

LHC/RHIC: **GlueBall Factory!** ... but **where** are all the GlueBalls gone?

Early proposals for two phase transitions and two timescales in RHICs:

Svetitsky&Yaffe, Pisarski&Wilczek, Raha&Sinha, Shuryak et al...

1. CGC Gluon Supersaturation

2. Gluon Equilibration

3. **First Transition:** 1.Order Phase Transition in YM pure gauge theory

4. Pure Gauge Theory vs. “physical” 2+1 N_f QCD

5. Glue Plasma vs Quark-Gluon Plasma 2.Transition: hadronization ?

6. Observable signals for GlueBalls in high multiplicity pp, pA - AA ?

- HagedornStates, hadron ratios, pt-distributions, Flow&**Ridge** pp & pA

- plus Dileptons, Photons, Centauros,... vs. **Multiplicity in pp**, pA...

Horst Stoecker, **CCNU, Wuhan** and GSI Helmholtzzentrum f. Schwerionenphysik

Judah M. Eisenberg Professor Laureatus, ITP & FIAS, Goethe Univ. Frankfurt 1

Acknowledgements

Transport colleagues: **Zhou, Seizel**, Xu, Zhuang, C. Greiner...

Hagedorn dynamics: **Beitel, Gallmeister**, C. Greiner...

FIAS: Schramm, **Dietrich**, Struckmeier, Vasak, ...

Early phase e-m probes colleagues: Raha, Sinha, Gorenstein, **Vovchenko**, Satarov, Mishustin, A. Srivastava, Csernai ...

Lattice colleagues: Fodor, **Borsanyi**, Szabo, Karsch, Philipsen...

Experimentalists: Giubellino, Harris, Oeschler, PBM, Masc..

Traditional picture of QCD matter in Heavy Ion Collisions

Initial Color Glass Condensate \longrightarrow Glasma thermalizes
 \longrightarrow fast equilibration of Gluons and Light flavor quarks
high pressure, entropy \longrightarrow hydrodynamic expansion
 \longrightarrow flow as excellent probe of QCD matter.

Hadronization @ $T=155\text{MeV}$: crossing of 2+1 flavor QCD.

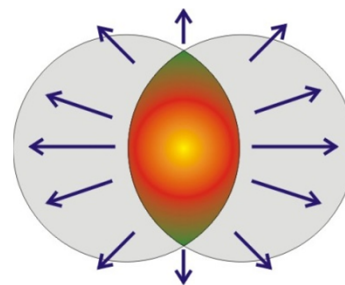
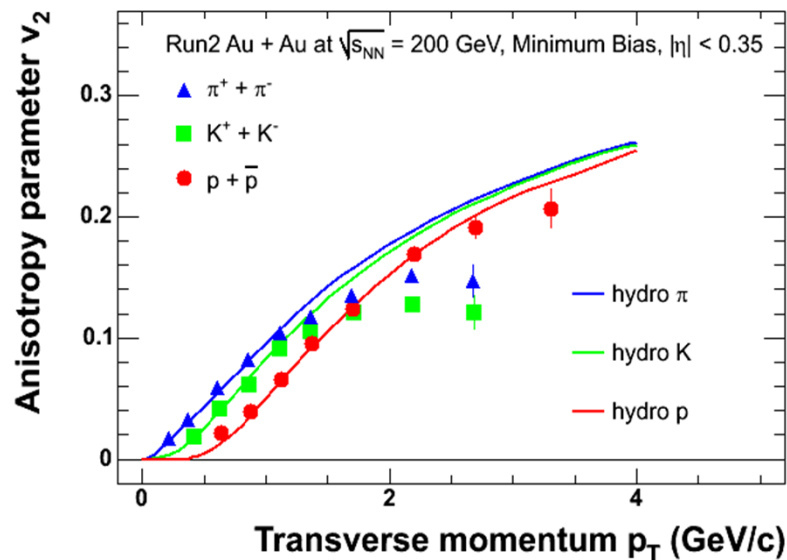
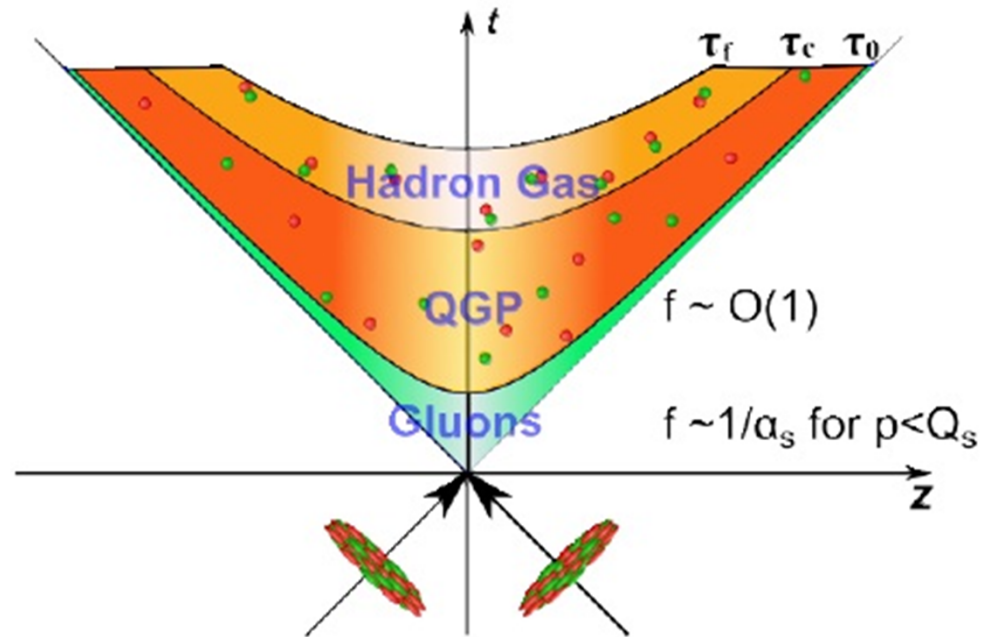
Hadronic yields and v_n at RHIC and LHC measured.

Comparison of HRG, $T=155\text{ MeV}$, with LHC data tests
our understanding of QCD matter.

