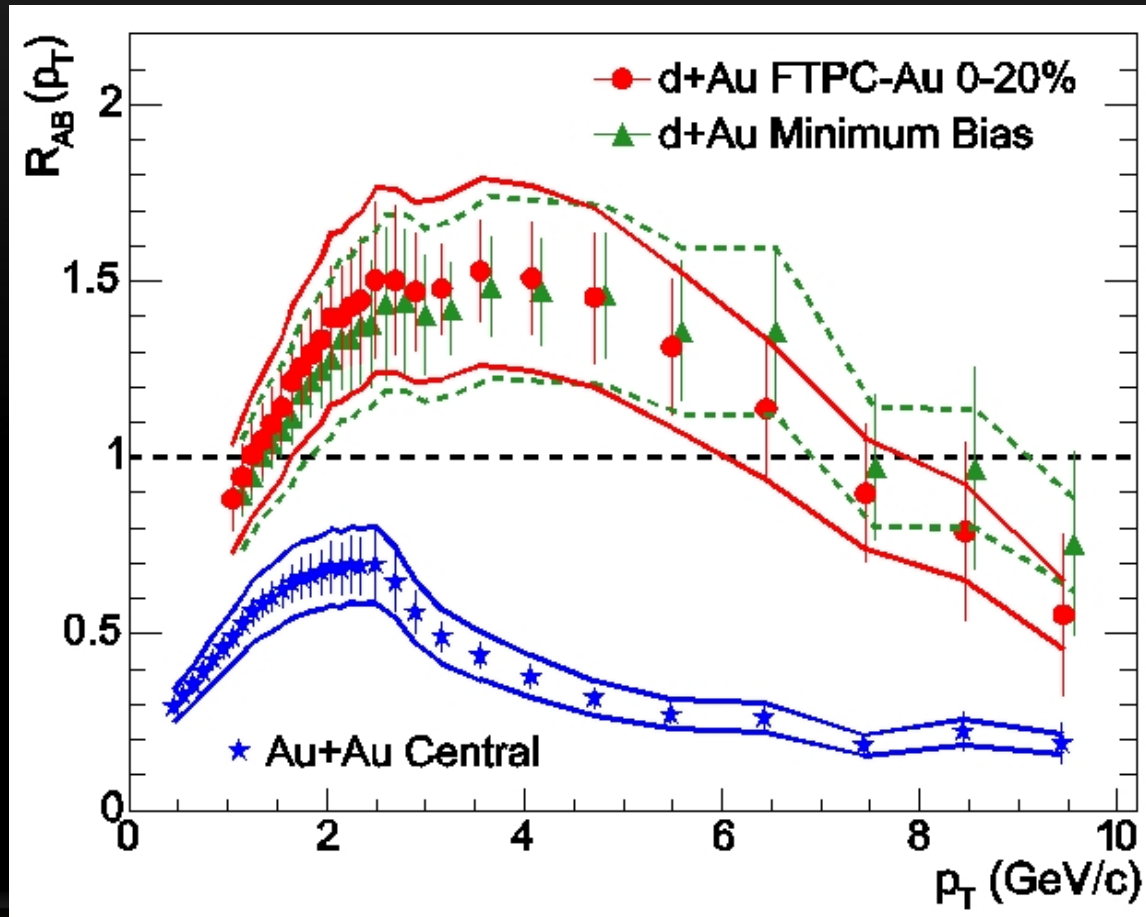
## Single Hadron Tomography





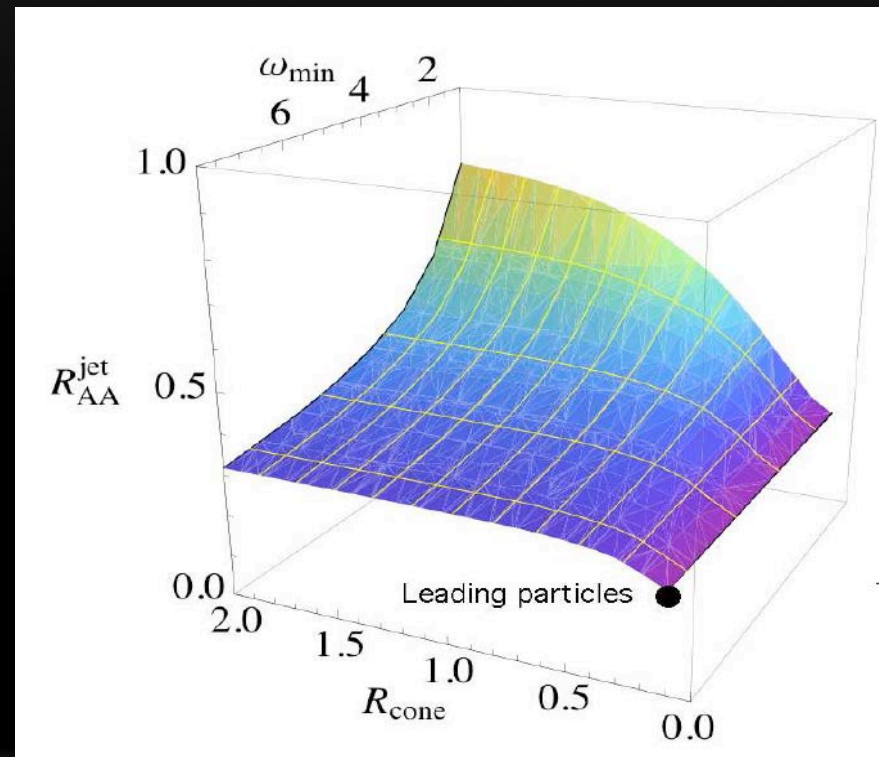
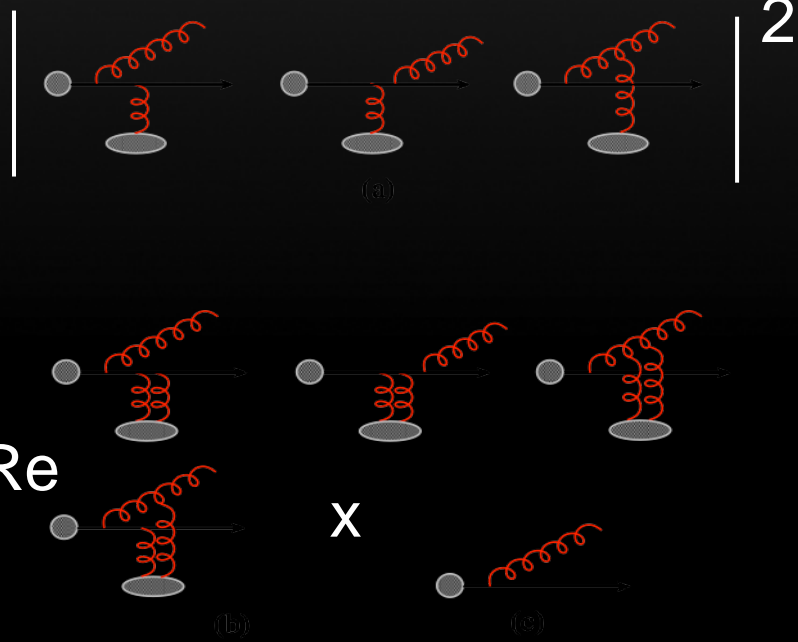
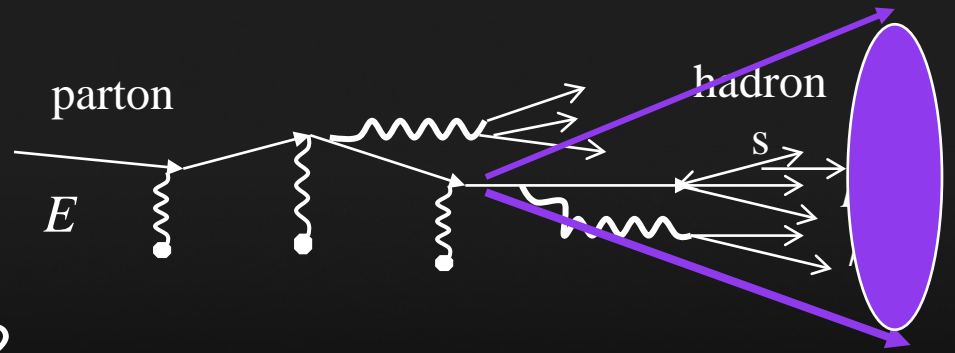
# Jet quenching at RHIC

$$R_{AA} = \frac{\text{Yield}_{\text{AuAu}} / \langle N_{\text{binary}} \rangle_{\text{AuAu}}}{\text{Yield}_{\text{pp}}}$$



# Eloss: From hadron to jets

Gyulassy-Levai-Vitev



Vitev, Wicks, BWZ, JHEP (2008)

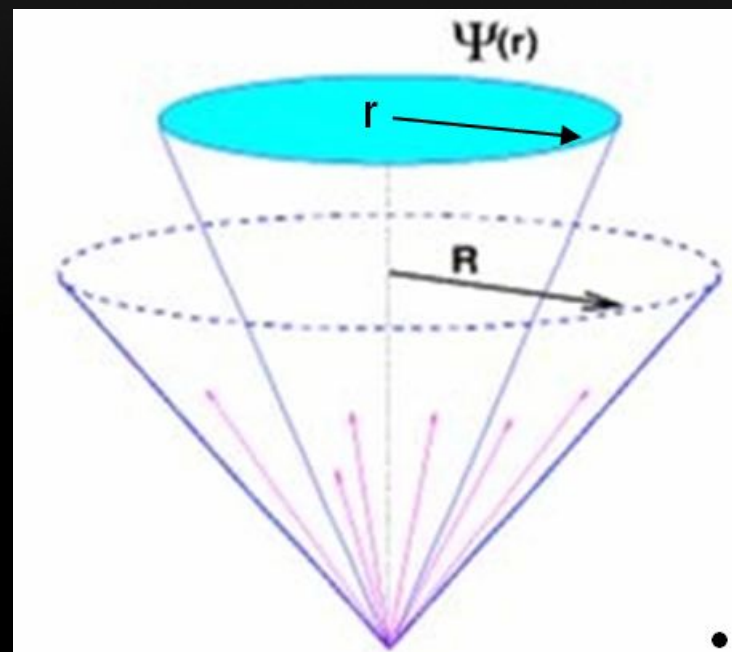
# Jets in HIC

# Jet shape in HIC

$$\Psi_{\text{int}}(r; R) = \frac{\sum_i (E_T)_i \Theta(r - (R_{\text{jet}})_i)}{\sum_i (E_T)_i \Theta(R - (R_{\text{jet}})_i)},$$

$$\psi(r; R) = \frac{d\Psi_{\text{int}}(r; R)}{dr}.$$

$$\Psi_{\text{int}}(r = R, R) = 1$$



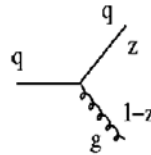
# LO & Resummation: p+p

An analytic approach to the energy distribution of jet

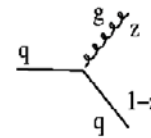
Seymour, M. (1998)

Jet shape at LO with the acceptance cut

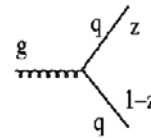
$$\psi_a(r; R) = \sum_b \frac{\alpha_s}{2\pi} \frac{2}{r} \int_{z_{min}}^{1-Z} dz z P_{a \rightarrow bc}(z).$$



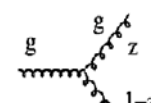
$$P_{qq}^{(1)}(x) = C_2(F) \left[ (1+x^2) \left( \frac{1}{1-x} \right)_+ + \frac{3}{2} \delta(1-x) \right]$$



$$P_{gq}^{(1)}(x) = C_2(F) \frac{(1-x)^2 + 1}{x}$$



$$P_{qg}^{(1)}(x) = T(F) \left[ (1-x)^2 + x^2 \right]$$



$$P_{gg}^{(1)}(x) = 2C_2(A) \left[ \frac{x}{(1-x)_+} + \frac{1-x}{x} + x(1-x) \right] + \left( \frac{11}{6} C_2(A) - \frac{2}{3} T(F) n_f \right) \delta(1-x),$$

$$z_{min} = \omega^{min} / E_T$$

Collinear divergence requires Sudakov resummation:

$$\begin{aligned} P(< r) &= \exp(-P_1(> r)) \\ &= \exp\left(-\int_r^R dr' \psi_{coll}(r')\right) \end{aligned}$$

13

$$\psi_{RS}(r) = \frac{dP(r)}{dr}$$

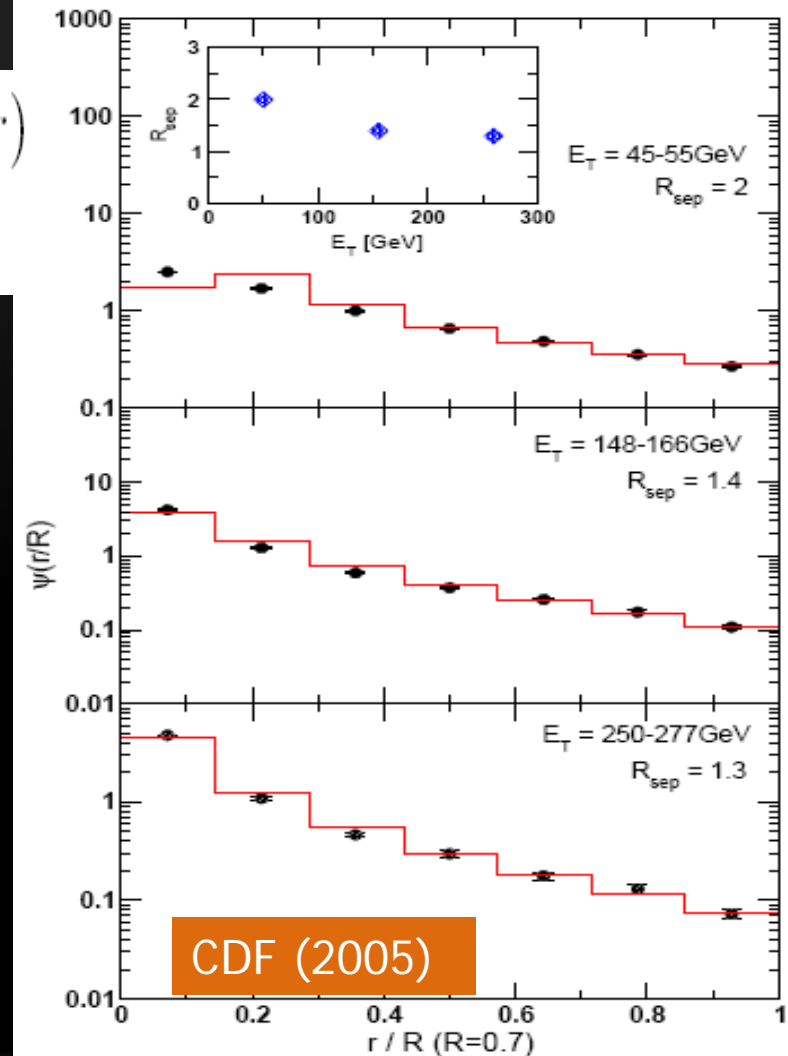
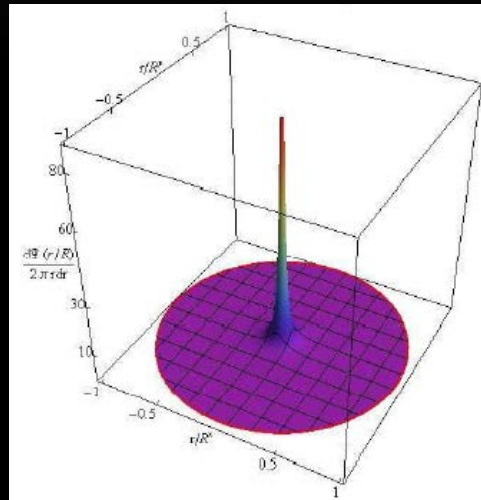
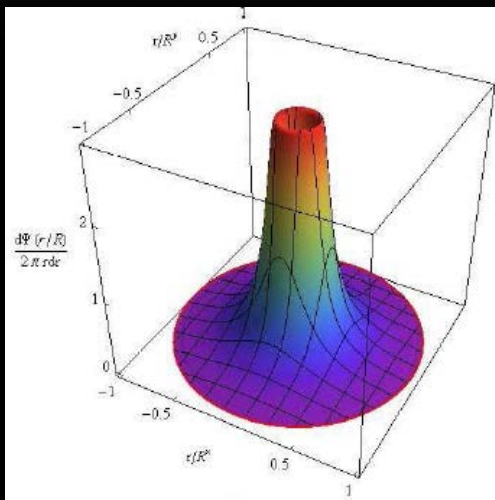
# Jet shape p+p: baseline

$$\psi(r) = \psi_{\text{coll}}(r) (P(r) - 1) + \psi_{\text{LO}}(r) + \psi_{i,\text{LO}}(r) + \psi_{\text{PC}}(r) + \psi_{i,\text{PC}}(r),$$

LHC

20 GeV

500 GeV



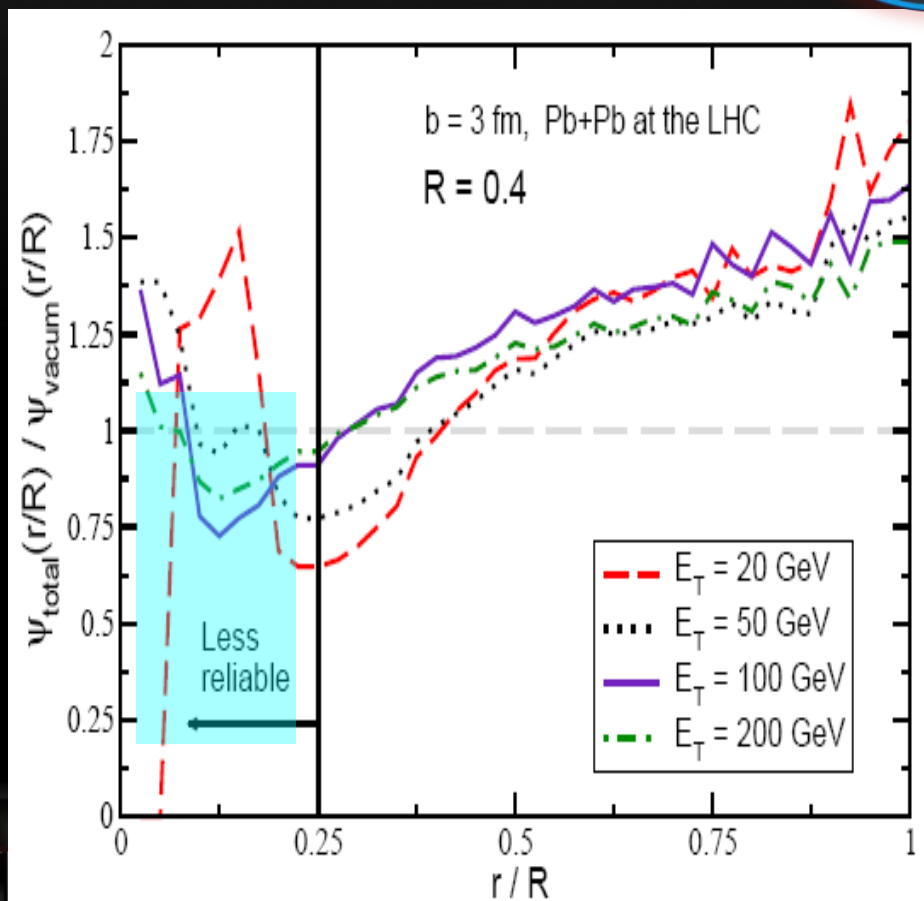
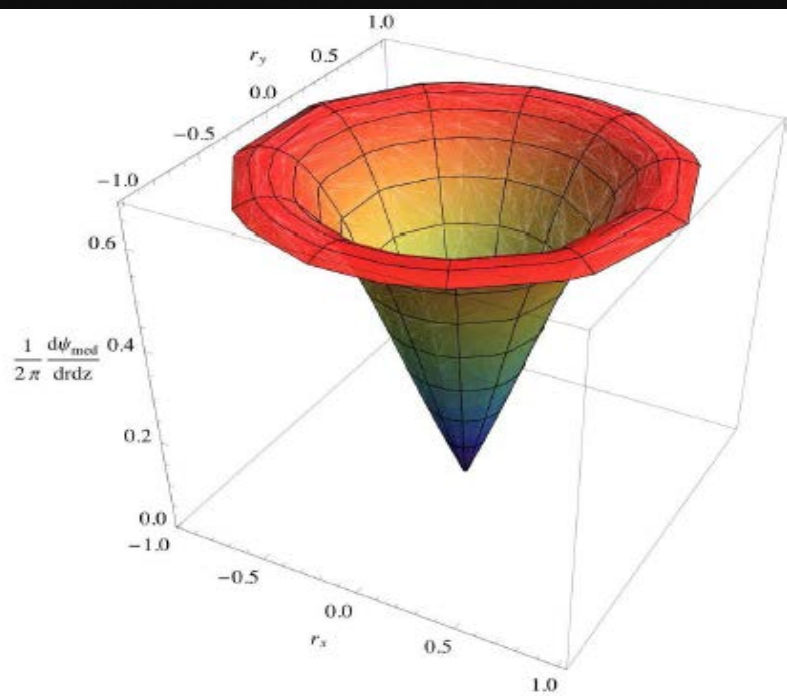
I Vitev, S Wicks, BWZ, JHEP 0811,093 (2008)

$\sqrt{s} = 1960 \text{ GeV}$

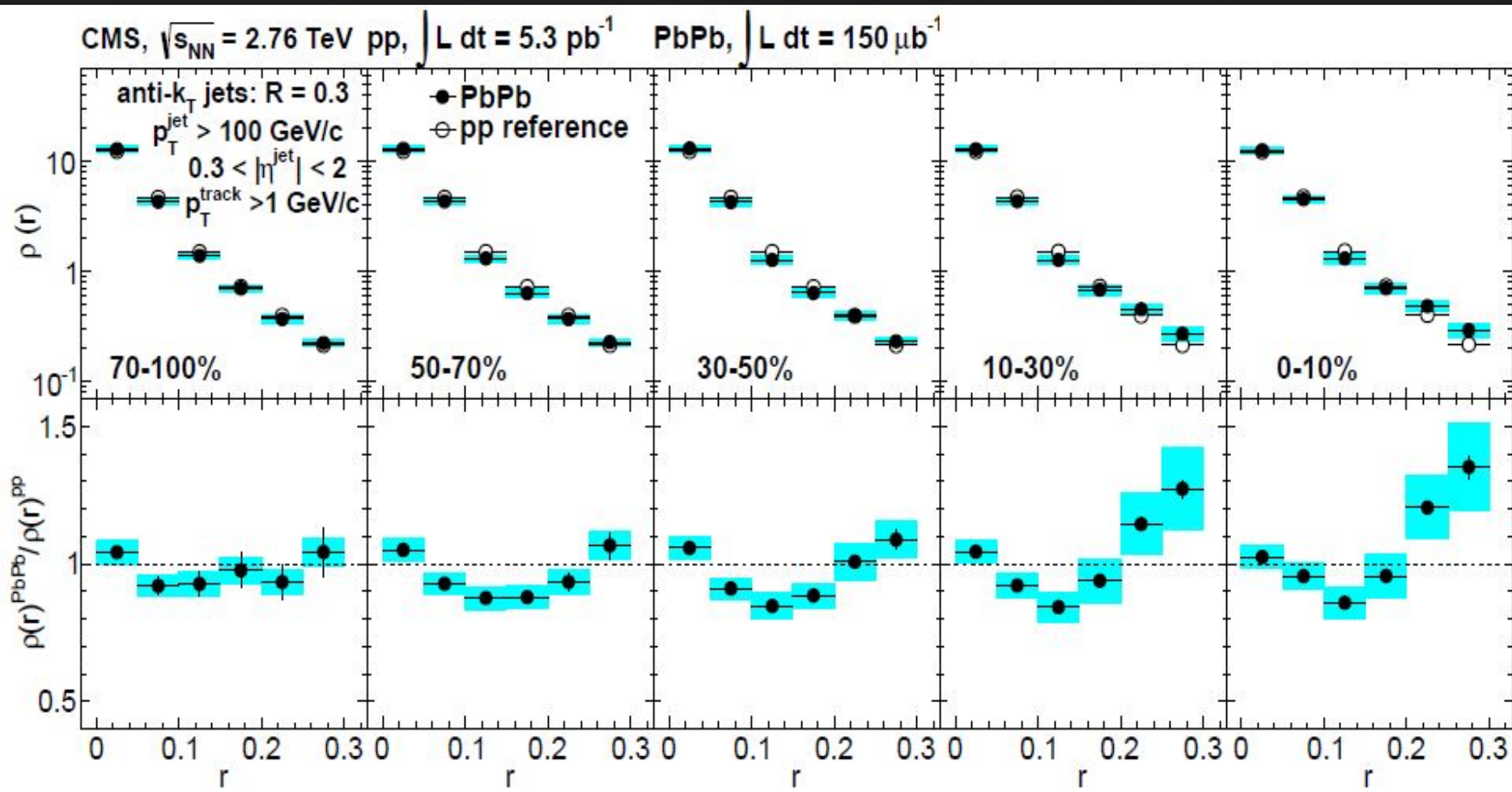
# Total jet shape in HIC

Medium-induced jet shape is much broader than the jet shape in p+p

$$\psi_{\text{tot.}}(r/R) = \frac{1}{\text{Norm}} \int_{\epsilon=0}^1 d\epsilon \sum_{q,g} P_{q,g}(\epsilon) \frac{1}{(1 - (1 - f_{q,g}) \cdot \epsilon)^3} \times \frac{\sigma_{q,g}^{NN}(R, \omega^{\min})}{d^2 E'_T dy} \left[ (1 - \epsilon) \psi_{\text{vac.}}^{q,g}(r/R) + f_{q,g} \cdot \epsilon \psi_{\text{med.}}^{q,g}(r/R) \right]$$



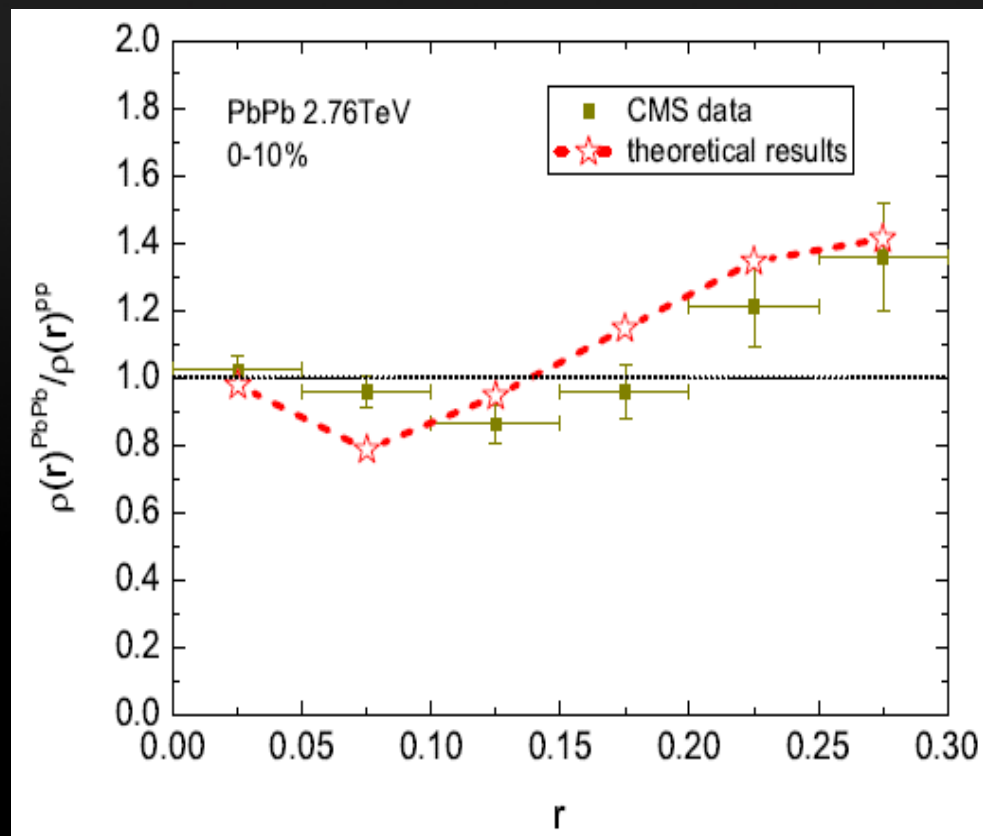
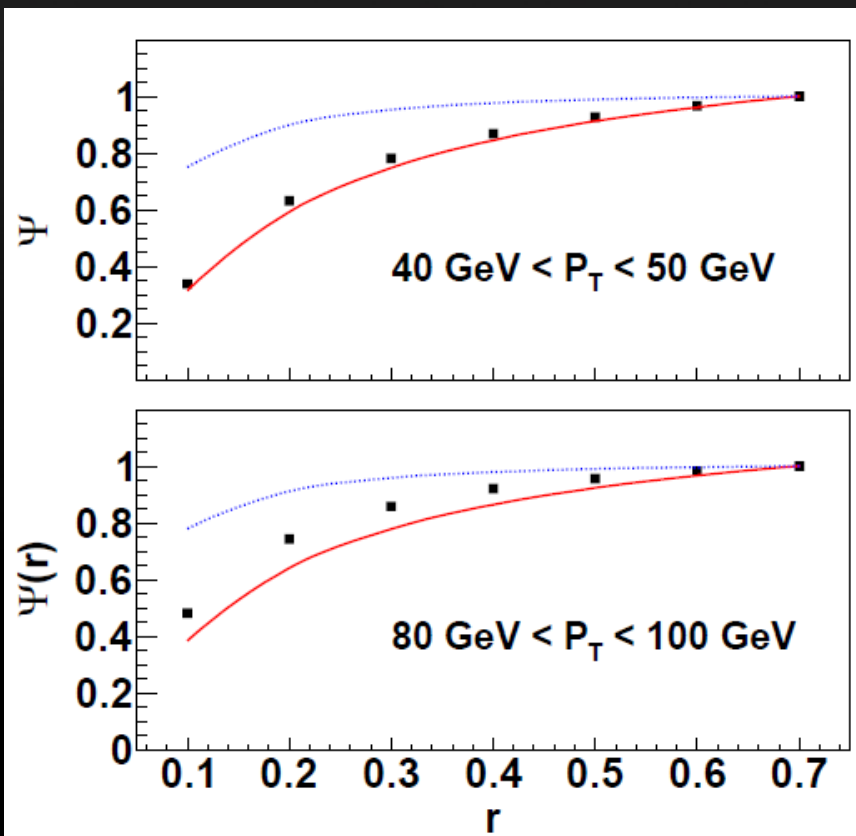
# Jet shapes measured at LHC



CMS, arXiv:1310.0878



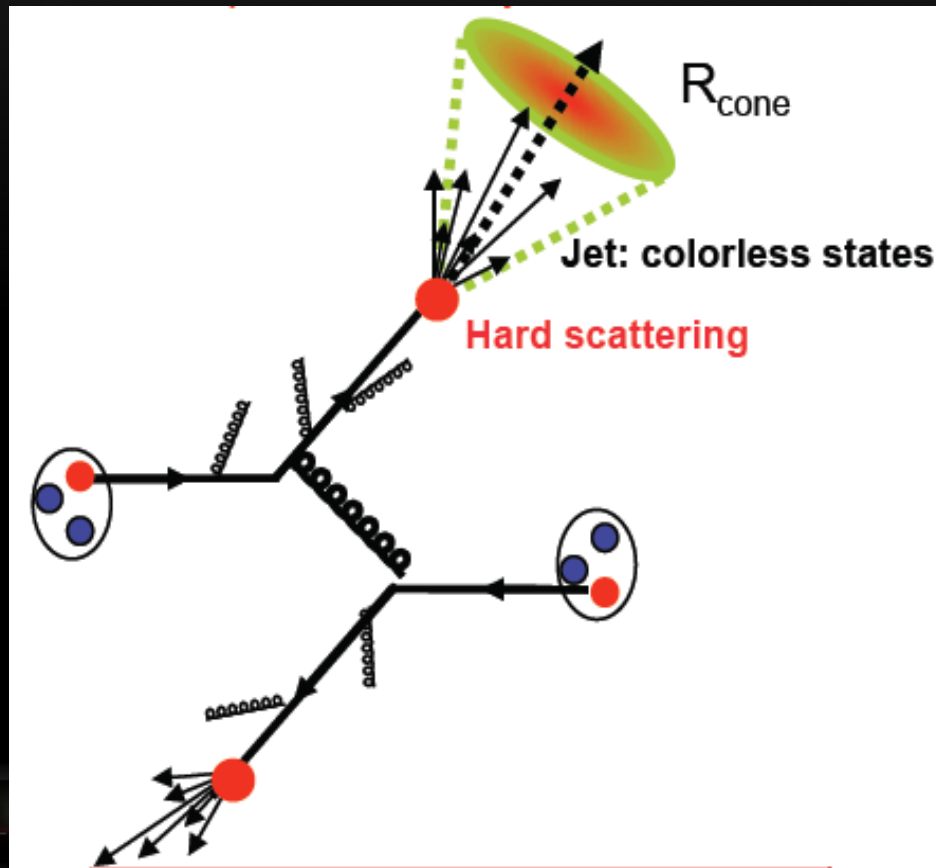
# Jet shapes: NLL+NLO



H-N Li, Z Li, C P Yuan,  
PRL (2011); PRD (2012)

S Chen, Z Li, BWZ,  
in progress

# Inclusive jet cross section in HIC



# Jet cross section at NLO in p+p

- Jet cross sections at NLO in p+p :

$$\frac{d\sigma^{\text{jet}}}{dE_T dy} = \frac{1}{2!} \int d\{E_T, y, \phi\}_2 \frac{d\sigma[2 \rightarrow 2]}{d\{E_T, y, \phi\}_2} S_2(\{E_T, y, \phi\}_2) + \frac{1}{3!} \int d\{E_T, y, \phi\}_3 \frac{d\sigma[2 \rightarrow 3]}{d\{E_T, y, \phi\}_3} S_3(\{E_T, y, \phi\}_3)$$

- Function  $S_2$  and  $S_3$  contain jet find algorithm:

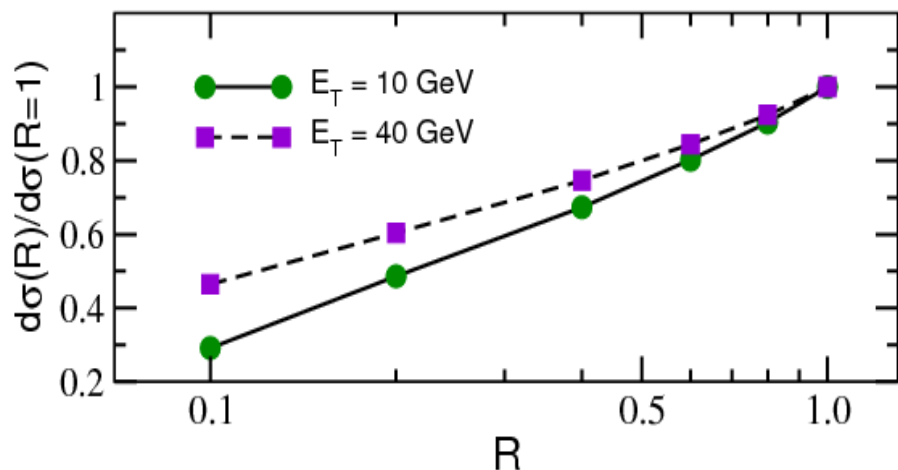
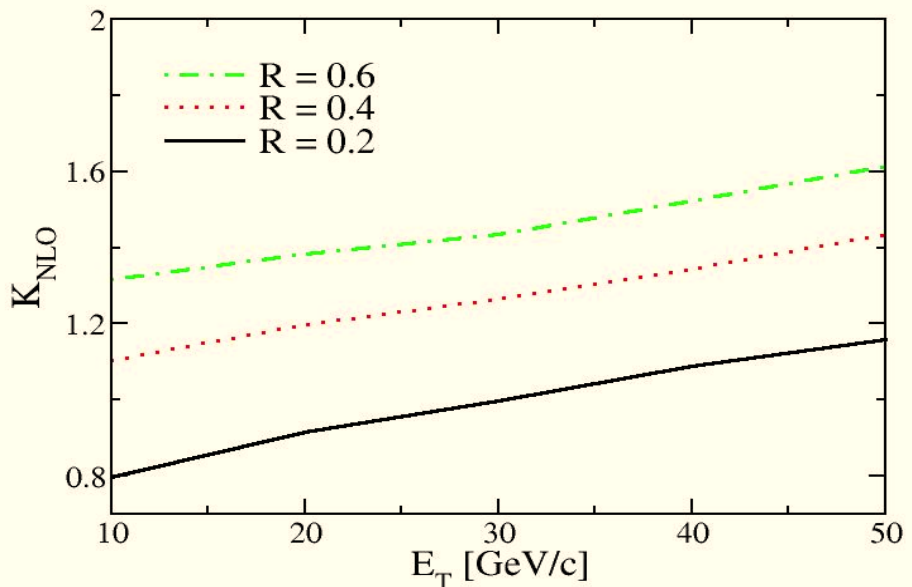
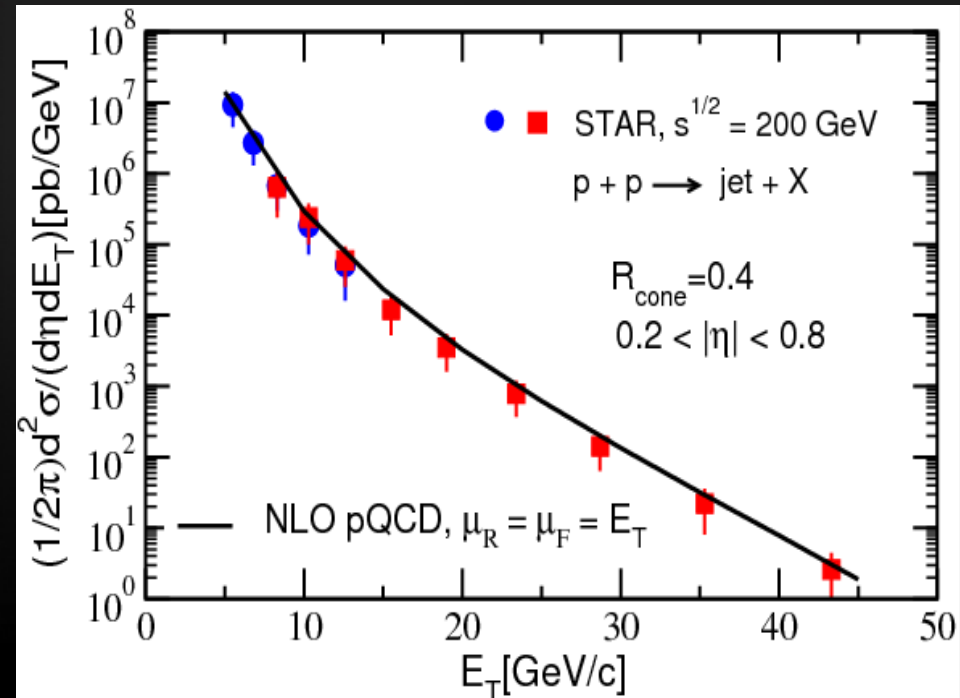
2 --> 2

$$S_2 = \sum_{i=1}^2 S(i) = \sum_{i=1}^2 \delta(E_{T_i} - E_T) \delta(y_i - y)$$

2 --> 3

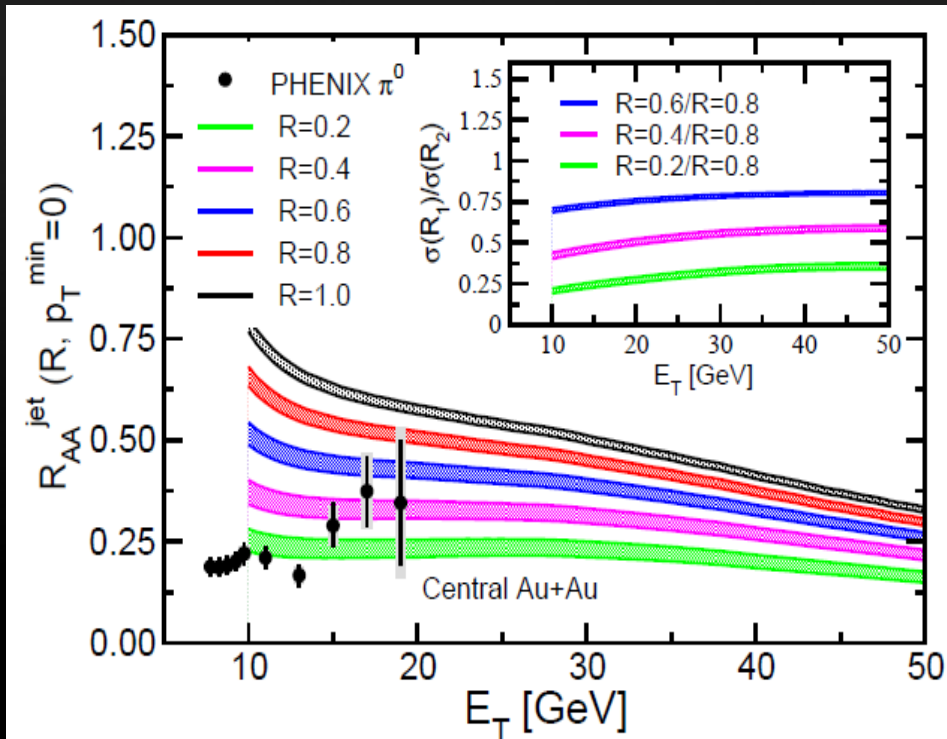
$$S_3 = \sum_i \delta(p_i - p_J) \delta(y_i - y_J) \prod_{j(j \neq i)} \theta \left( R_{ij} > \frac{p_i + p_j}{\max(p_i, p_j)} R \right) + \sum_{i,j(i < j)} \delta(p_i + p_j - p_J) \delta \left( \frac{p_i y_i + p_j y_j}{p_i + p_j} - y_J \right) \theta(R_{ij} < R_{\text{rc}})$$