Introduction : Fast thermalization

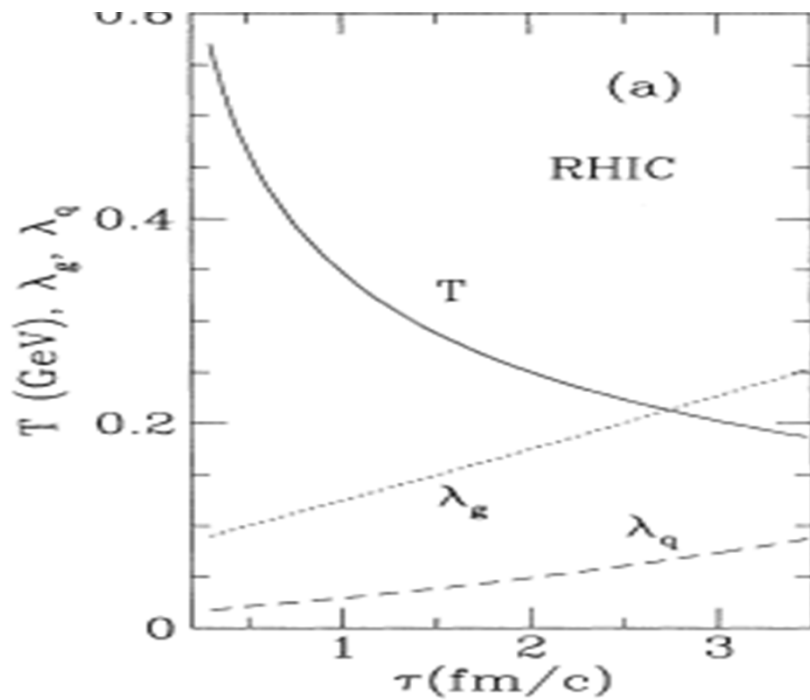
“how the systems evolve to thermal equilibrium in a very short time scale”

Initial: far from equilibrium

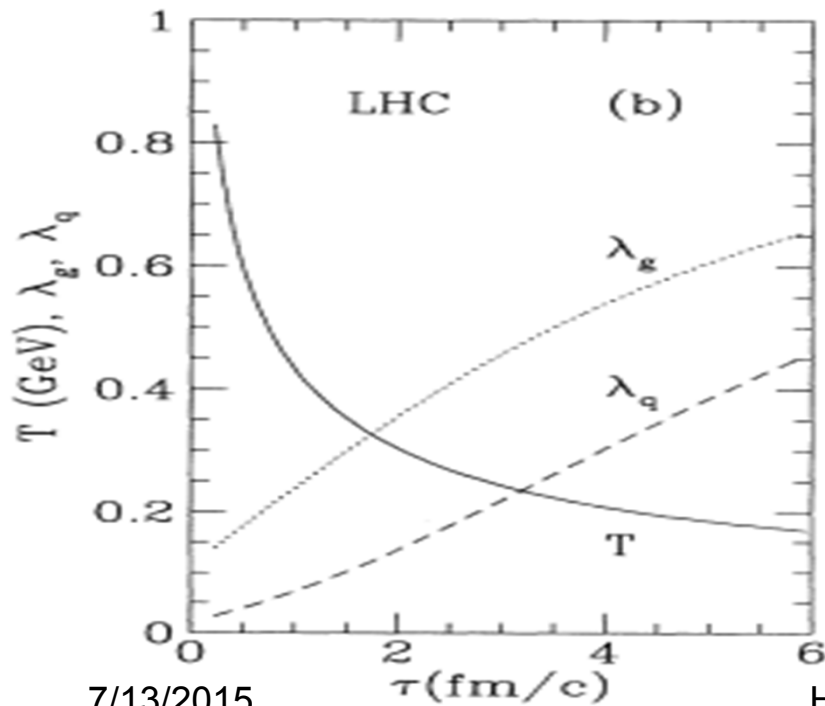


2+1 QCD Hydrodyna.
Onset time $\sim 1\text{fm}/c$?

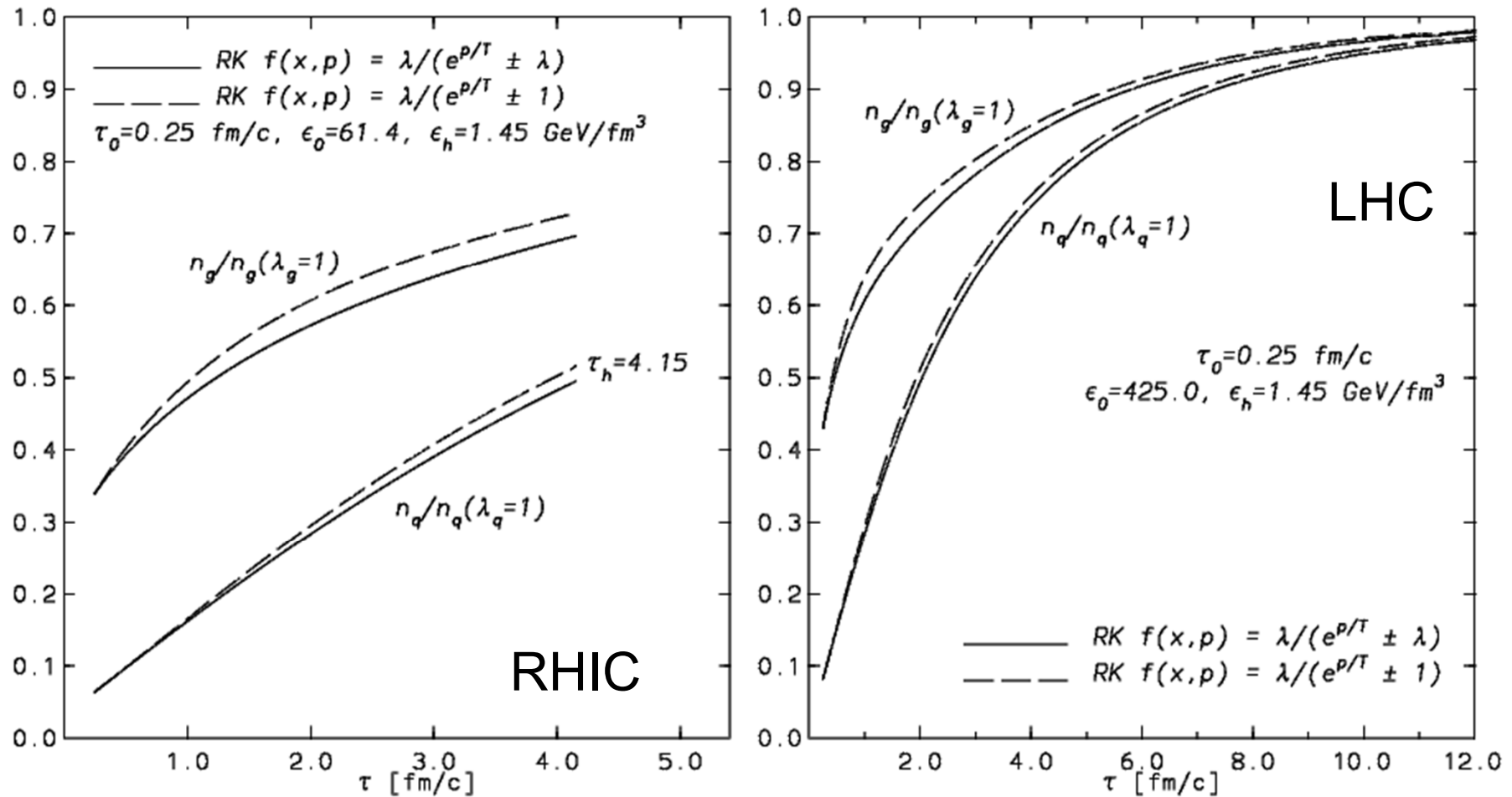
BMW: Early stage **NO QCD** ! Pure glue.