# Inclusive jet in p+p at NLO

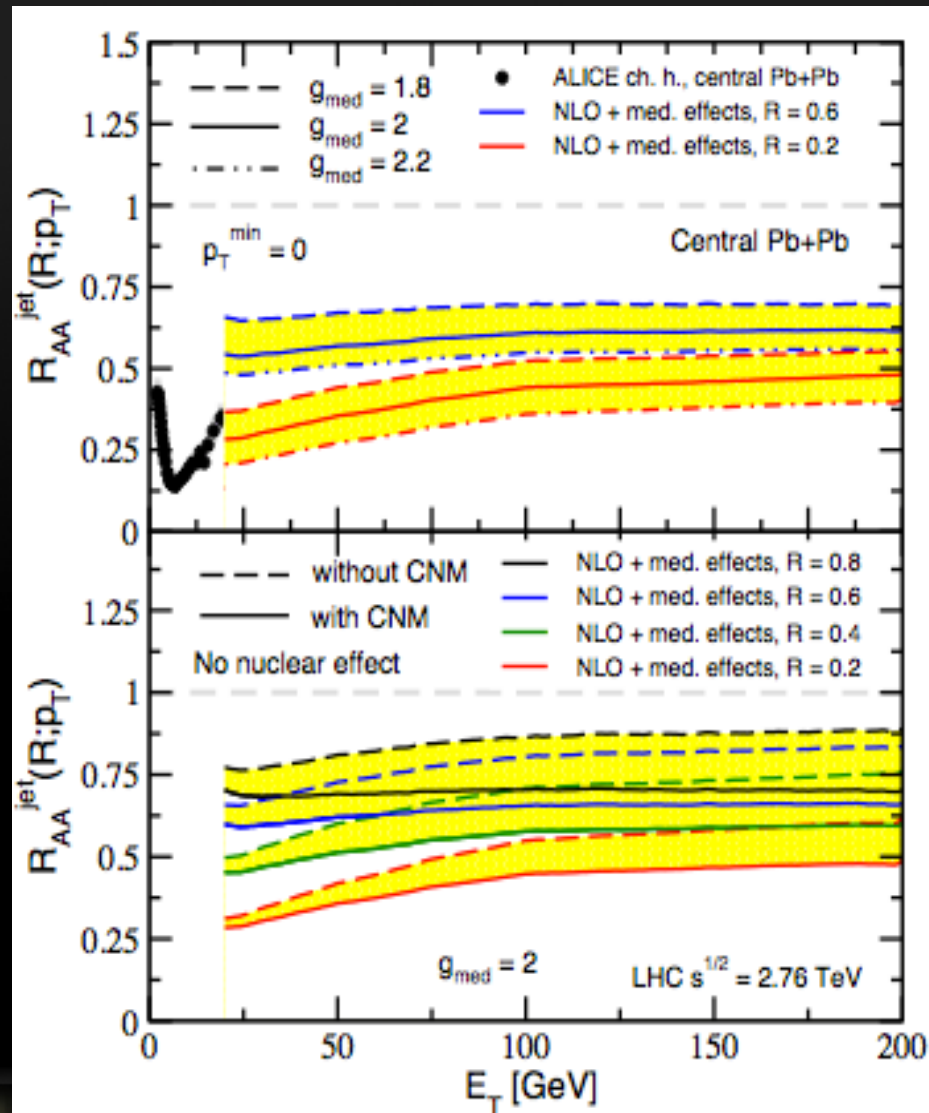


- Very good agreement between data and theory is achieved;
- $K_{\text{NLO}} = \text{NLO}/\text{LO}$  can be smaller than 1 at small cone radius.

# Inclusive jets in A+A at RHIC



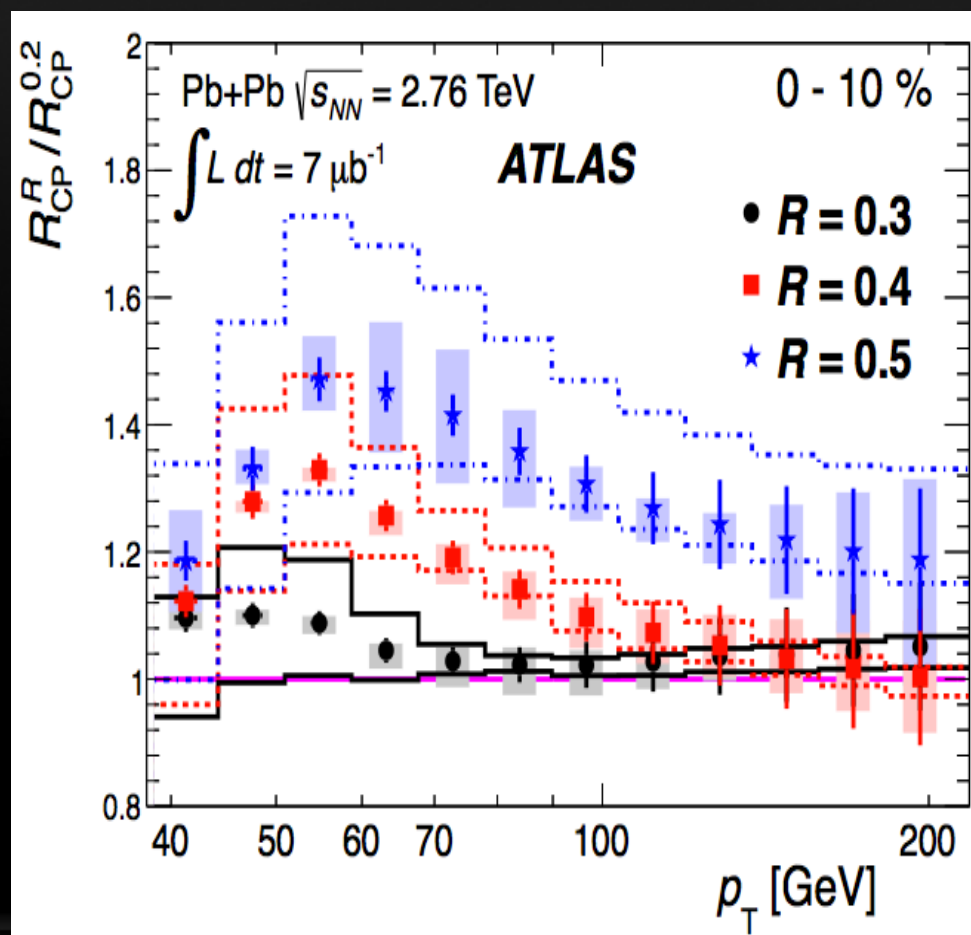
I Vitev, BWZ, PRL (2010).



Y He, Vitev, BWZ, PLB (2012)

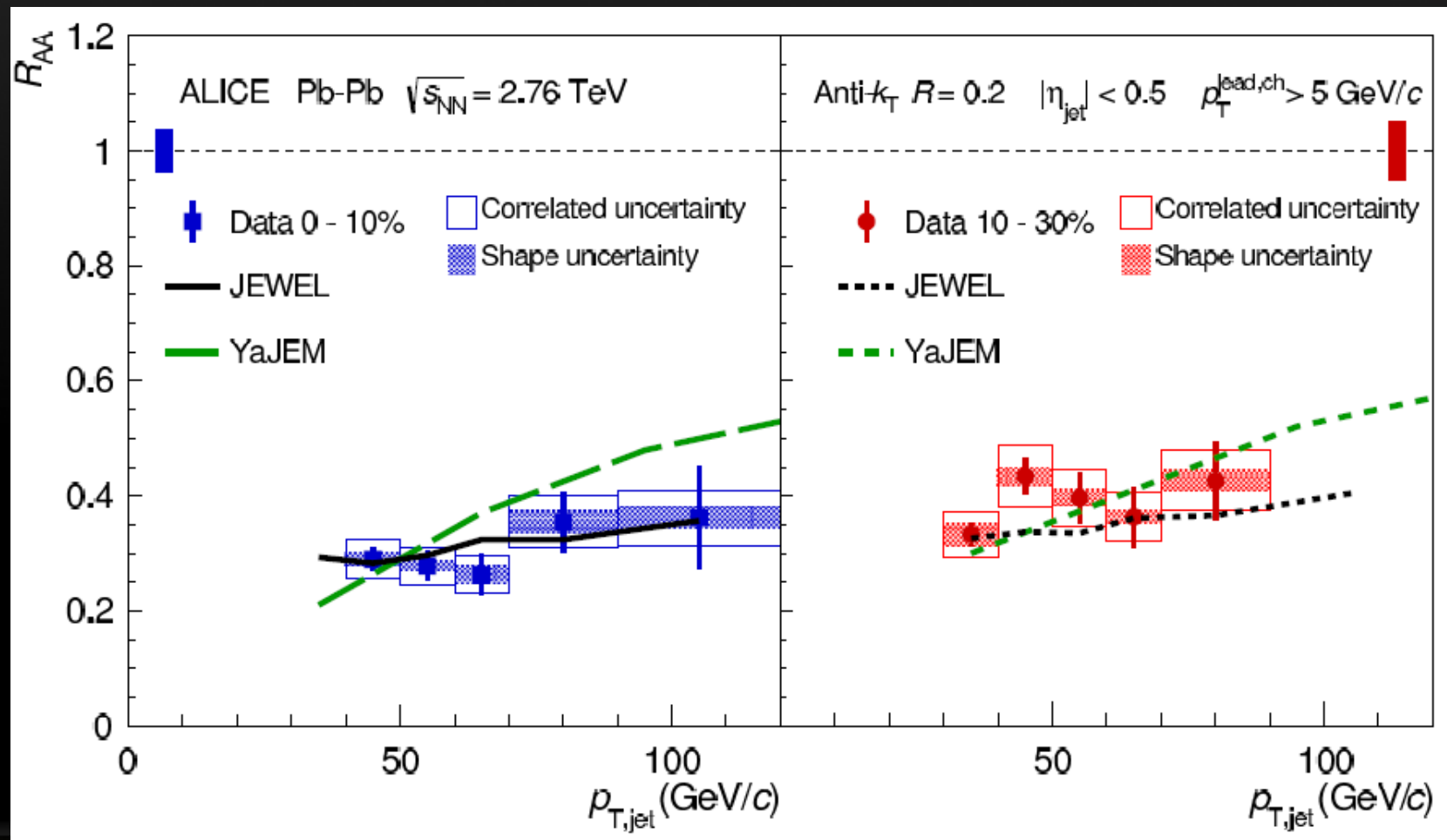
# Inclusive jet in Pb+Pb: Exp.

- The jet radius dependence of  $R_{AA}$  on inclusive jets has been confirmed by ATLAS measurements most recently.

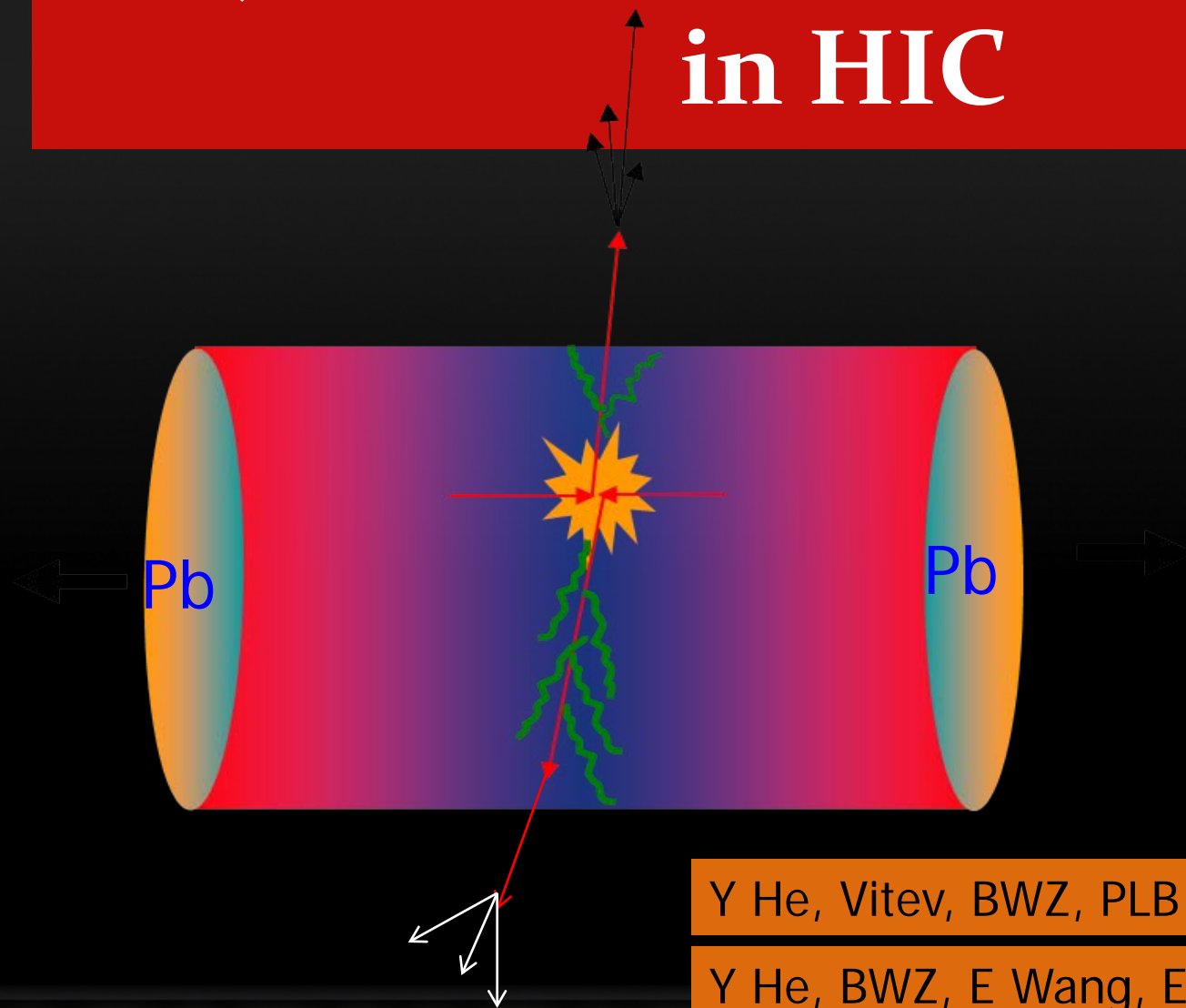


# Inclusive jet in Pb+Pb: Exp.

- Inclusive jet  $R_{AA}$  has also recently measured by ALICE.



# Dijet momentum imbalance in HIC



Y He, Vitev, BWZ, PLB (2012)

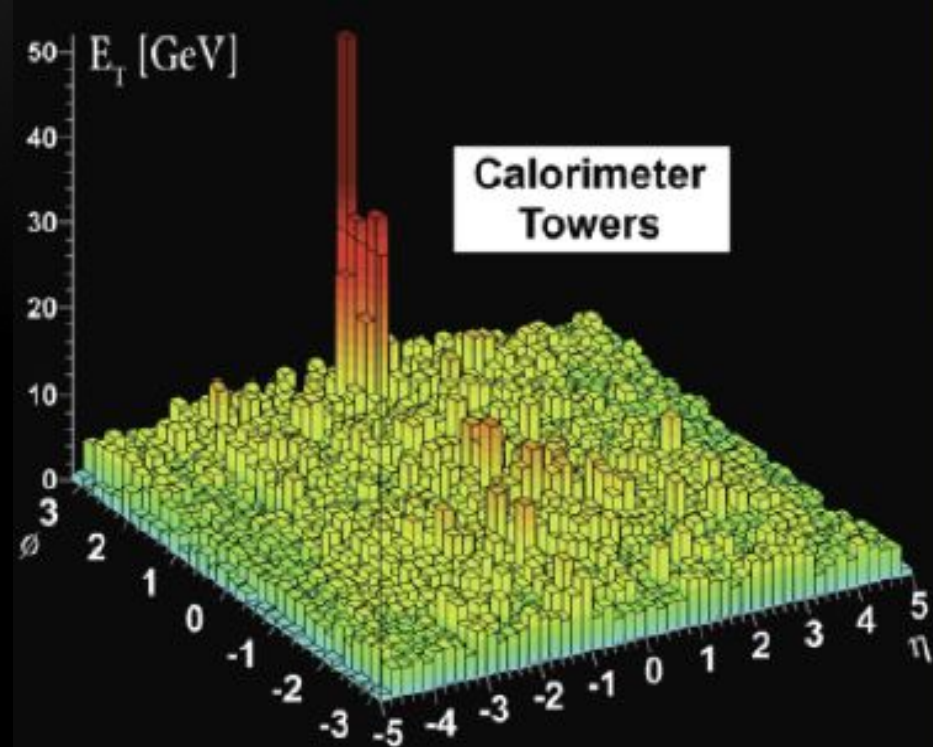
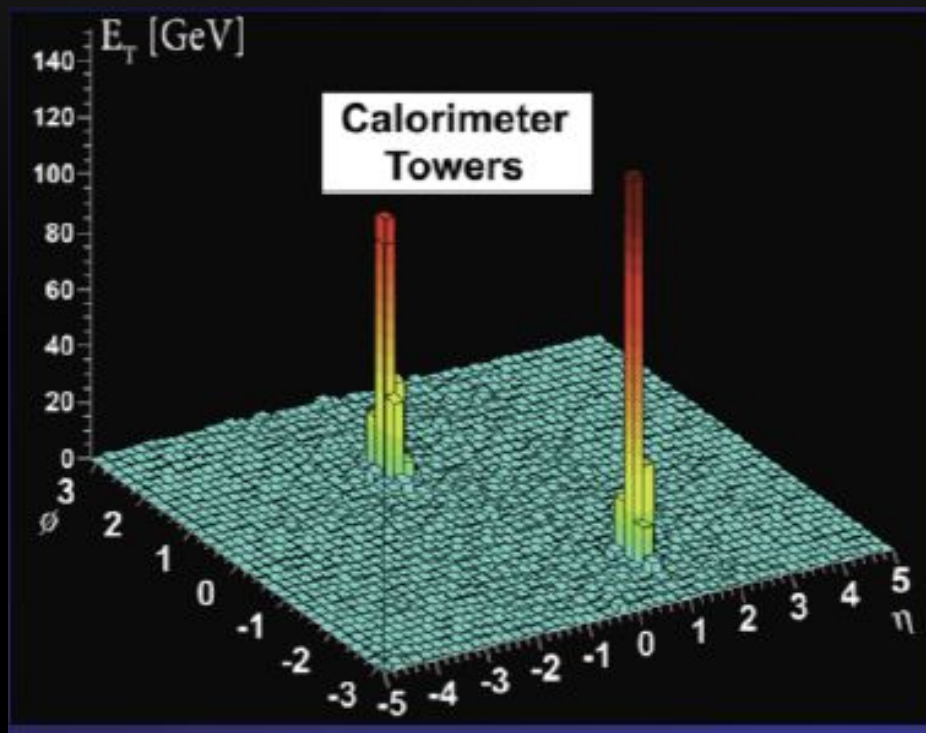
Y He, BWZ, E Wang, EJPC (2012)

Y He, Neufeld, Vitev, BWZ, in preparation



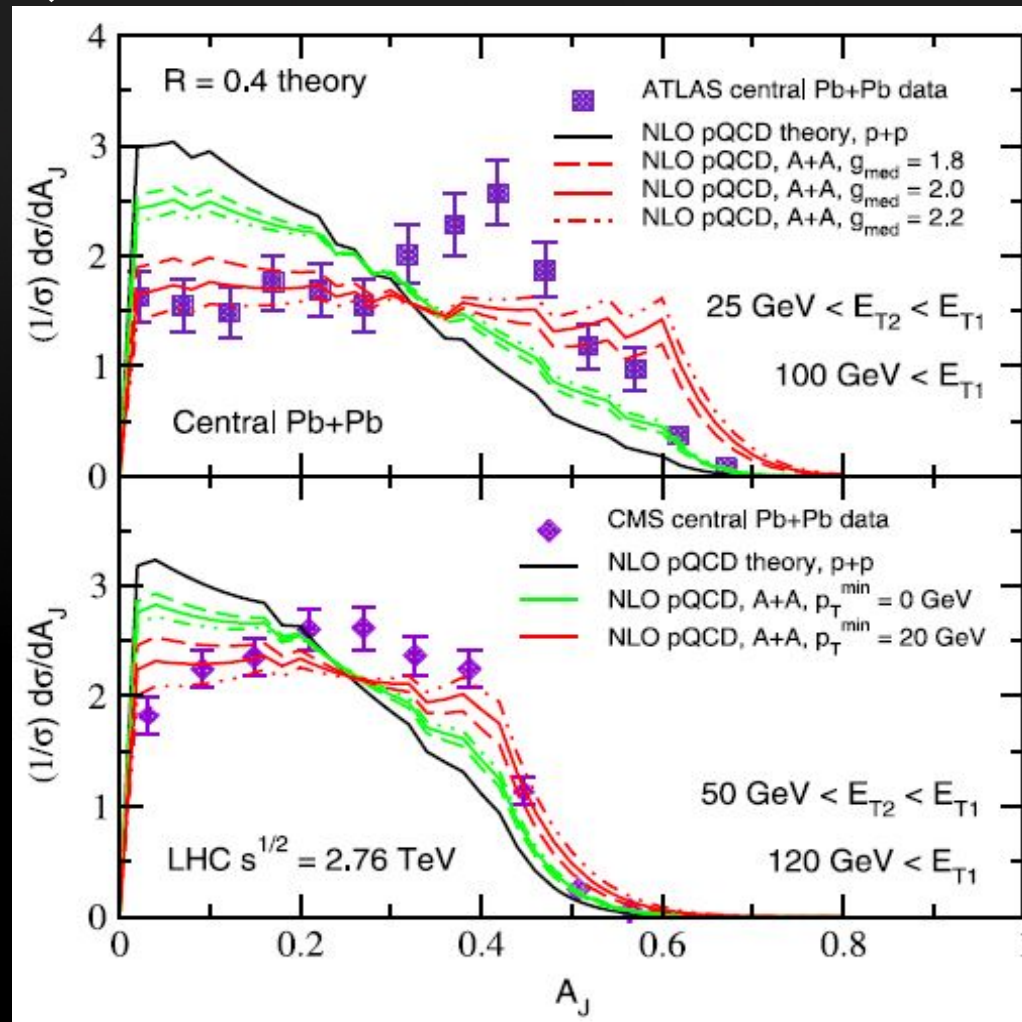
# Measuring Dijets in Pb+Pb

- Jet quenching at LHC has been observed for the first time in dijet productions at Pb+Pb by ATLAS and CMS.



# Dijet in Pb+Pb at LHC

$$A_J = \frac{E_{T1} - E_{T2}}{E_{T1} + E_{T2}}$$



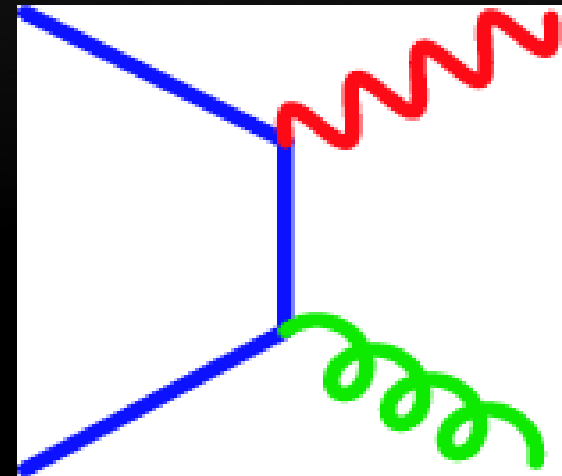
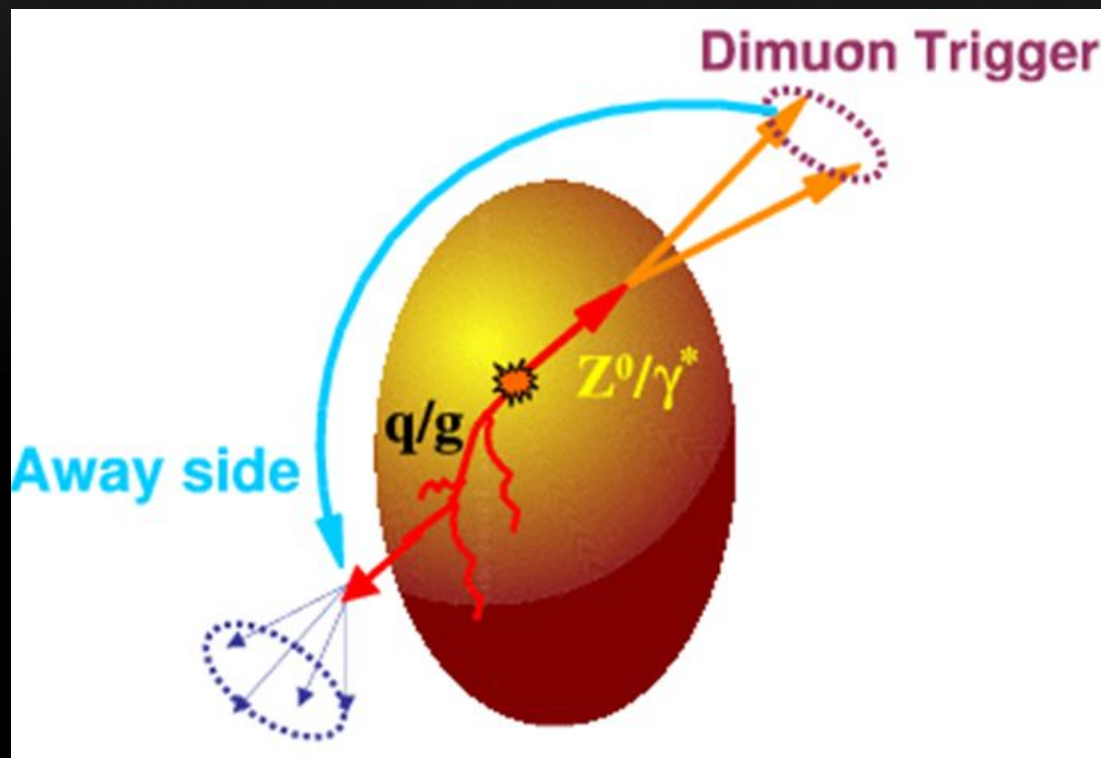
Y He, Vitev, BWZ, PLB (2012)

G Qin, B Muller, PRL (2011)

ATLAS, arXiv:1011.6182, PRL (2011);

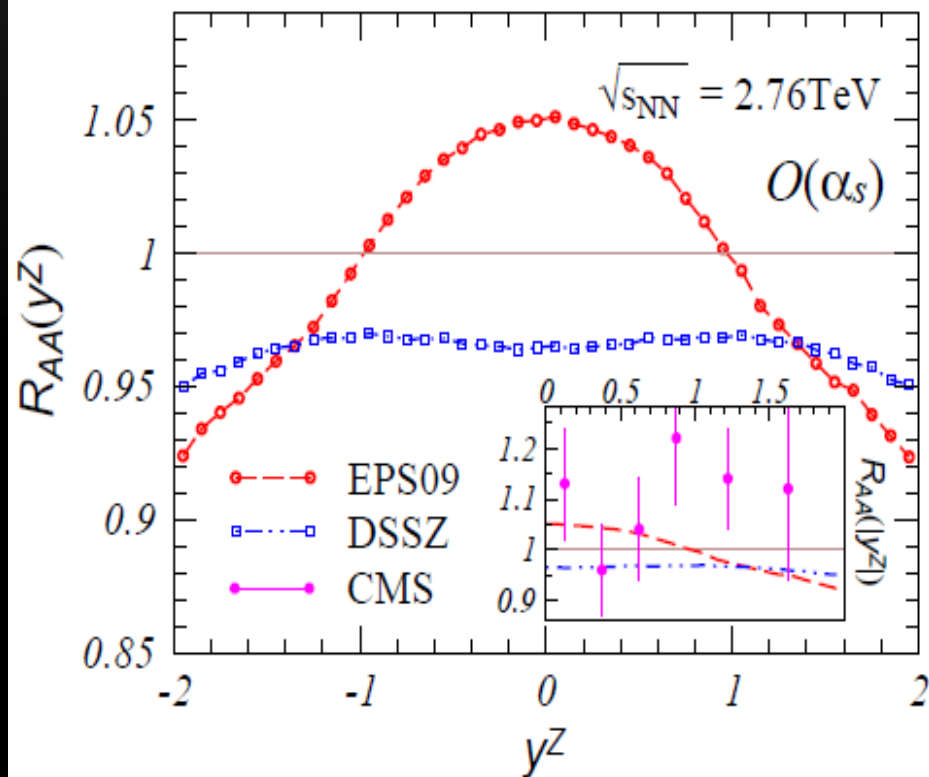
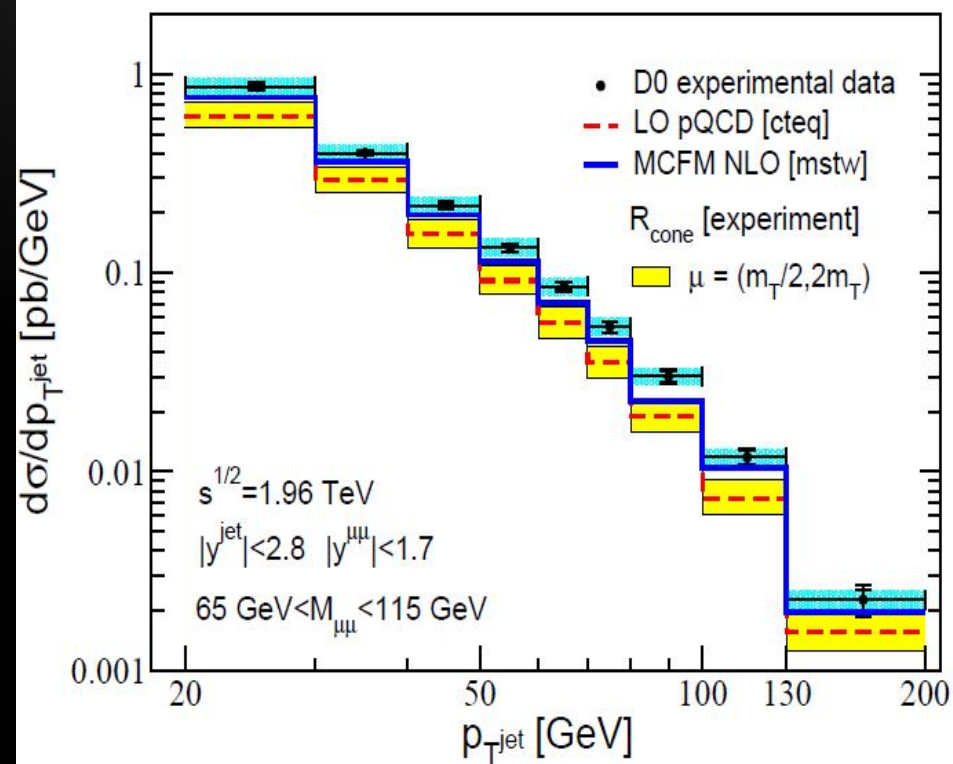
CMS, arXiv: 1102.1957, PRC (2012)

# Tagged jet production in HIC



# Z<sup>0</sup> in pp and PbPb

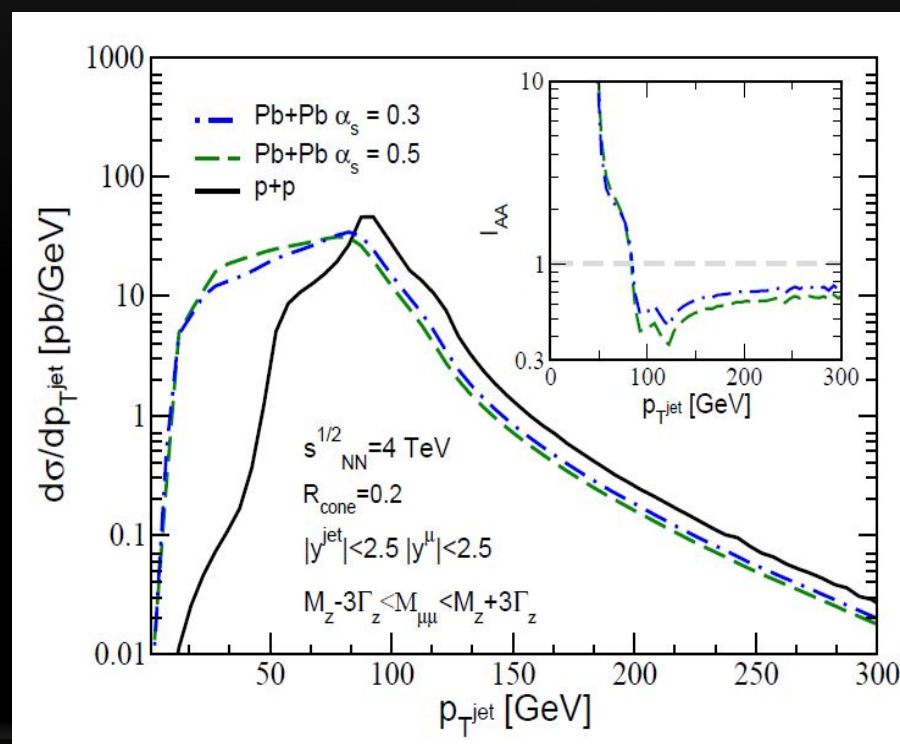
- pQCD gives a good description of the data at the LHC and DO.
- The CNM effects for Z boson is small.



# Z<sup>0</sup> + jet in A+A: I<sub>AA</sub>

- A sharp transition from tagged jet suppression above  $\sim p_T$  of Z to tagged jet enhancement below  $\sim p_T$  of Z

$$I_{AA}^{\text{jet}}(R, \omega_{\min}) = \frac{1}{\langle N_{\text{bin}} \rangle} \frac{d\sigma_{AA}}{dp_T(Z) dp_T(Q)} \bigg/ \frac{d\sigma_{pp}}{dp_T(Z) dp_T(\text{jet})}$$



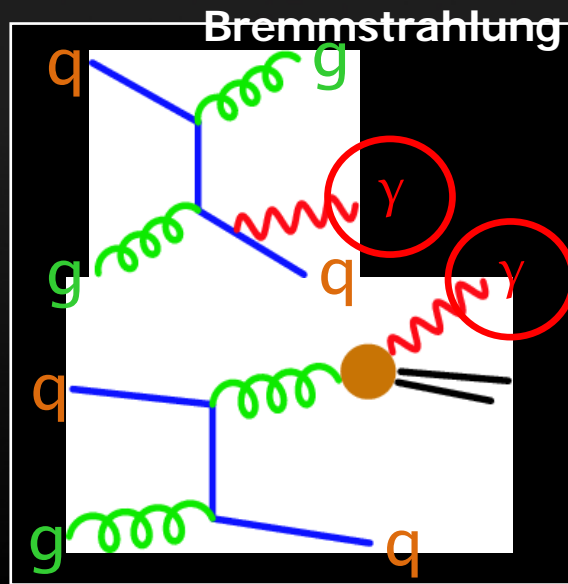
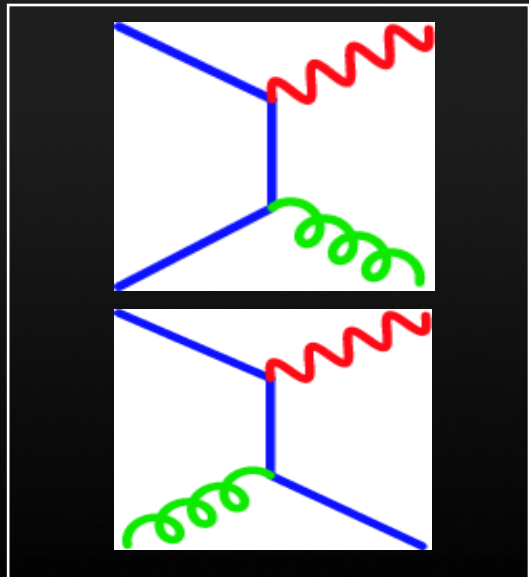
# Prompt photon in pp collisions

**LO**

Annihilation

$\alpha\alpha_s$

Compton



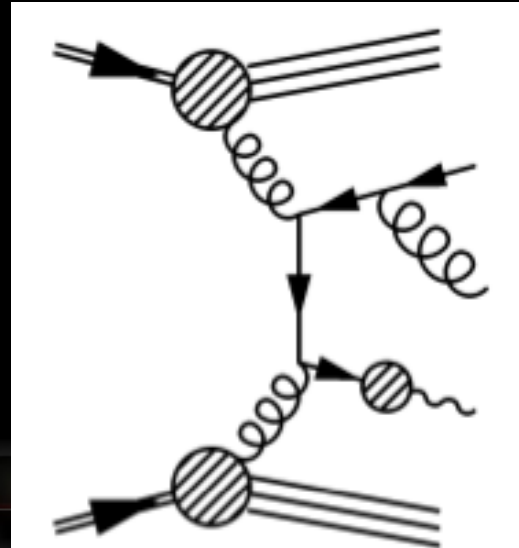
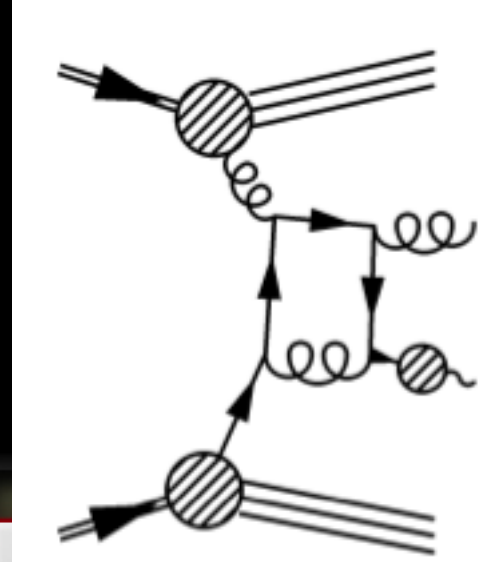
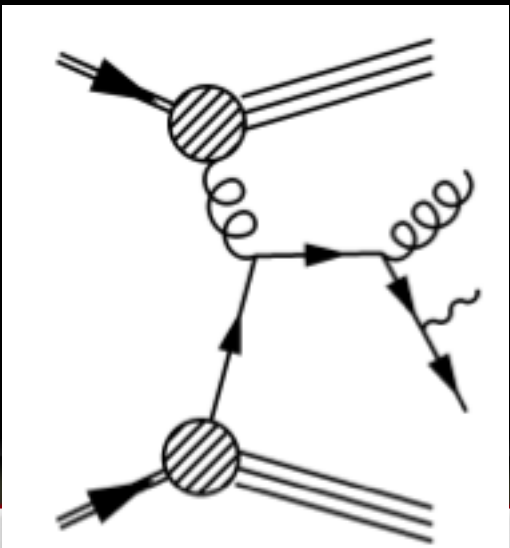
$$\alpha_s(Q) \propto \ln^{-1}\left(\frac{Q^2}{\Lambda^2}\right)$$

$$D_{\gamma/c}(z, Q^2) \propto \ln\left(\frac{Q^2}{\Lambda^2}\right)$$

$$\alpha\alpha_s^2 D_{\gamma/c} \propto \alpha\alpha_s$$

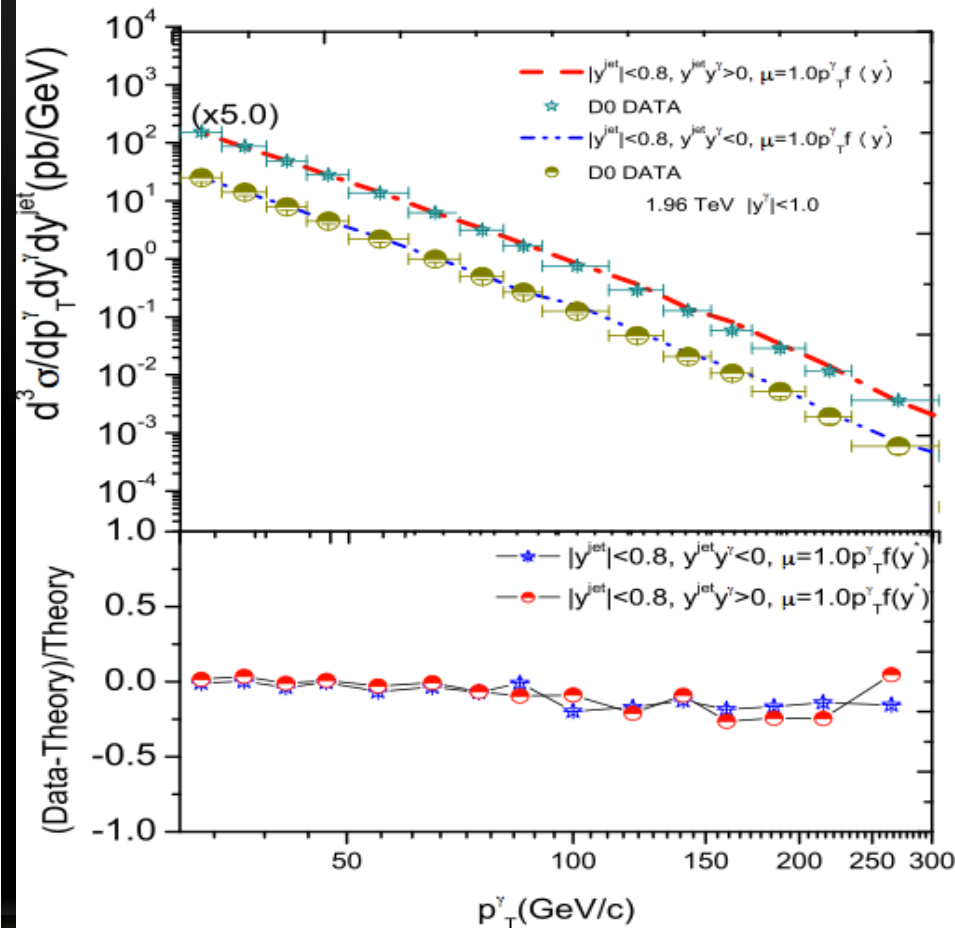
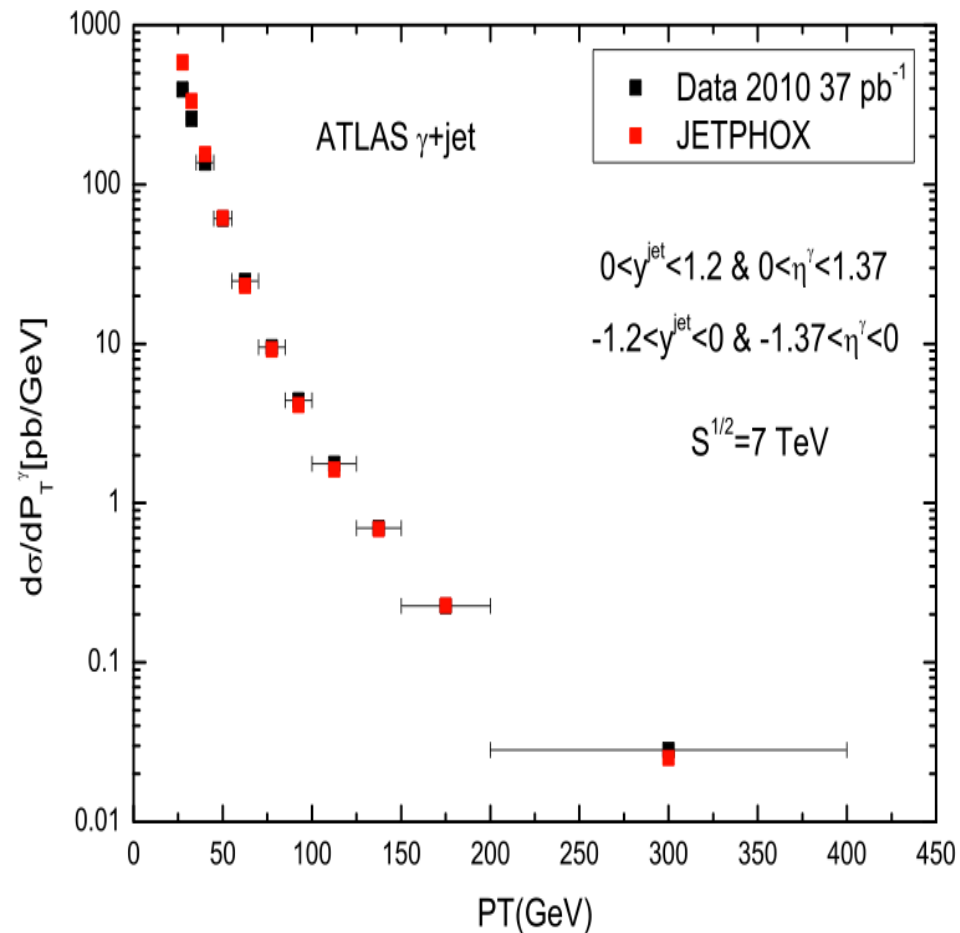
**NLO**