Time evolution of fugacity of gluons and quarks (g, q) from pQCD-based rate eq.
 T. S. Biró, B. Mueller, X. Wang, BMW, PRC48,1275 (1993)

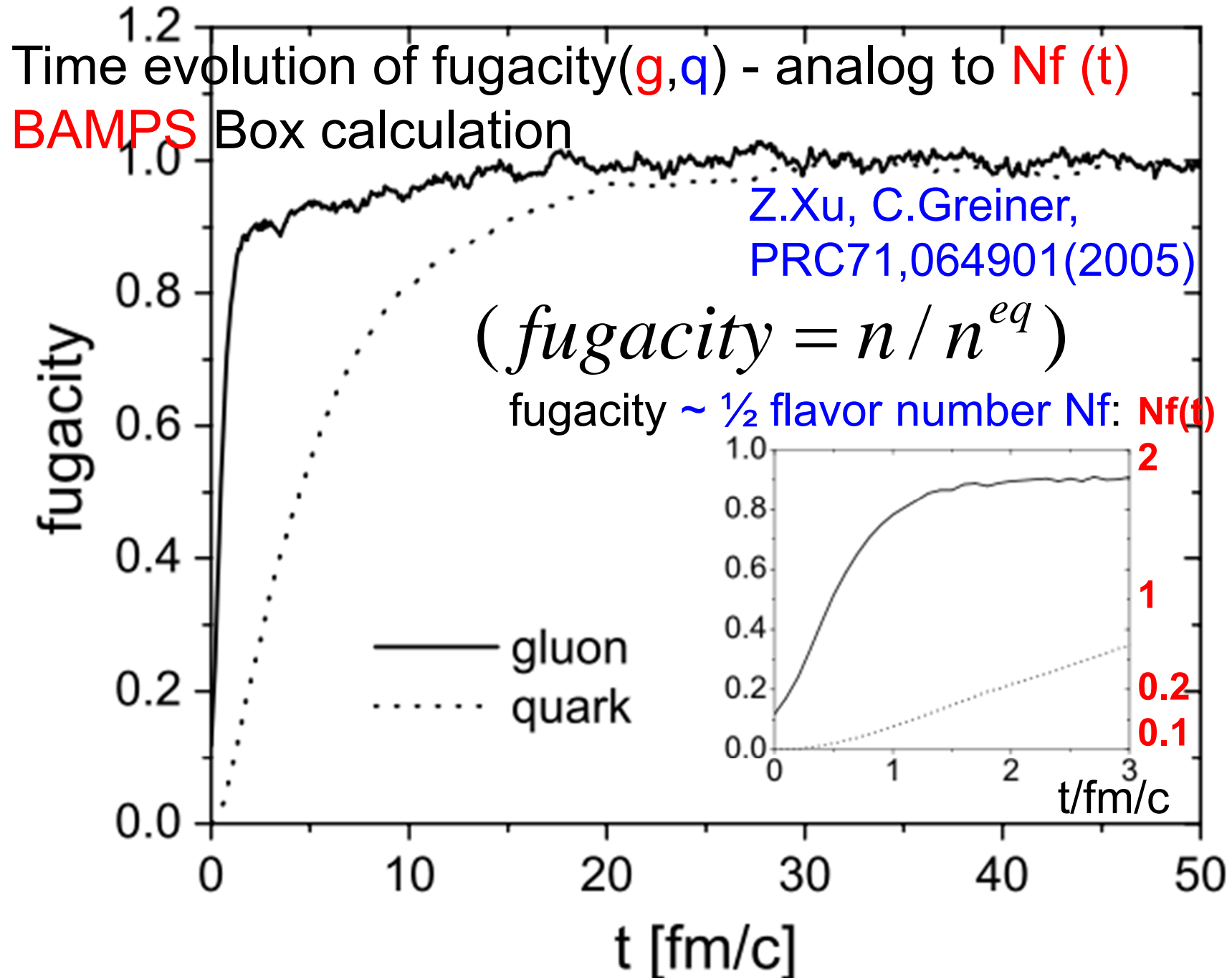


($fugacity = n / n^{eq}$)



Rate equation calculation

D.M. Elliott, D.H. Rischke, Nucl.Phys. A671,583 (2000)



Introducing the **Color Glass Condensate**

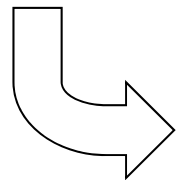
CGC=effective field theory for hadrons at high energy limit

- high energy (time dilation) $\left\{ \begin{array}{l} \text{fluctuation(sea partons) lifetime} \\ \text{internal interaction time scales} \\ \text{small } x \left(x \sim p_z / E_{hadron} \right) \end{array} \right\} \longrightarrow$

gluon number increase at small x with increasing energy

- gluon fusion $f \sim f^2 \alpha_s \implies f \sim 1 / \alpha_s$ **Saturation**

- Saturation momentum $Q_s(\sim \text{GeV})$** $xG(x, Q^2) / Q^2 \rightarrow 1 / \alpha_s$



$$f \sim 1 / \alpha_s (Q < Q_s)$$

this feature can be inherited by initial Glasma through indirect way

Introducing the **Glasma**

Glasma=non-equilibrium state in between CGC and QGP

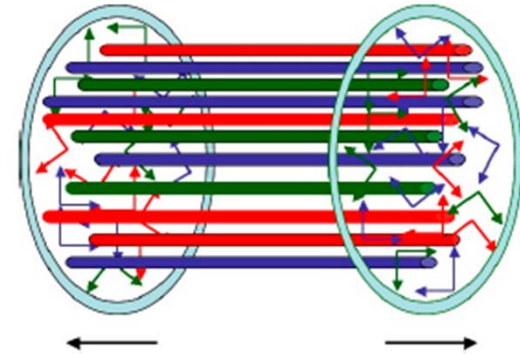
- using CGC as initial states for nuclei

$$\longrightarrow T^{\mu\nu} = \text{diag}(\varepsilon, \varepsilon, \varepsilon, -\varepsilon)$$

highly anisotropic initial glasma fields

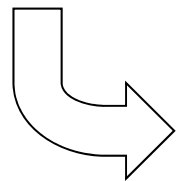


(won't last longer than $1/Q_s$)