$\alpha\alpha_s^2$

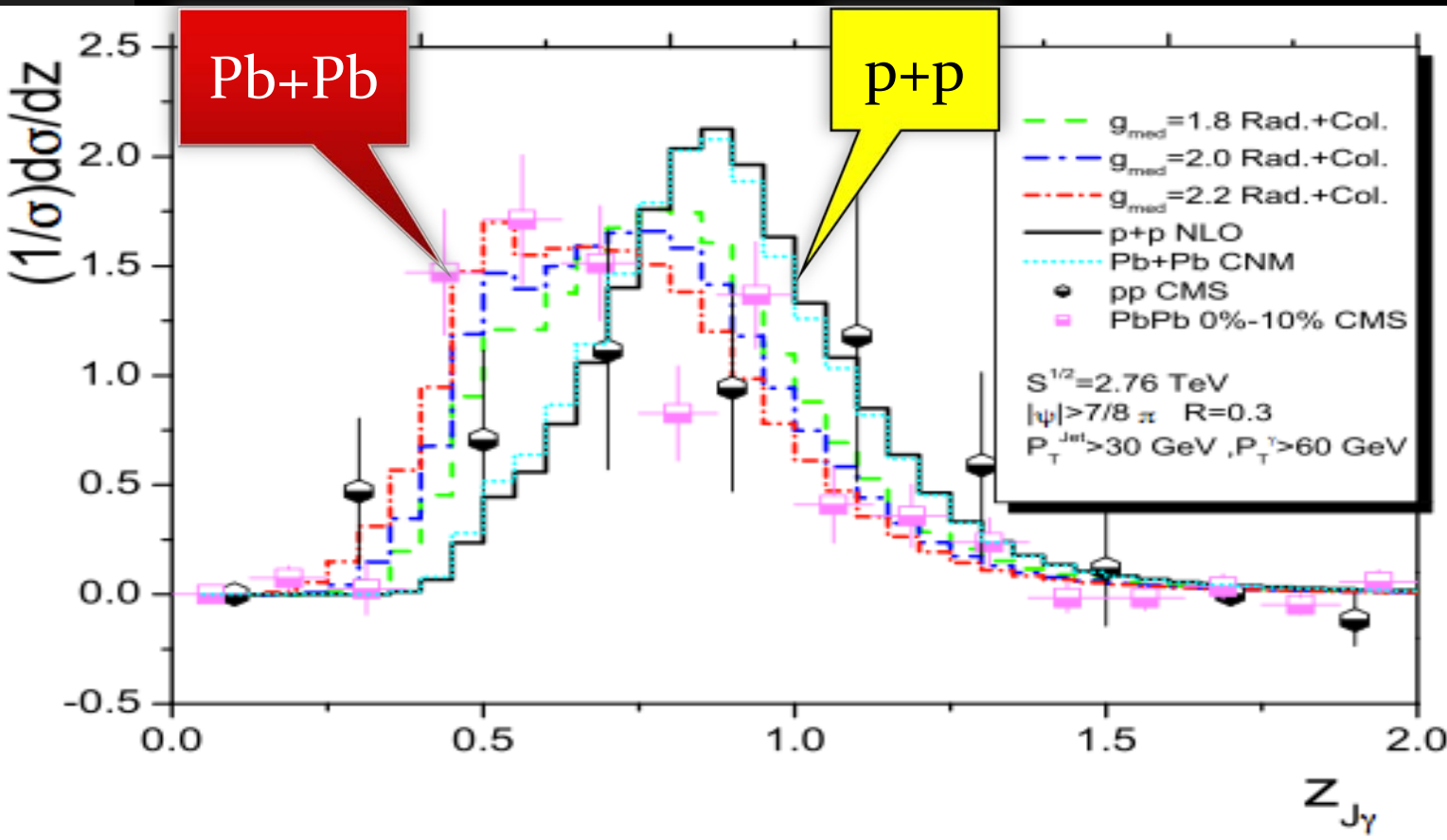


# Photon + jet in p+p at NLO

- A good baseline for photon+jet in hadron-hadron production has been given by the NLO pQCD.



# Asymmetry in photon + jet



$$z_{J\gamma} = \frac{p_{T,jet}}{p_{T,\gamma}}$$

System	$\langle z_{J\gamma} \rangle_{LHC}$	$\langle z_{J\gamma} \rangle_{RHIC}$
p+p	0.94	0.90
A+A, CNM	0.94	0.89
A+A, $g_{med} = 1.8$ , Rad.+Col.	0.84	0.78
A+A, $g_{med} = 2.0$ , Rad.+Col.	0.80	0.74
A+A, $g_{med} = 2.2$ , Rad.+Col.	0.71	0.70

CMS, PLB(2013)

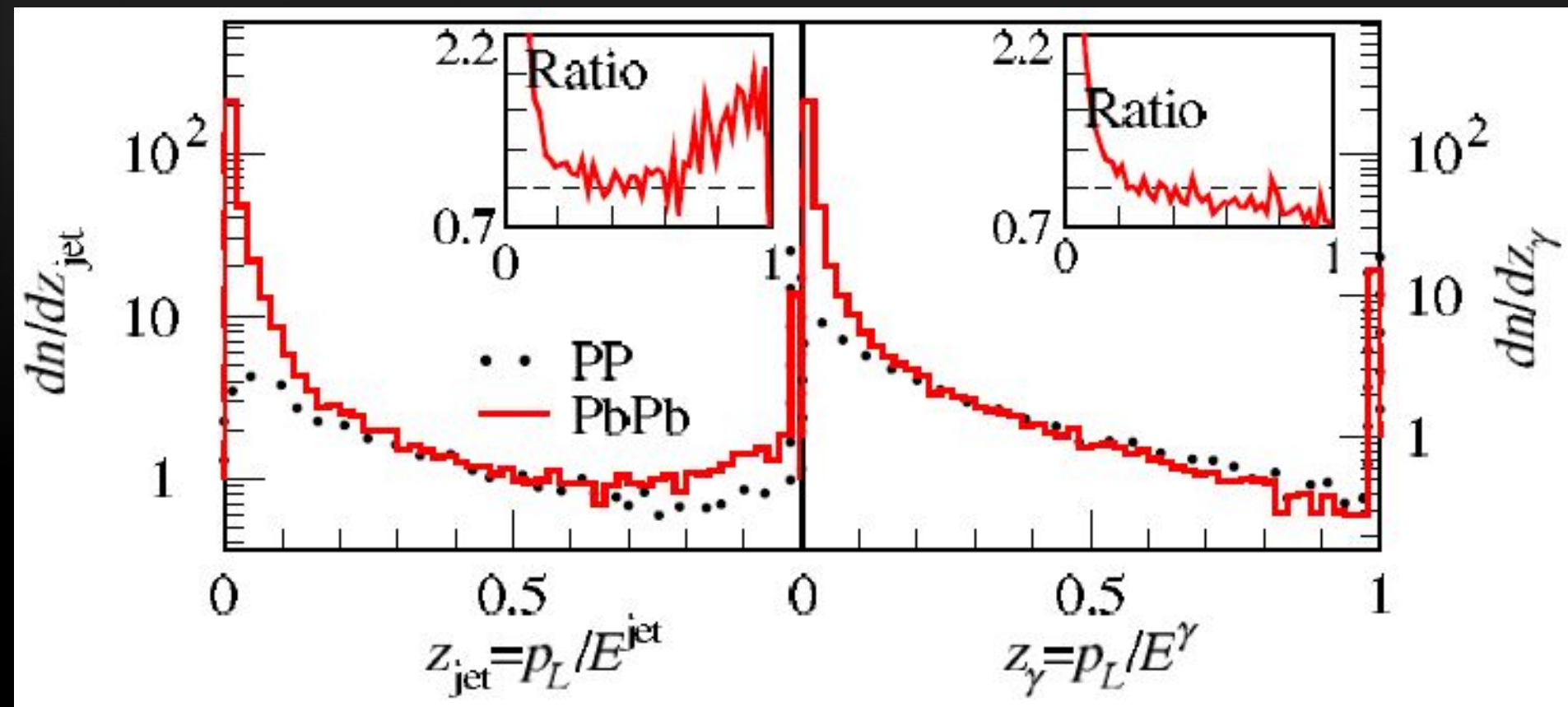
$\langle z_{J\gamma} \rangle = 0.73 \pm 0.02$

Dai, Vitev, BWZ, PRL(2013)



# photon + jet with LBT

$$p \cdot \partial f(p) = -C(p)$$

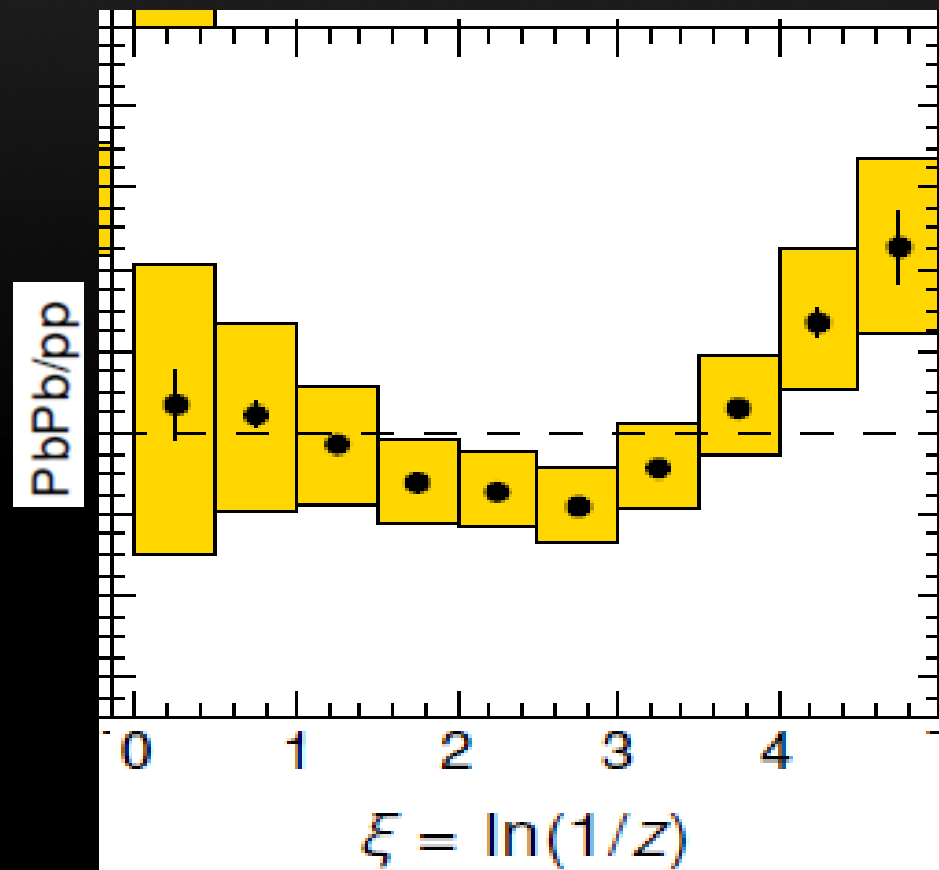
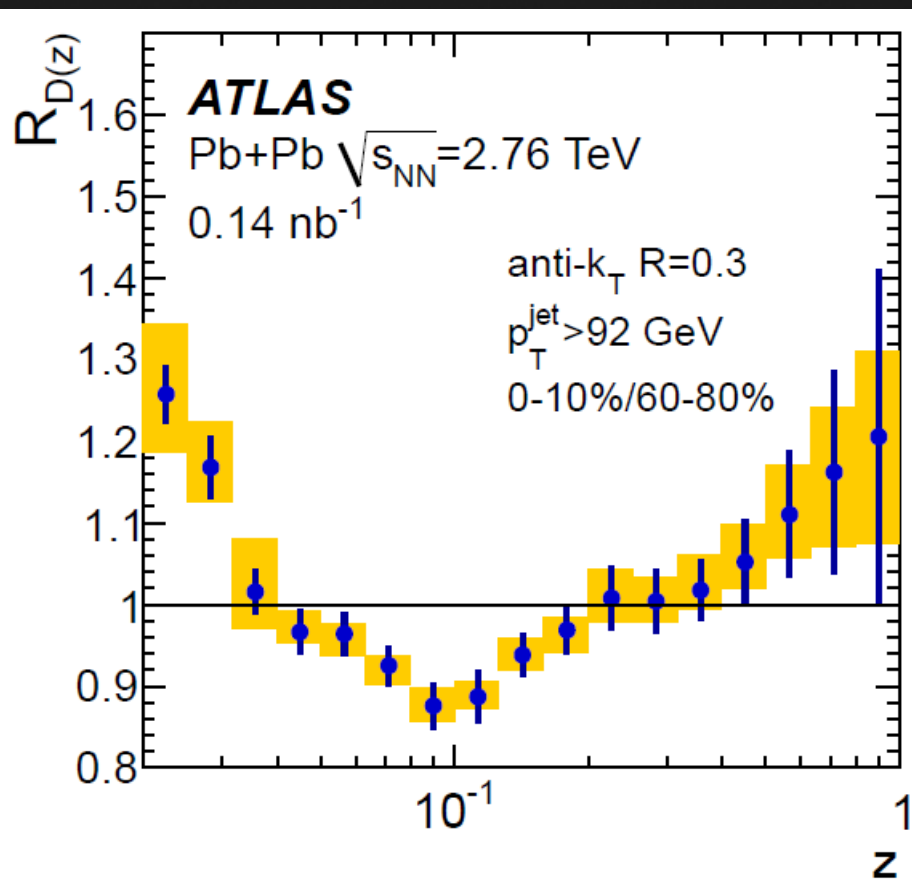


Xin-Nian Wang, Yan Zhu, PRL (2013)

# Jet Fragmentation Function

$$D(z) \equiv \frac{1}{N_{\text{jet}}} \frac{dN_{\text{ch}}}{dz}$$

$$z = p_T^h / p_T^{\text{jet}}$$



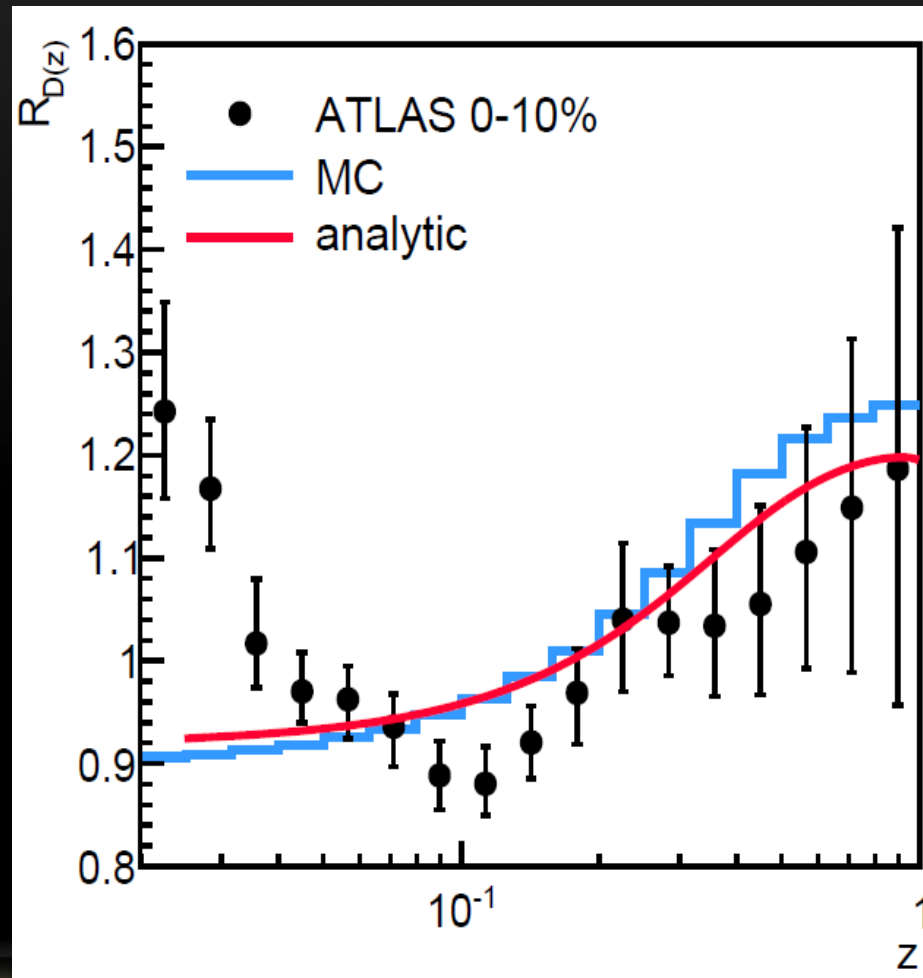
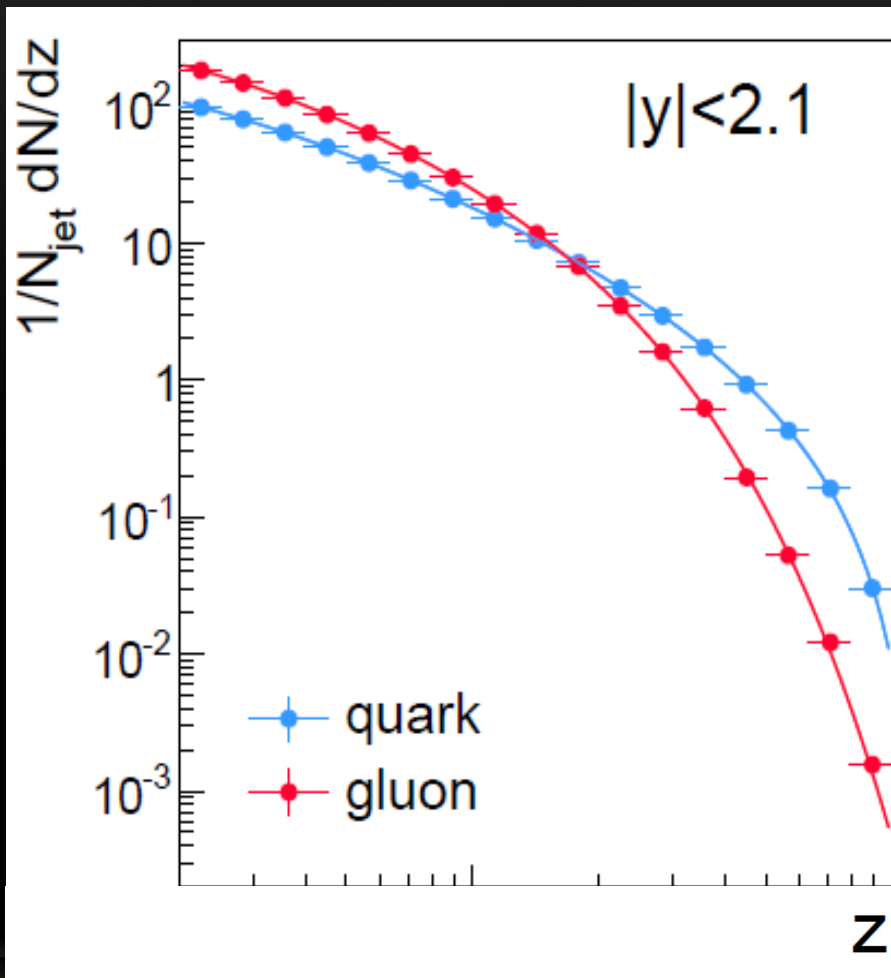
ATLAS, 1406.2979

CMS, 1406.0932

# Jet FF: Quark VS Gluon

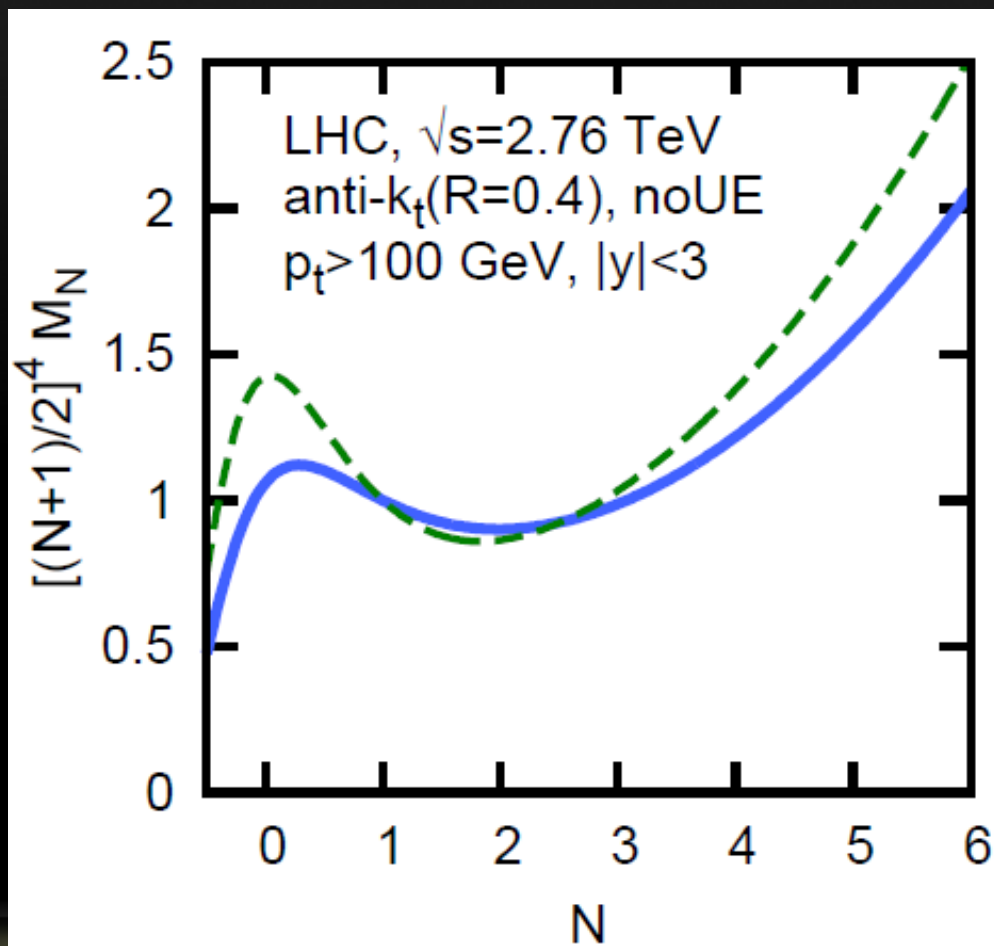
$$D(z) \equiv \frac{1}{N_{\text{jet}}} \frac{dN_{\text{ch}}}{dz}$$

$$z = p_T^h / p_T^{\text{jet}}$$

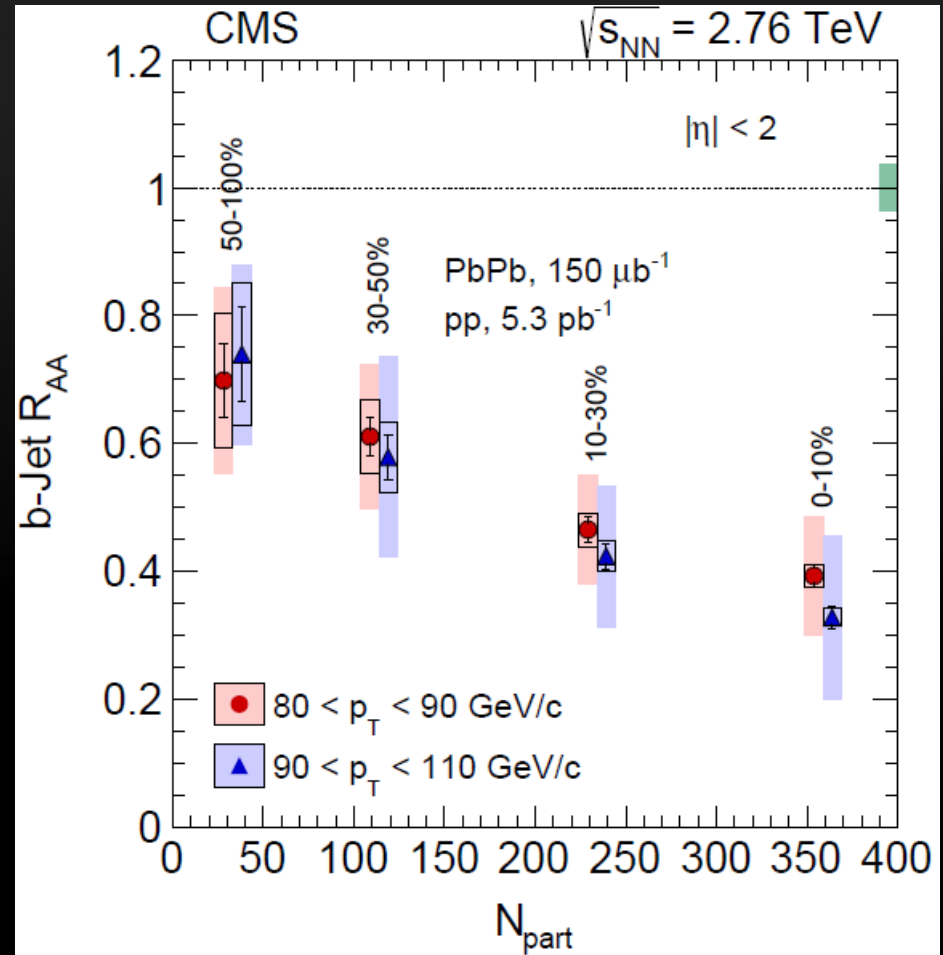
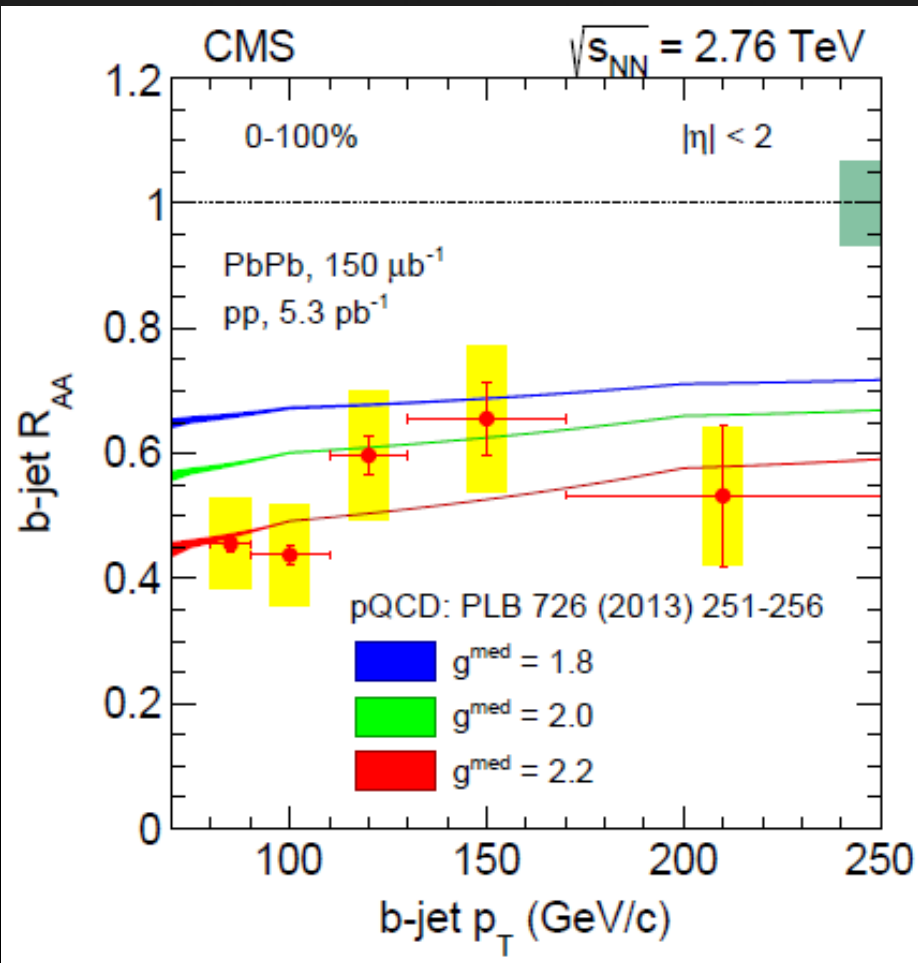


# Jet FF Moments

$$M_N = \frac{1}{N_{\text{jet}}} \int_0^1 z^N \frac{dN_h}{dz} dz$$

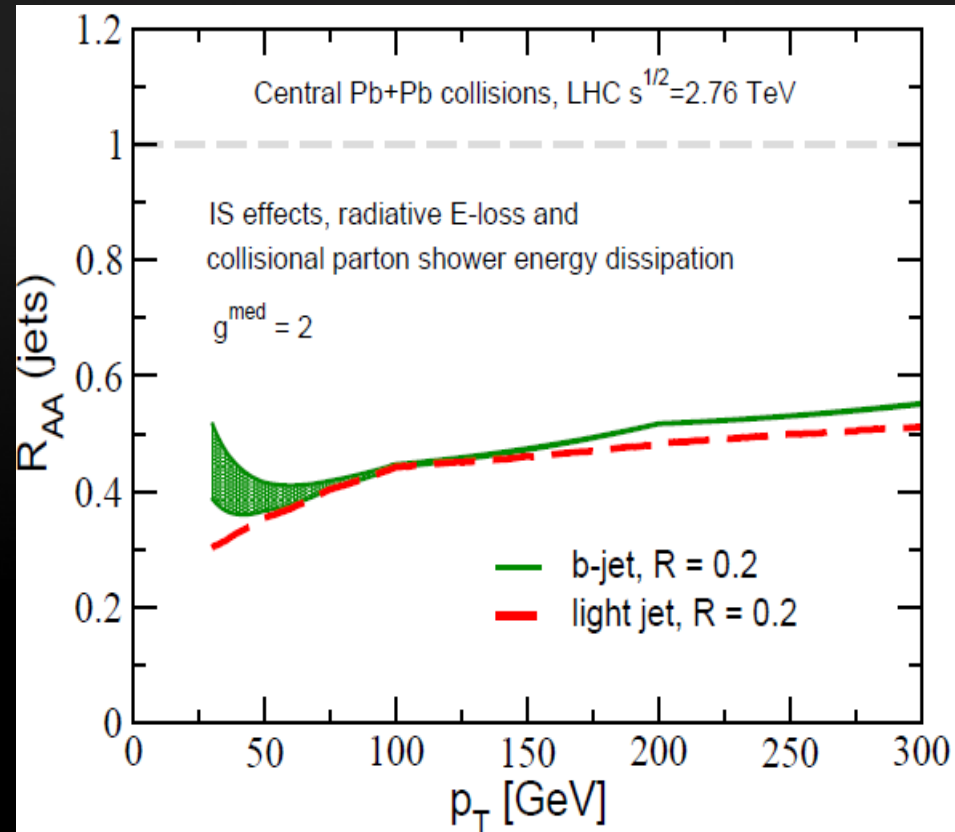
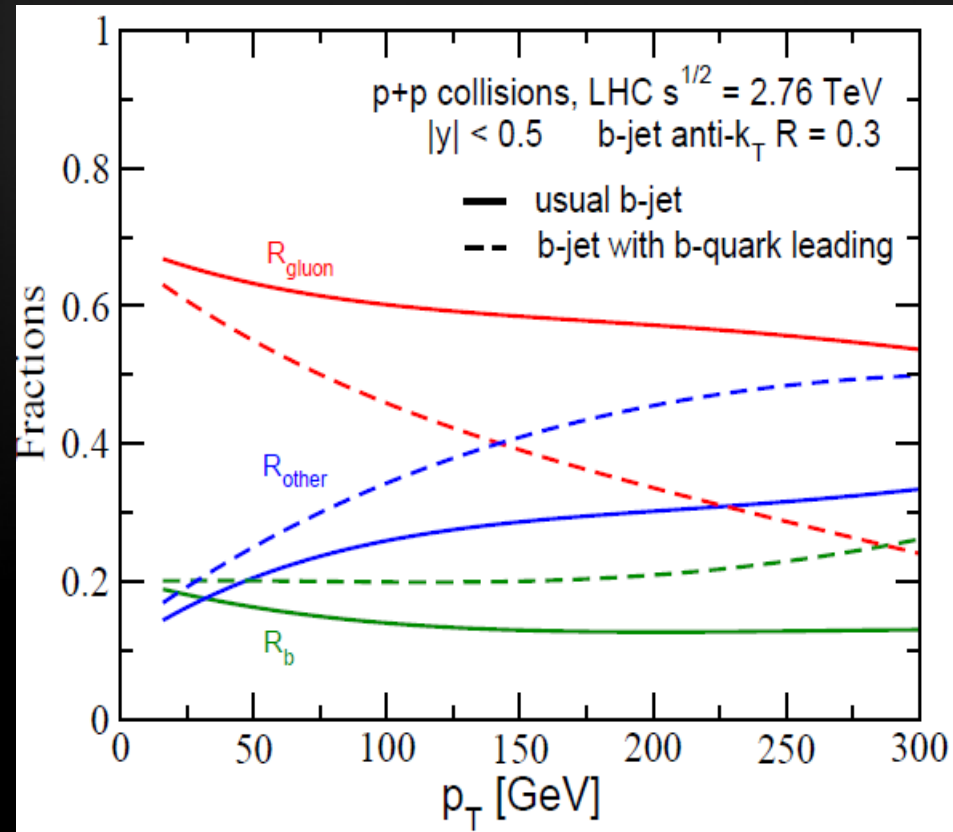


# b-tagged Jet in HIC (1)



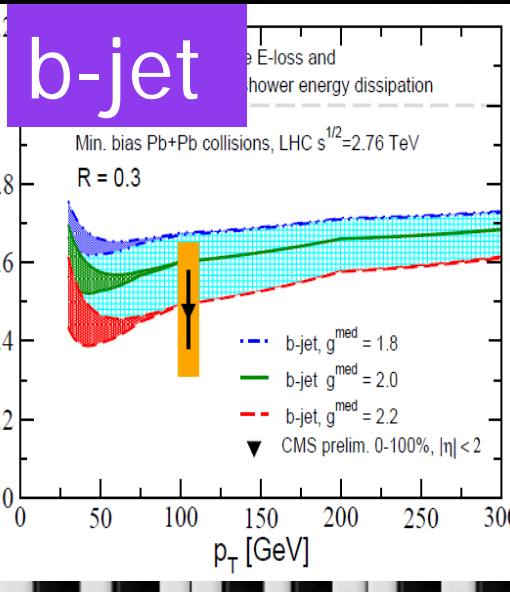
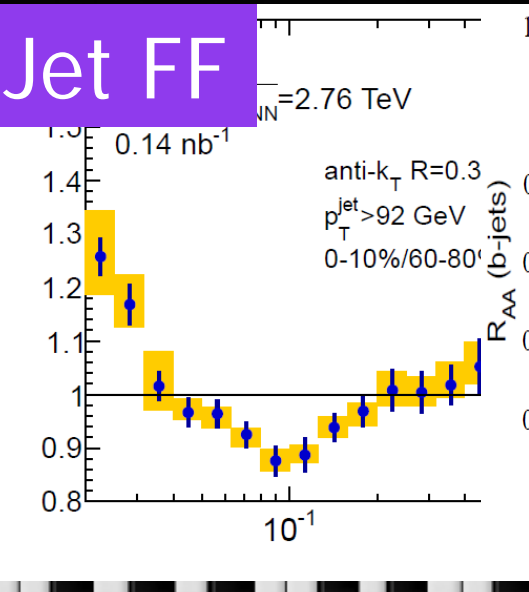
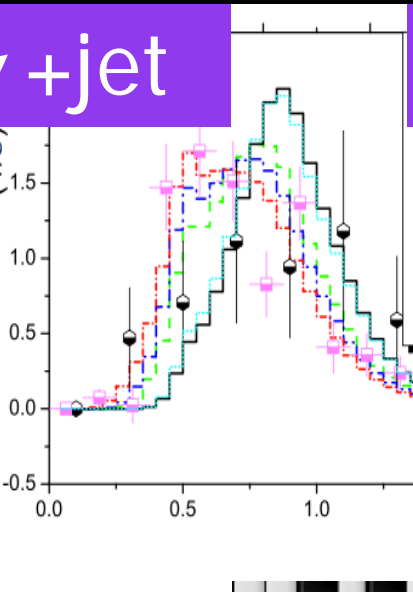
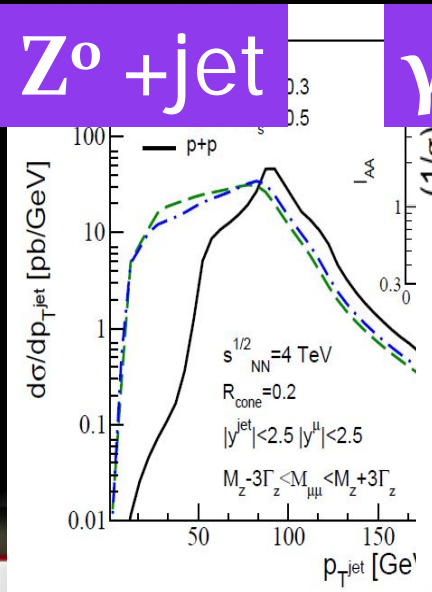
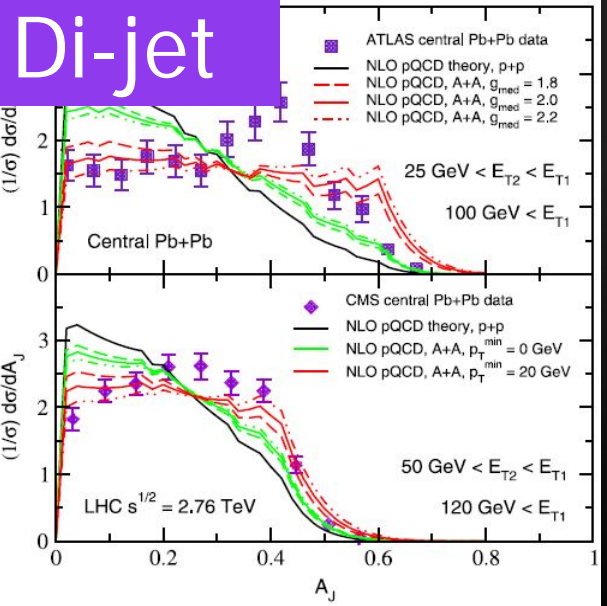
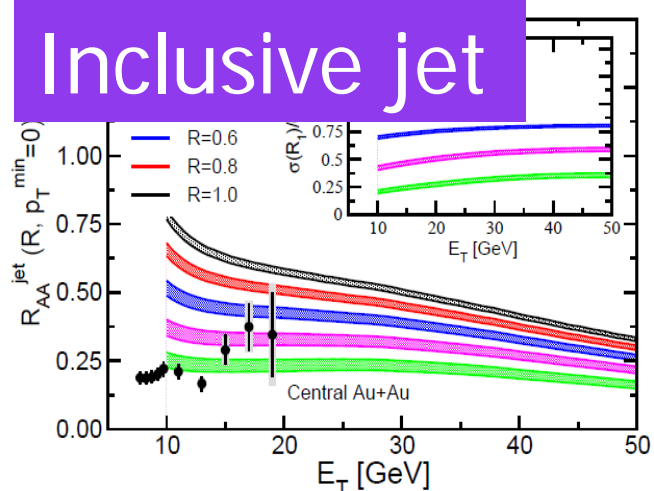
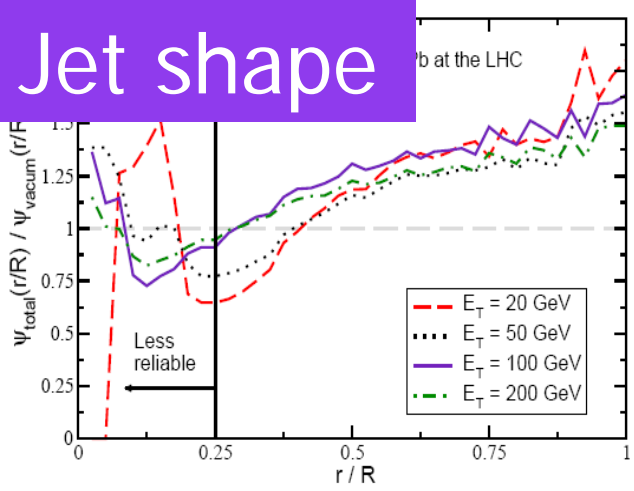
CMS, PRL (2014)