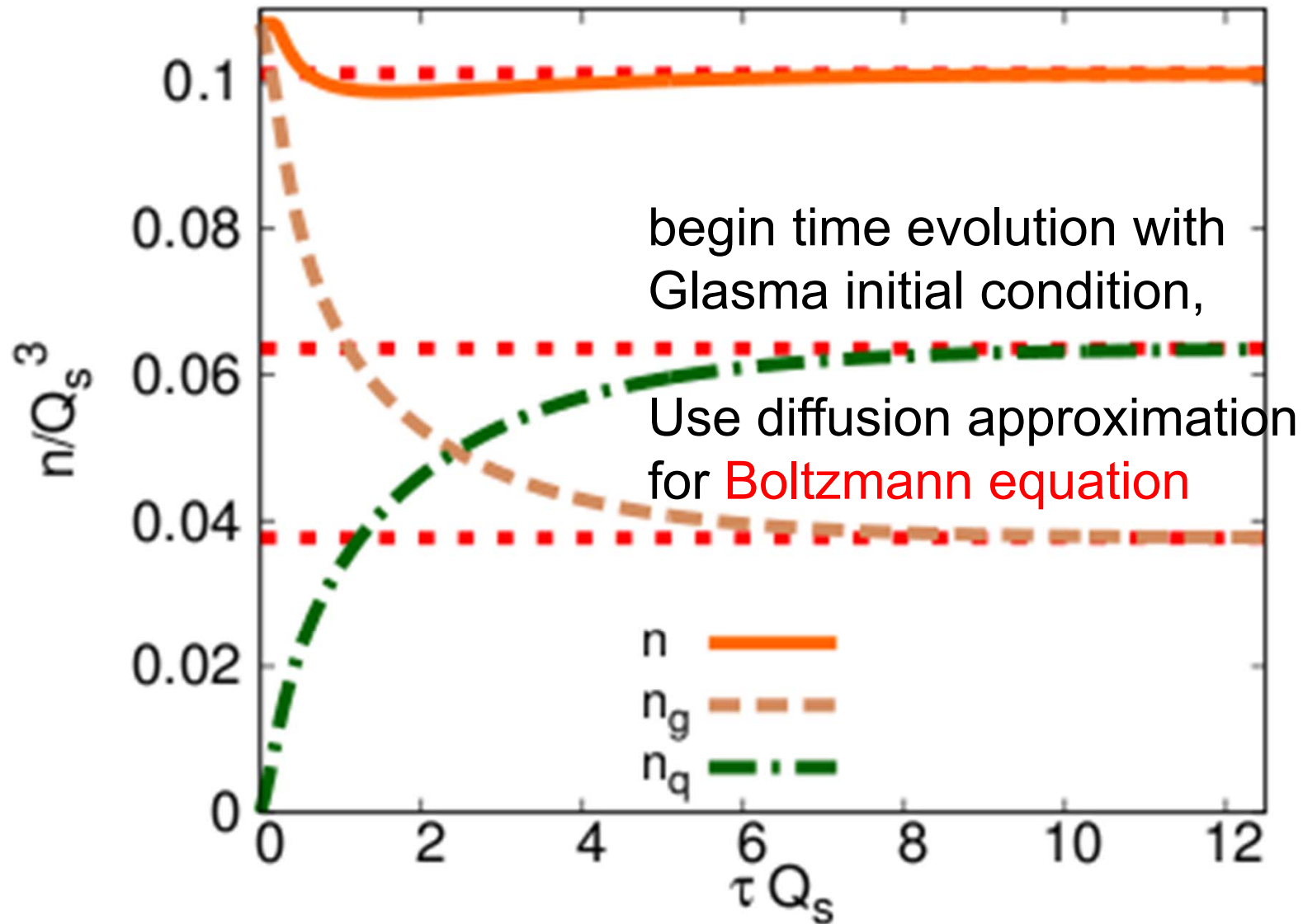


- **Instabilities** --> wide range of unstable modes (up to Q_s)
grow exponentially until saturation density

\longrightarrow { redistribute momentum ---> **isotropization**
free up quanta from classical field



$f_0 = 1/\alpha_s(p < Q_s)$ **initial condition amenable for kinetic theory**



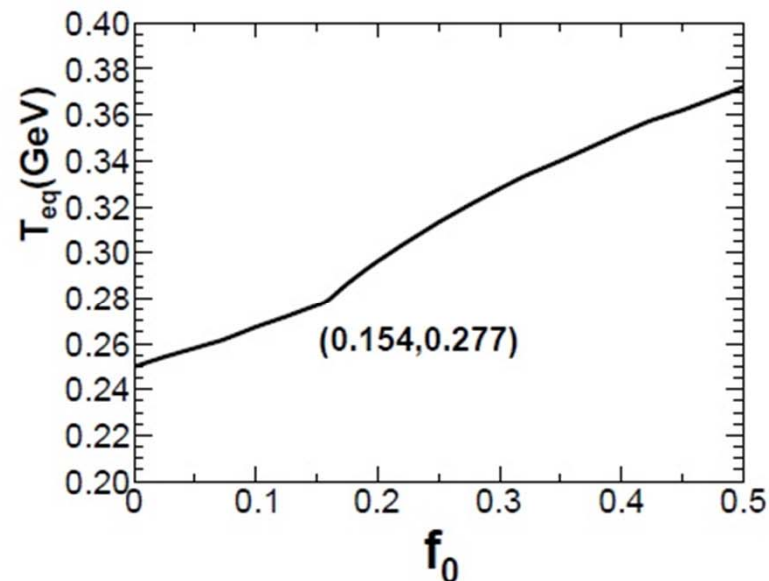
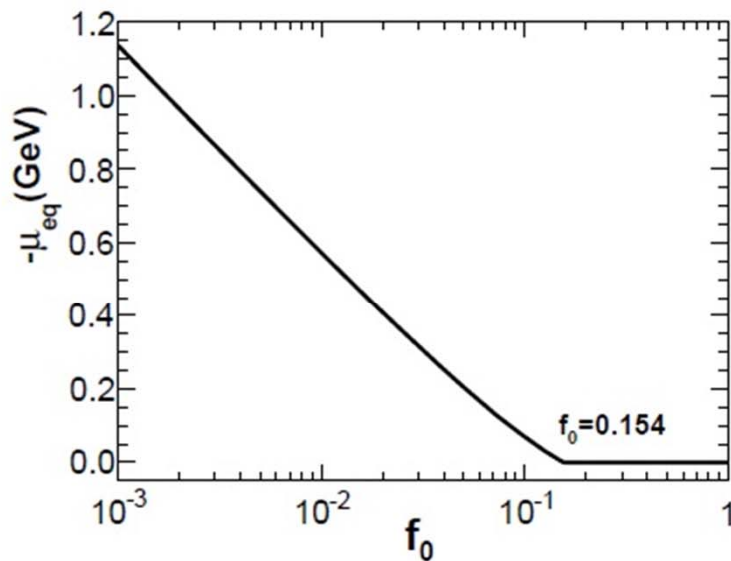
Jean-Paul Blaizot, Bin Wu, Li Yan, Nucl.Phys. A930,139(2014)