# b-tagged Jet in HIC (2)

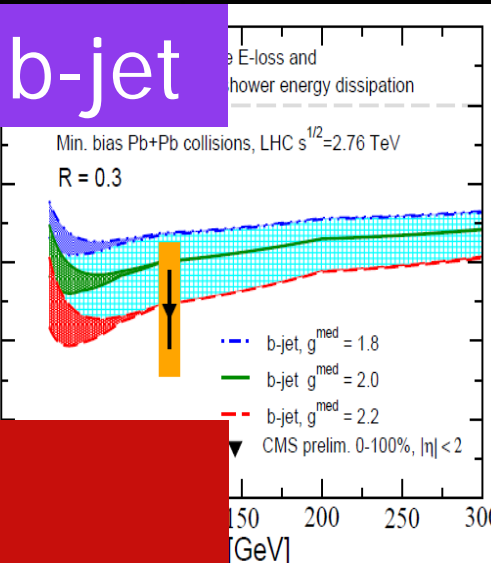
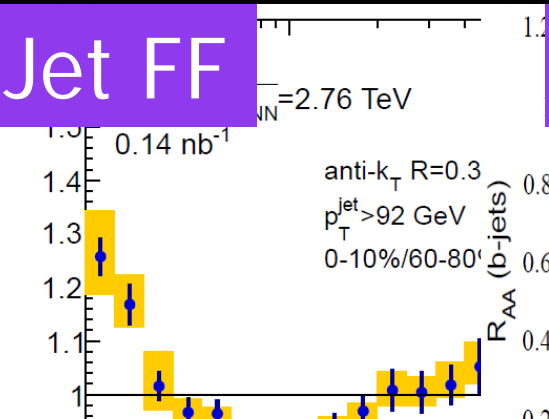
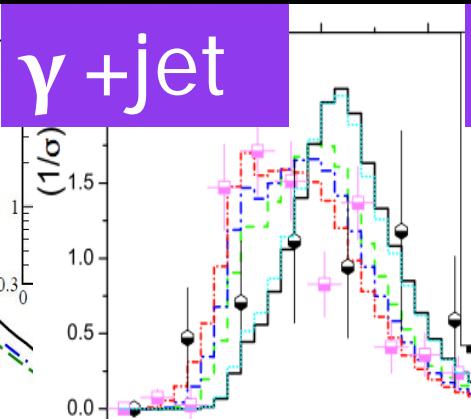
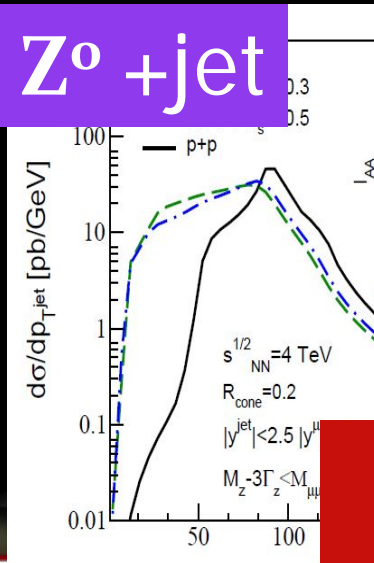
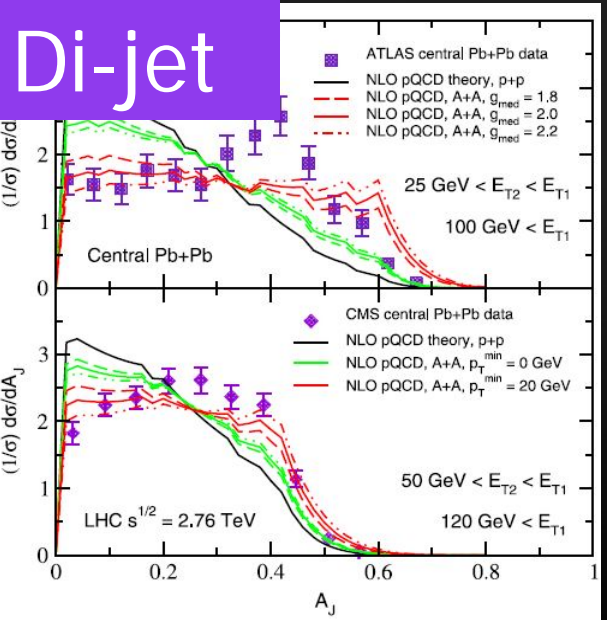
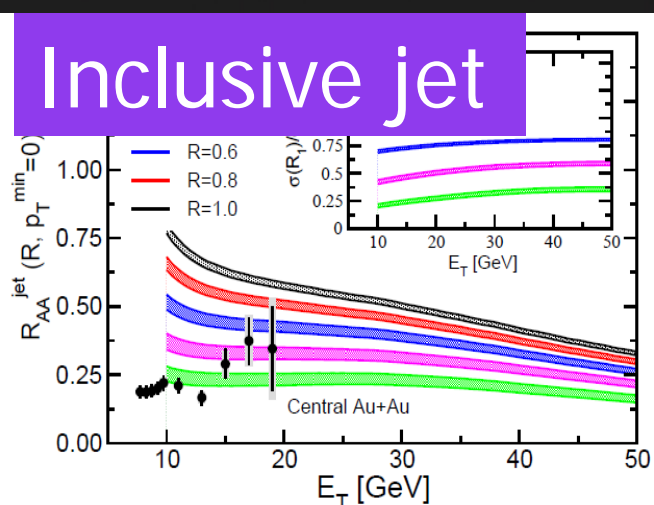
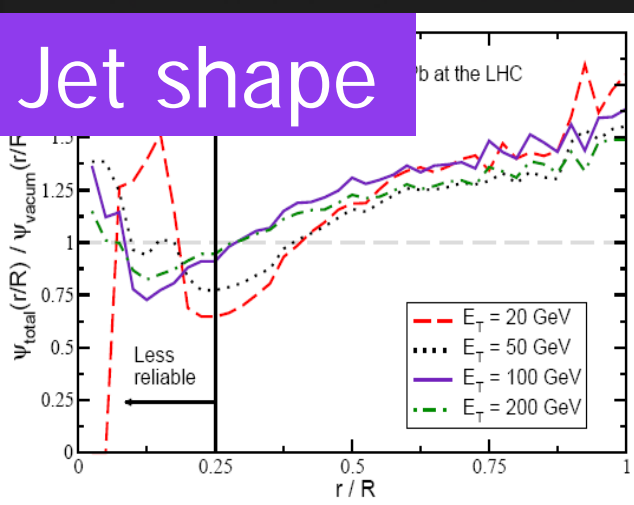


Huang, Kang, Vitev, PLB (2013)

# Recap: a world of jets



# Recap: a world of jets



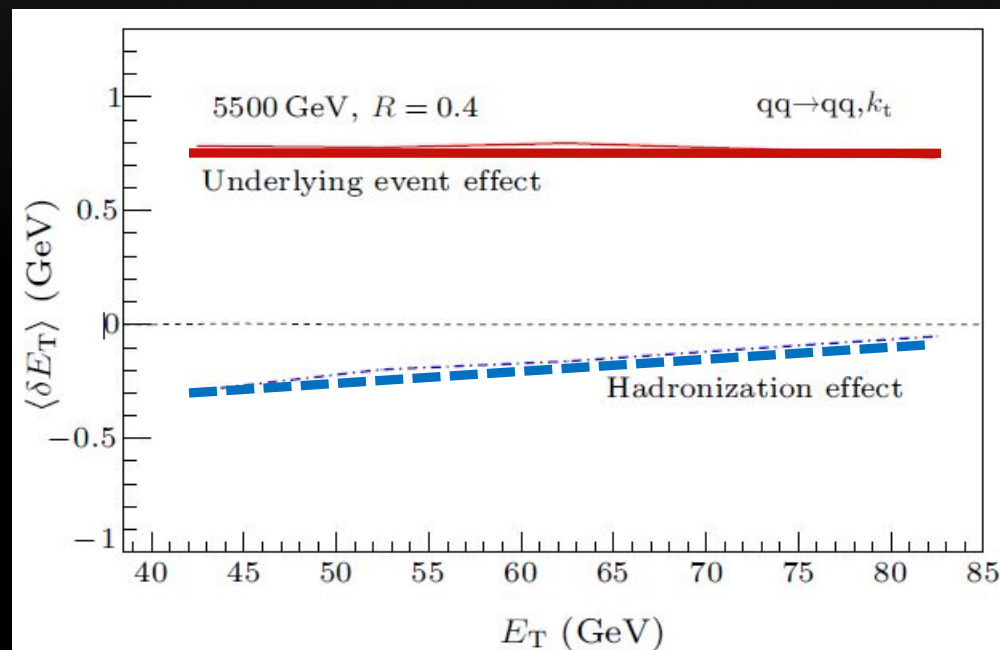
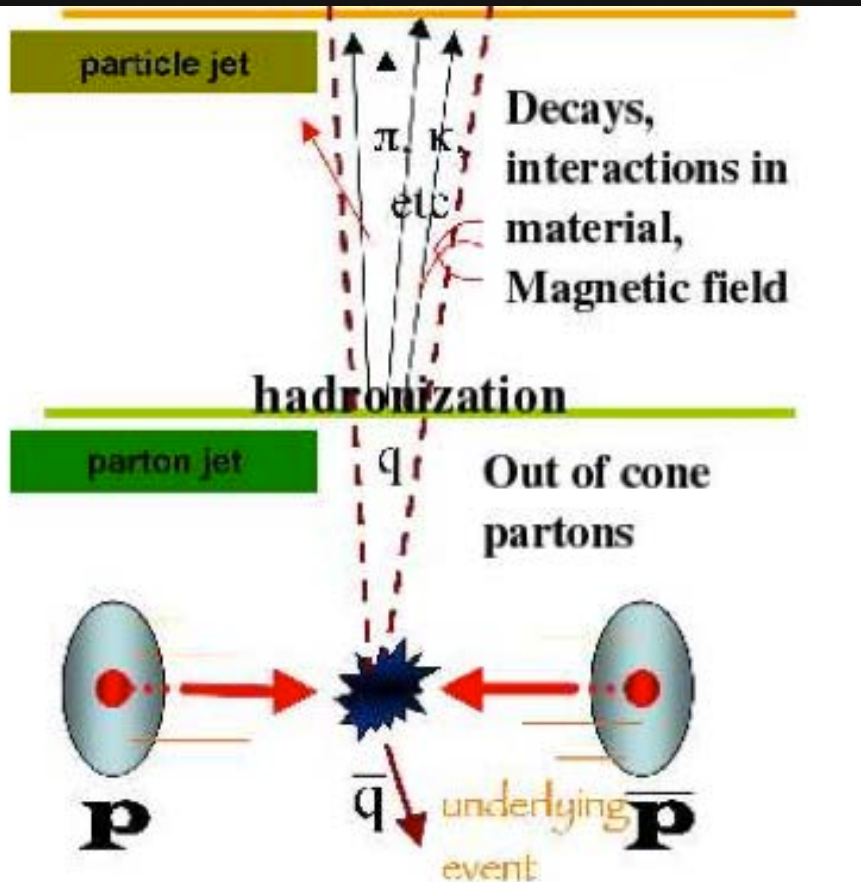
Thank you!





# Non-perturbative effects

- Non-perturbative effects: hadronization & underlying event.
- Two effects will go in opposite direction: partial cancellation between “splash-out” effect and “splash-in” effect.



H Li, BWZ, E Wang (2013)

# Sudakov resummation

Jet shapes for a quark and a gluon are:

$$\psi_q(r) = \frac{C_F \alpha_s}{2\pi} \frac{2}{r} \left( 2 \log \frac{1 - z_{min}}{Z} - \frac{3}{2} [(1 - Z)^2 - z_{min}^2] \right),$$

$$\begin{aligned} \psi_g(r) = & \frac{C_A \alpha_s}{2\pi} \frac{2}{r} \left( 2 \log \frac{1 - z_{min}}{Z} - \left( \frac{11}{6} - \frac{Z}{3} + \frac{Z^2}{2} \right) (1 - Z)^2 \right. \\ & \left. + \left( 2z_{min}^2 - \frac{2}{3}z_{min}^3 + \frac{1}{2}z_{min}^4 \right) \right) \\ & + \frac{T_R N_f \alpha_s}{2\pi} \frac{2}{r} \left( \left( \frac{2}{3} - \frac{2Z}{3} + Z^2 \right) (1 - Z)^2 - \left( z_{min}^2 - \frac{4}{3}z_{min}^3 + z_{min}^4 \right) \right) \end{aligned}$$

Collinear divergence  
Requires Sudakov  
resummation

$$\begin{aligned} P(< r) &= \exp(-P_1(> r)) \\ &= \exp\left(-\int_r^R dr' \psi_{\text{coll}}(r')\right) \end{aligned}$$

Sudakov form factors:

$$\psi_{\text{RS}}(r) = \frac{dP(r)}{dr}$$

$$\begin{aligned} P_q(r > z_{min}R) &= \exp\left(2C_F \log \frac{R}{r} f_1\left(2\beta_0 \alpha_s \log \frac{R}{r}\right) \right. \\ &\quad \left. - \left[\frac{3}{2}C_F - CR^2 - c_q^>(z_{min})\right] \right. \\ &\quad \left. \times f_2\left(2\beta_0 \alpha_s \log \frac{R}{r}\right)\right), \end{aligned}$$

$$\begin{aligned} P_g(r > z_{min}R) &= \exp\left(2C_A \log \frac{R}{r} f_1\left(2\beta_0 \alpha_s \log \frac{R}{r}\right) \right. \\ &\quad \left. - \left[\frac{1}{2}b_0 - CR^2 - c_g^>(z_{min})\right] \right. \\ &\quad \left. \times f_2\left(2\beta_0 \alpha_s \log \frac{R}{r}\right)\right). \end{aligned}$$

$$\begin{aligned} P_q(r < z_{min}R) &= P_q(r > z_{min}R; r = z_{min}R) \\ &\quad \times \exp\left(-\left[\frac{3}{2}C_F - c_q^<(z_{min})\right] \right. \\ &\quad \left. \times f_2\left(2\beta_0 \tilde{\alpha}_s \log \frac{z_{min}R}{r}\right)\right), \end{aligned}$$

$$\begin{aligned} P_g(r < z_{min}R) &= P_g(r > z_{min}R; r = z_{min}R) \\ &\quad \times \exp\left(-\left[\frac{1}{2}b_0 - c_g^>(z_{min})\right] \right. \\ &\quad \left. \times f_2\left(2\beta_0 \tilde{\alpha}_s \log \frac{z_{min}R}{r}\right)\right). \end{aligned}$$

# Tagged jet production in HIC

photon + jet

- Advantage: large yield
- Disadvantage: final-state effects

$Z^0$  + jet

- Disadvantage: small cross section
- Advantage: no final-state effects

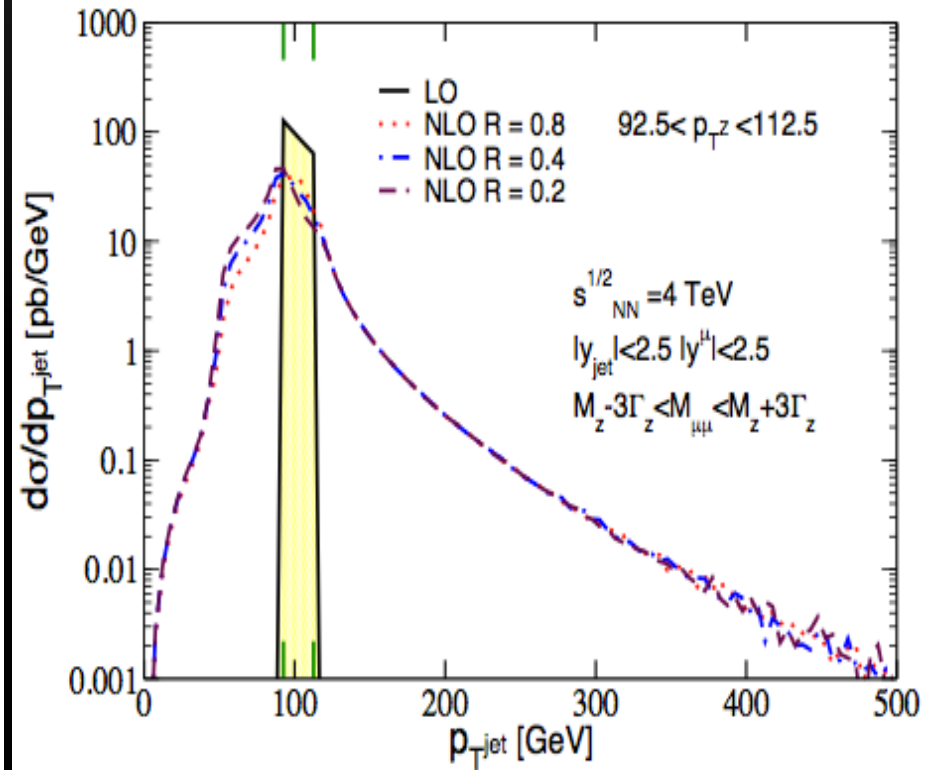
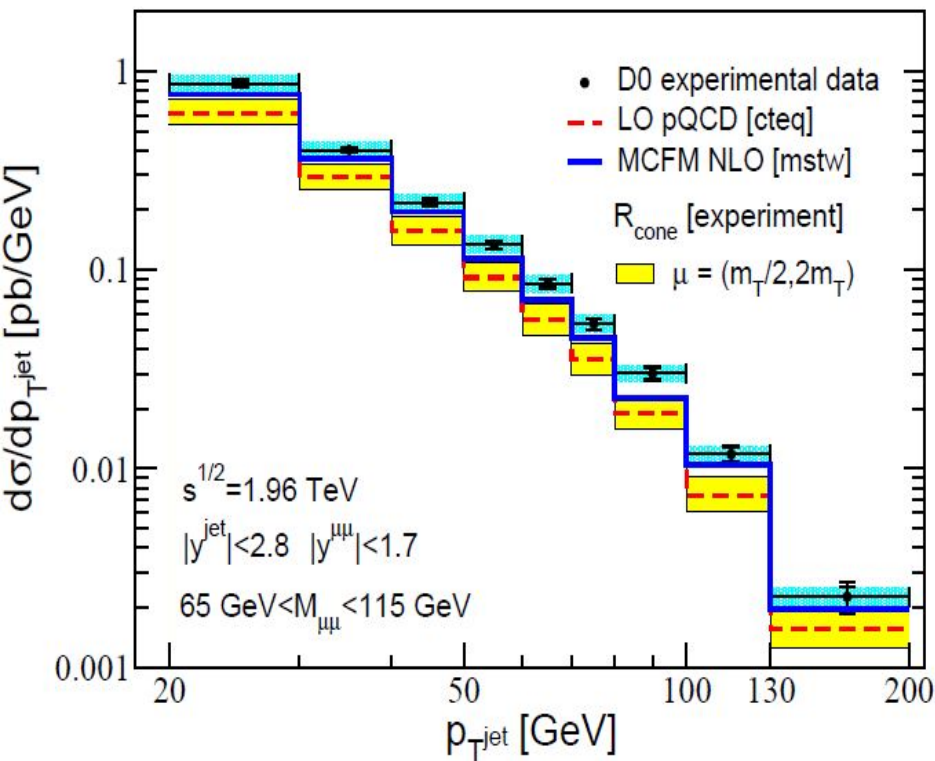


You are so light, I am too heavy.



# $Z^0 + \text{jet in } h+h$

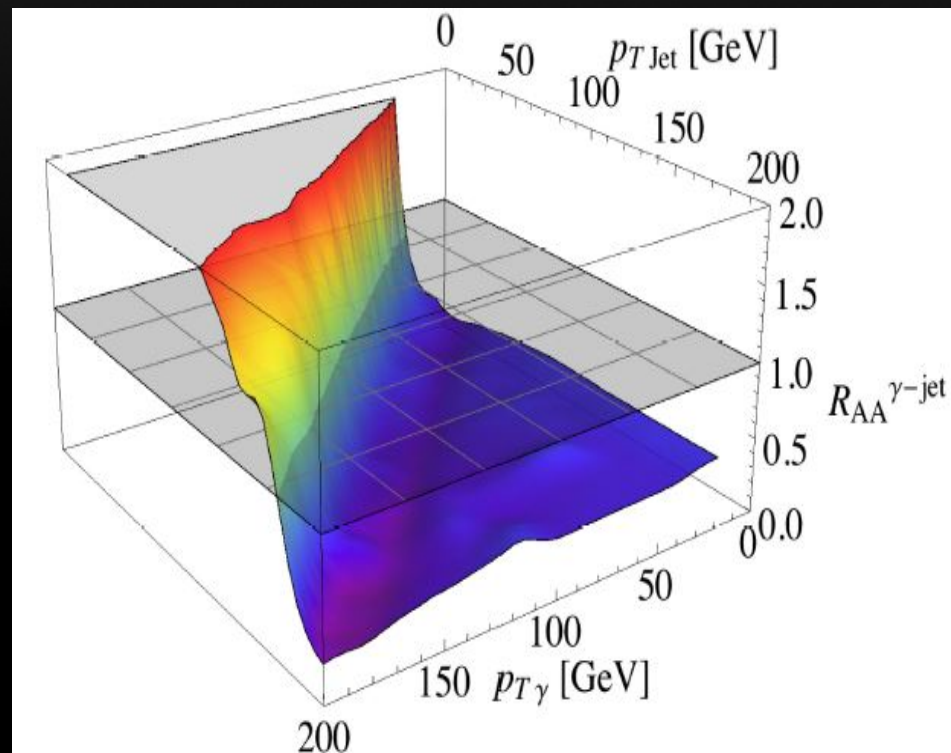
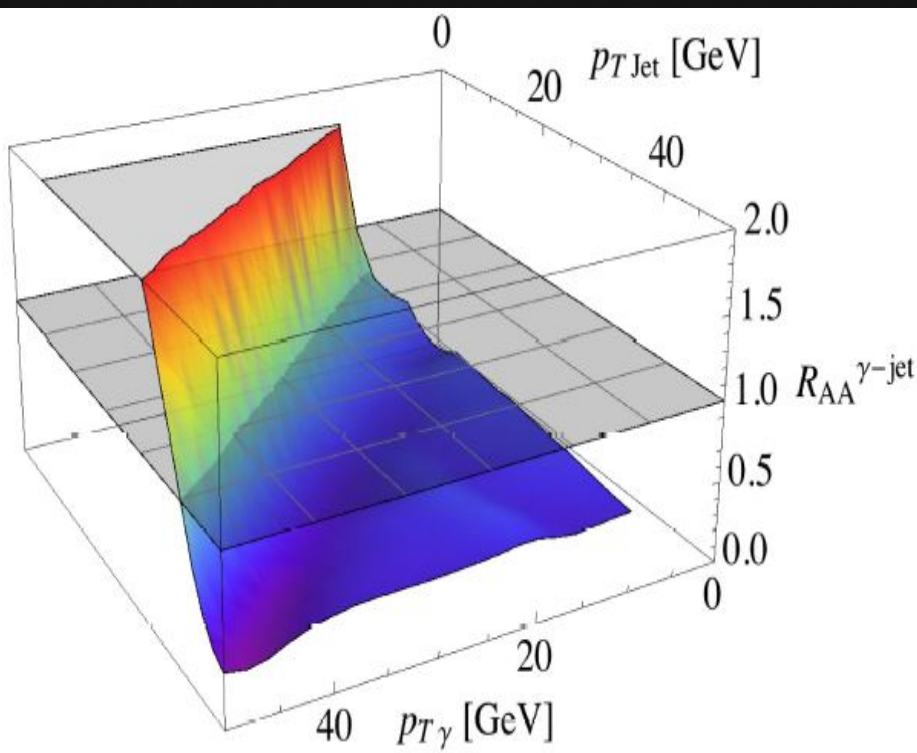
- NLO pQCD gives a good description of the data at DO
- The momentum balance is broken due to NLO contribution



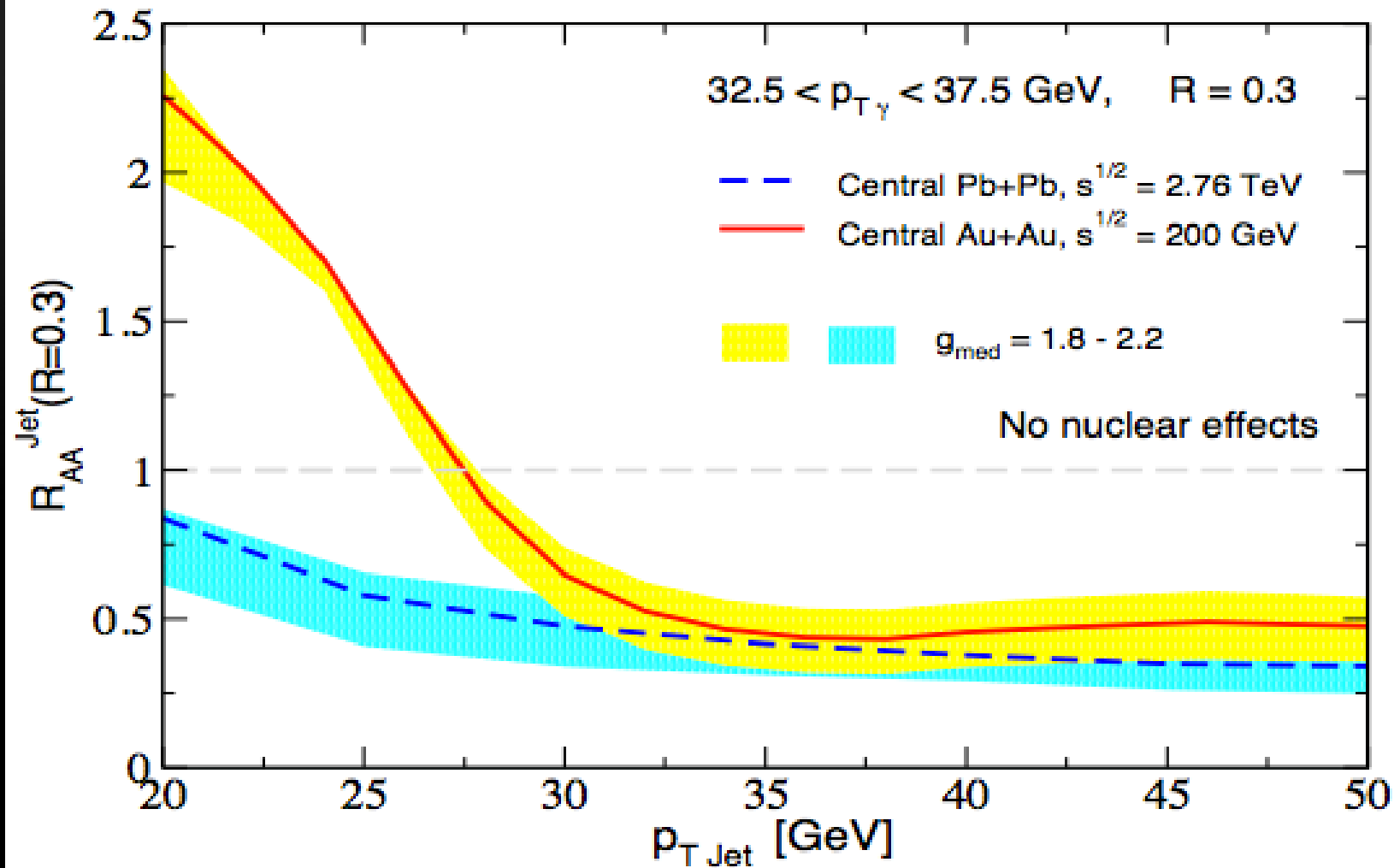
$p_T \in (92.5\text{GeV}, 112.5\text{GeV})$

# Photon + jet in A+A (II)

- Direct comparison between RHIC and LHC is possible for this exclusive channel.



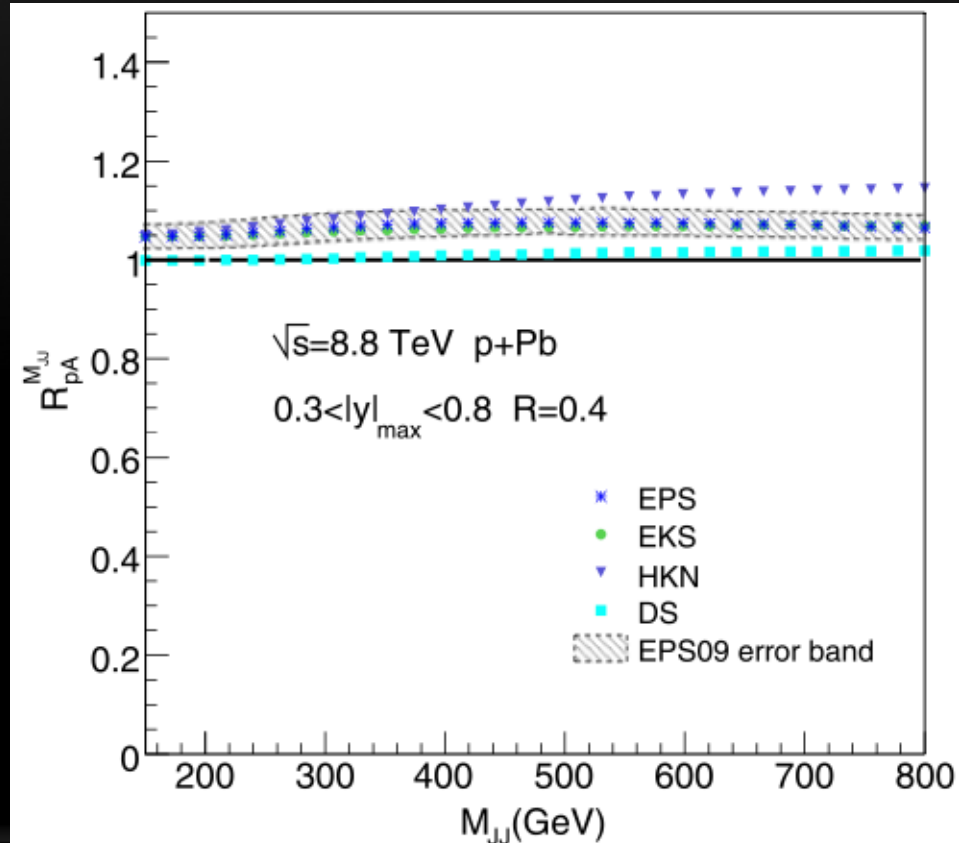
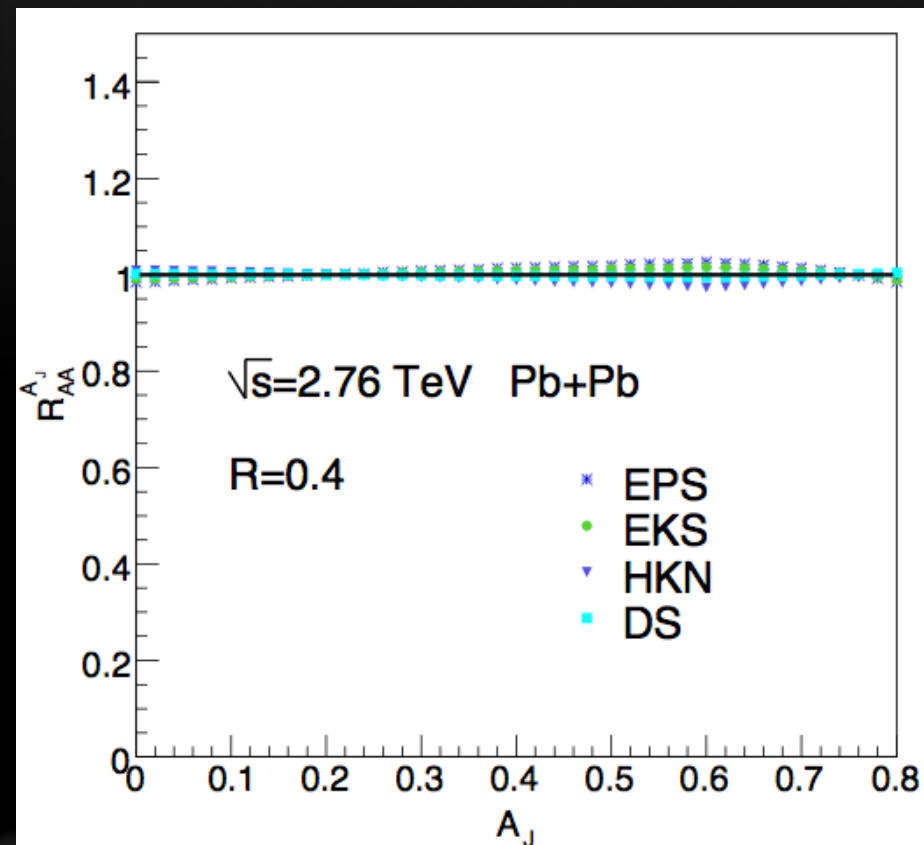
# photon + jet in A+A (I)



# Dijet in HIC: CNM

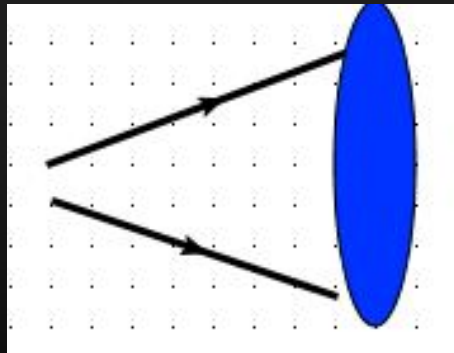
$$A_J = \frac{E_{T1} - E_{T2}}{E_{T1} + E_{T2}}$$

$$M_{jj}^2 = 2p_T^2 [1 + \cosh(y_1 - y_2)]$$

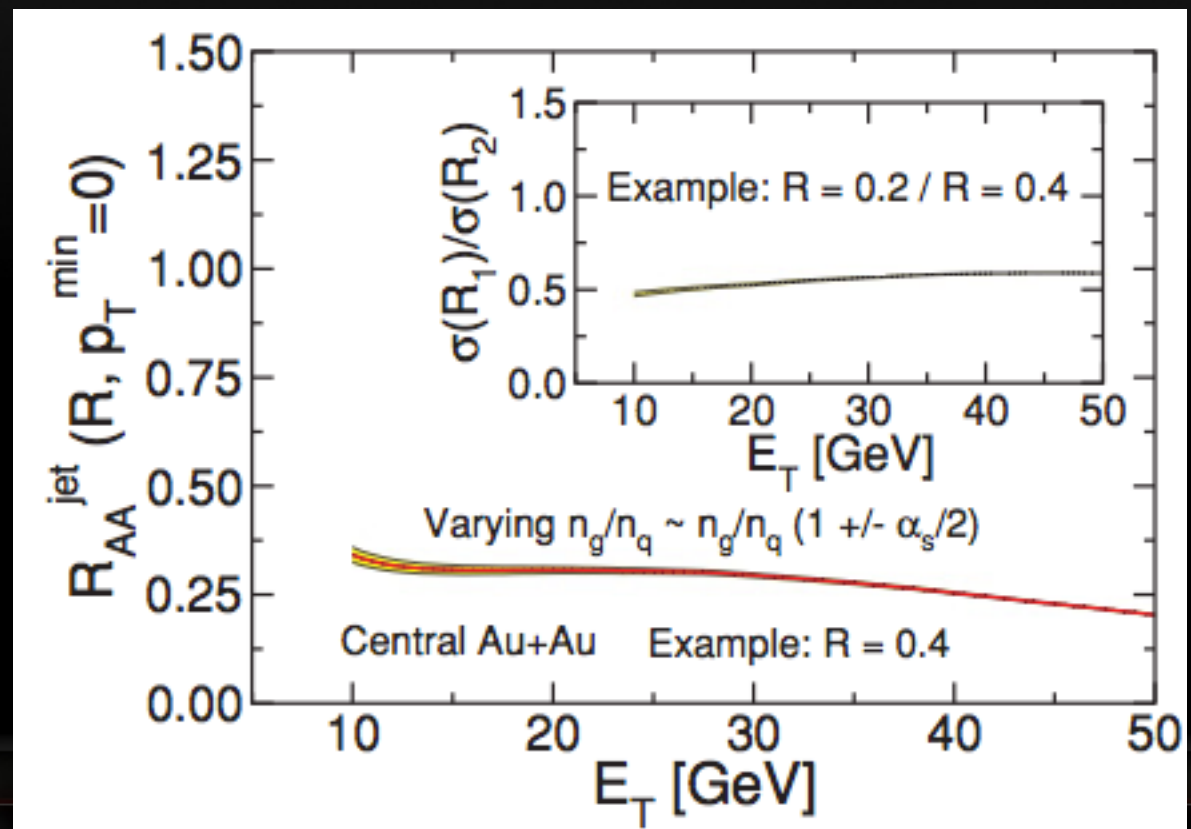
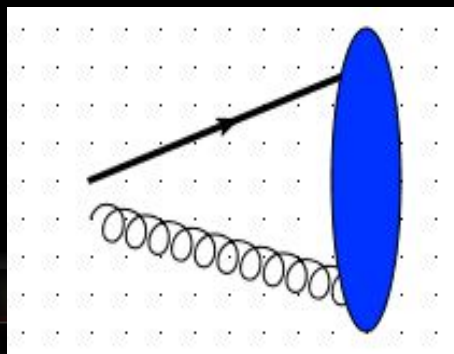
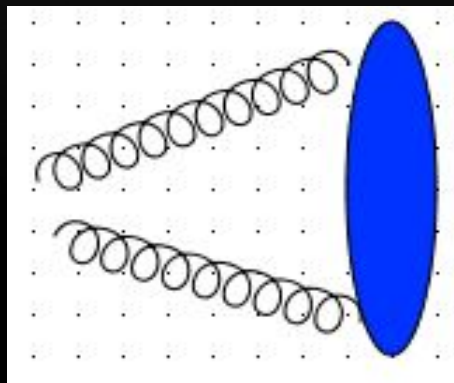




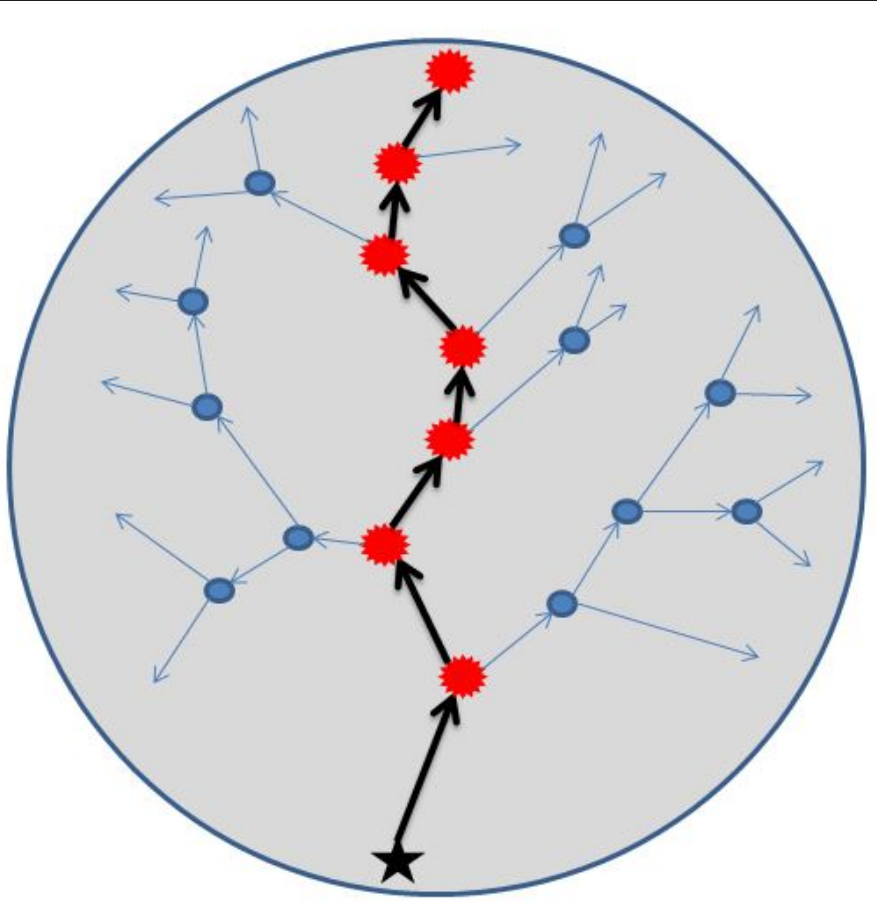
# Quark jet and Gluon jet





$$n_q = \frac{d\sigma^{q \text{ jet}}}{dp_T} \bigg/ \frac{d\sigma^{\text{jet}}}{dp_T}, \quad n_g = \frac{d\sigma^{g \text{ jet}}}{dp_T} \bigg/ \frac{d\sigma^{\text{jet}}}{dp_T}$$



# LBT model of parton ELoss



-  leading parton---thermal parton scattering
-  recoiled parton---thermal parton scattering

*Linearized Boltzmann jet transport*  
neglect scatterings between recoiled medium partons.

It's a good approximation when the jet induced medium excitation  $\delta f \ll f$ .