Introducing: Overpopulation

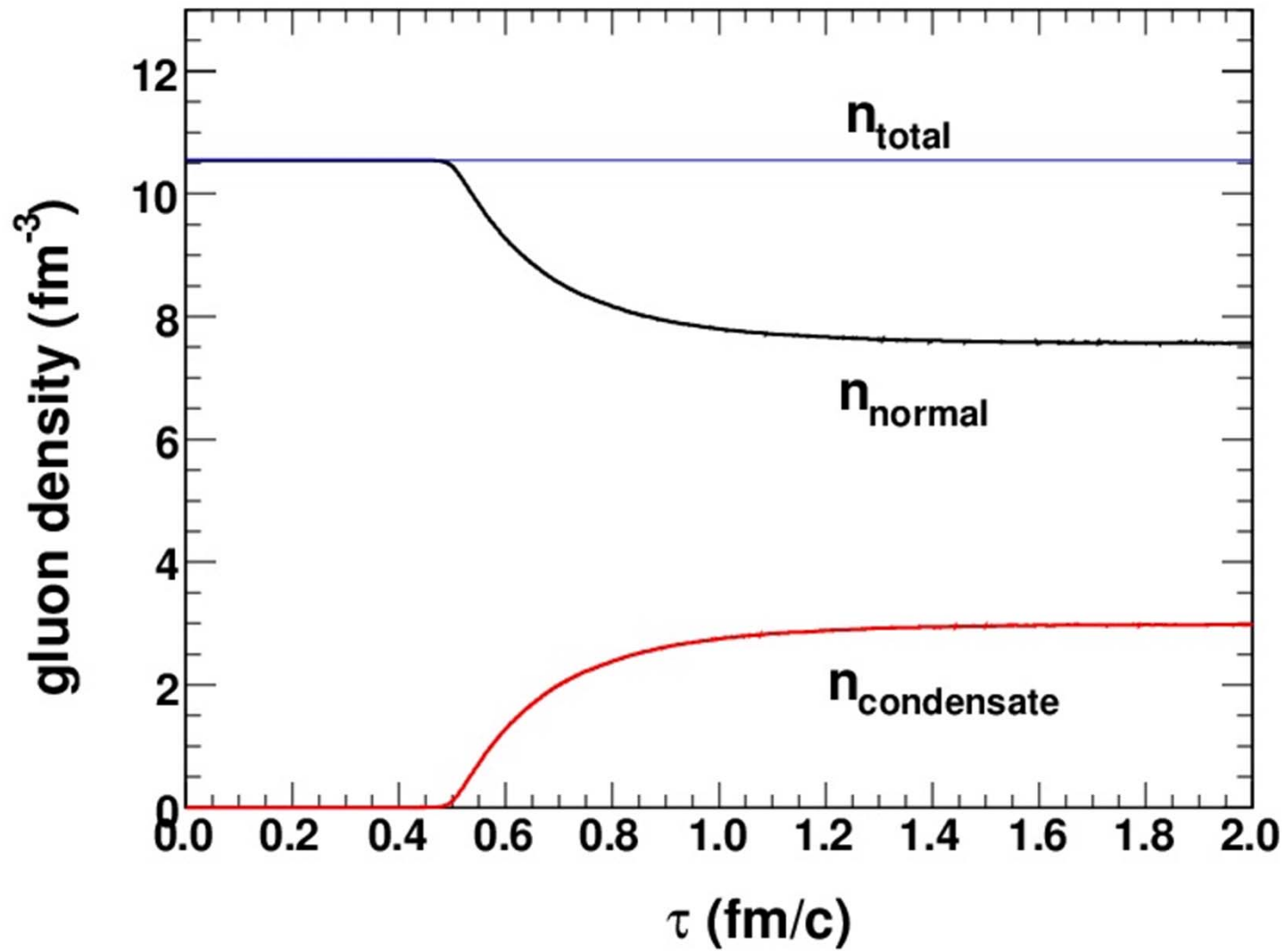
Overpopulation = the system contain more gluons than can be accommodated by a Bose-Einstein distribution

initially: $f_{init}(p) = f_0 \theta(1 - p/Q_s)$ expected final: $f_{eq}(p) = 1/(e^{(p-\mu_{eq})/T_{eq}} - 1)$

$$\left. \begin{aligned} \varepsilon_{eq}(T_{eq}, \mu_{eq}) = \varepsilon_0 &= \int \frac{d^3 p}{(2\pi)^3} \frac{p}{e^{(p-\mu_{eq})/T_{eq}} - 1} \\ n_{eq}(T_{eq}, \mu_{eq}) = n_0 &= \int \frac{d^3 p}{(2\pi)^3} \frac{1}{e^{(p-\mu_{eq})/T_{eq}} - 1} \end{aligned} \right\} \begin{aligned} f_{critical} &= f_0 = 0.154 \\ \text{even for } \alpha_s &\sim 0.3, \\ \text{still highly } &\text{overpopulated} \end{aligned}$$

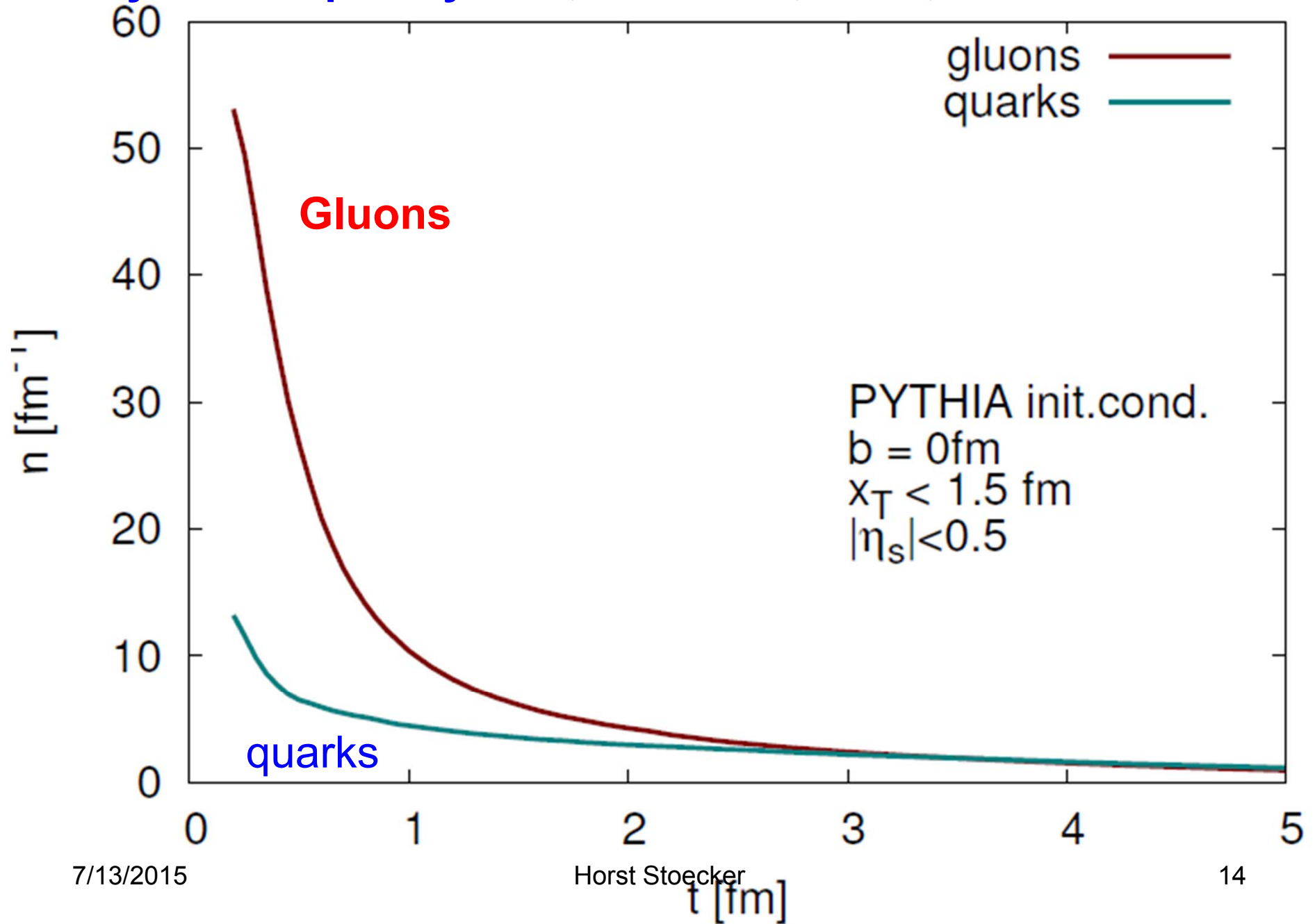


Kai Zhou, Goethe U.



Kai Zhou, Zhe Xu, Carsten Greiner,

Gluon yields & quark yields, F. Senzel, Z. Xu, C. Greiner BAMPS



Extreme Computing Challenges !!!

=> the **FAIR** Tier 0 **GreenCube** Data Center



*****No. 1*** Green500: Nov. 2014**

5.27 GFlops/Watt - World Record

L-CSC GSI Darmstadt PUE <1.07

powerefficient Supercomputer

AMD FirePro GPU, Intel Xeon CPU

Tier-0 data center: FAIR **GreenCube**

Helmholtz funding 770 Racks 2.2m

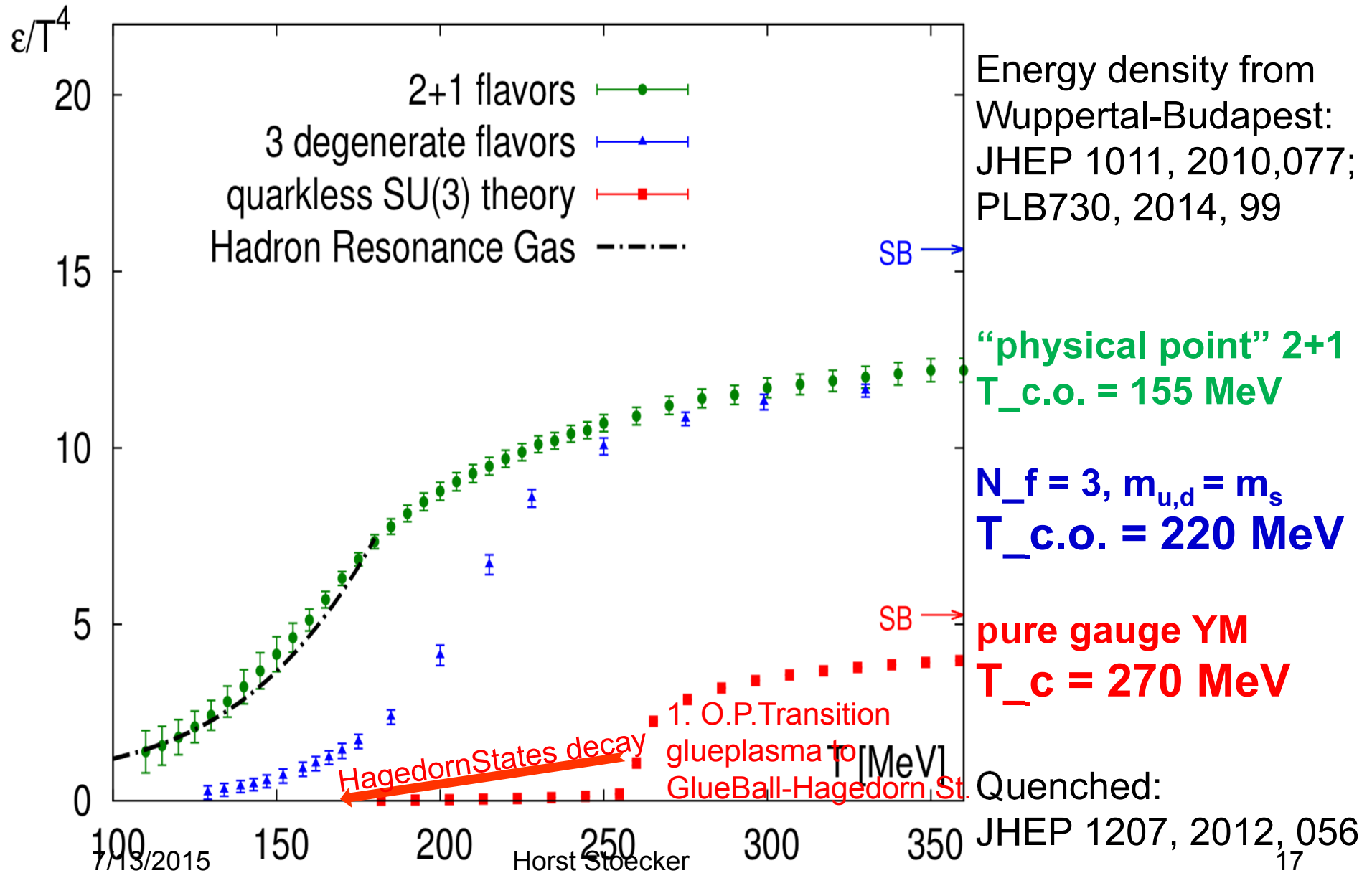
- 12 M€ building cost
- 7 M€ initial HPC installation
- Completion of CC in Q4/2015
- Max cooling power 12 MW
- Fully redundant (N+1)



Lattice QCD vs pure YM: glueballs

Pure YM LGT vs. 2+1 flavor Lattice QCD

Energy density (EoS) **DIFFERENT** for different **quark masses**



Time evolution of high multiplicity pp at RHIC and LHC in pure YM scenario

Alternate Scenario: pure gauge matter in pp, pA – AA ?

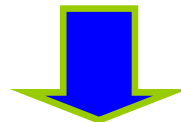
Initial Color Glass Condensate \longrightarrow Glasma thermalizes
fast equilibration of Gluons, **slow** equil. of quarks
high pressure, entropy **gluon** plasma
 \longrightarrow **fast** hydrodynamic expansion of **gluon** plasma.



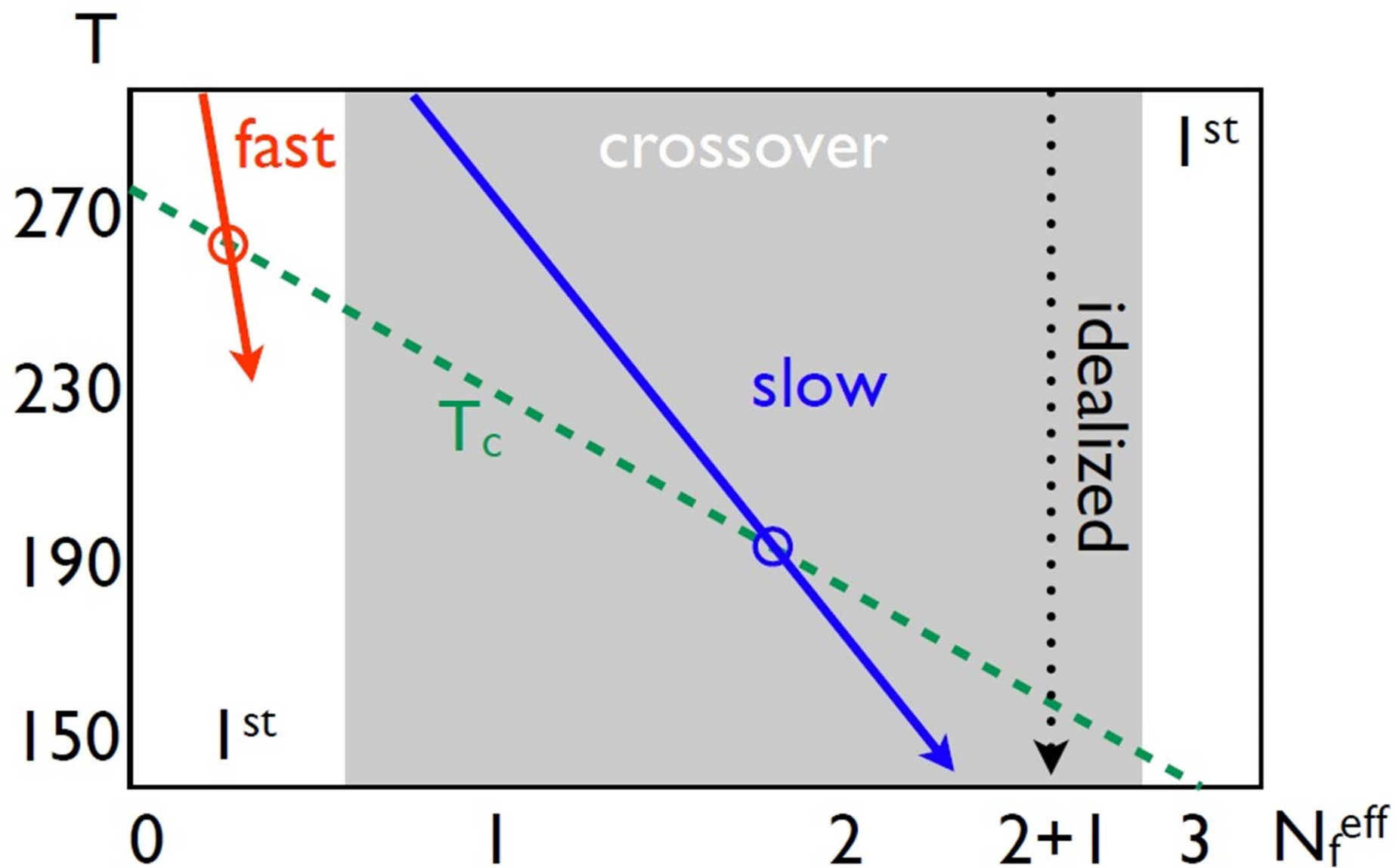
1. Order Phase Transition at $T_c = 270$ MeV of flavorless QCD.



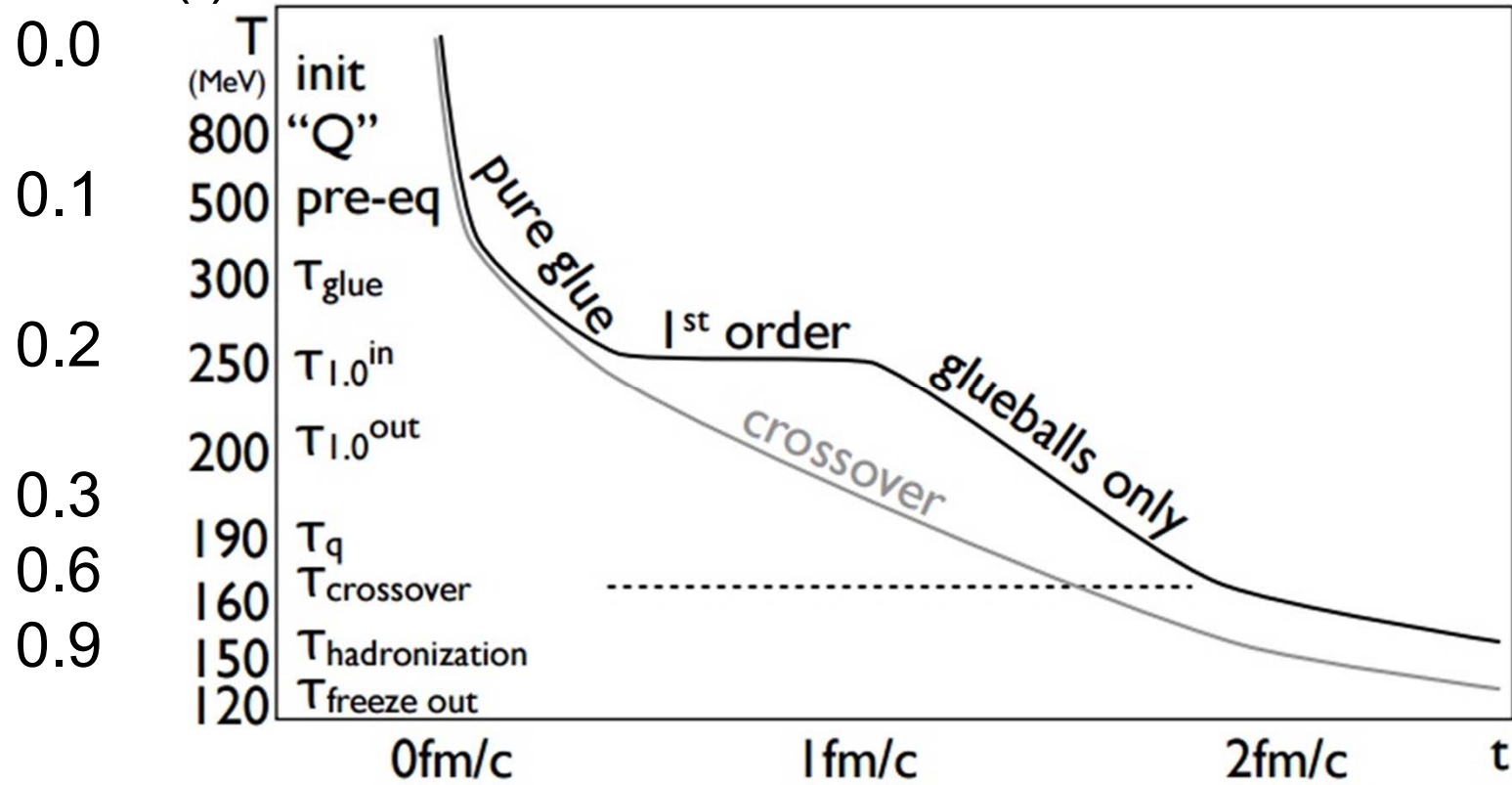
Transition from glue plasma in GlueBall fluid



Glueballs' Hagedorn states decay directly into Hadrons
Comparison of theory with the experiments tests our
understanding of QCD matter.

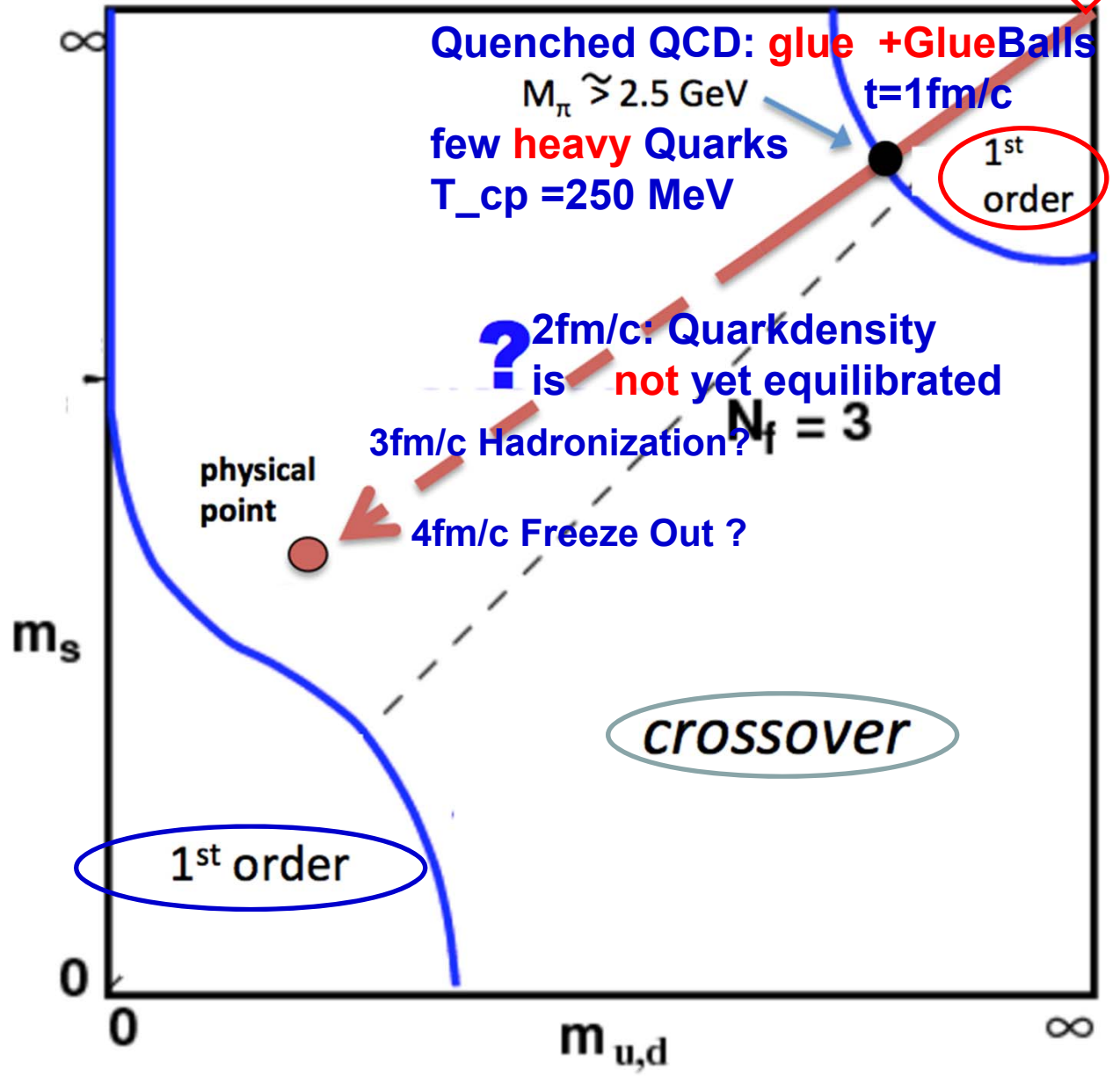


Eff.Nf(t)



Eff.Nf(t): 0.0 0.1 0.2 0.3 0.6 0.9

LHC/FCC: time evol. high mult. pp & AA $t=0.1\text{fm}/c$ pure gauge: glue only! No Quarks!



i neory
 Columbia Plot: Order of
 Phase Transition

„Time dependence“ in Columbia plot: $N_f(t)$

pp (& AA?) initial: Color Glass Condensate $t=0.1\text{fm}/c$:
glue thermalizes fast ~ **pure glue-plasma**: $N_f(t=0.1)=0.1$

Expansion

Pure Yang Mills Lattice gauge theory:
1. **Order Phase Transition @ $T_c = 270\text{MeV}$**
From glue plasma to **GlueBall** fluid

Expansion to critical point

$T_{cp} = 240\text{ MeV}$ $t \sim 2\text{ fm}/c$

more and more quarks produced

$N_f(t=2\text{fm}/c) \sim 0.6$

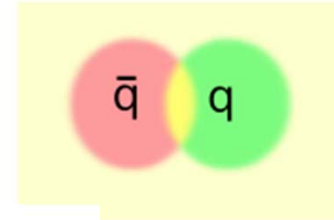
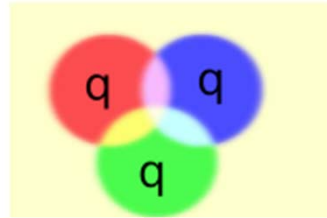
GlueBalls, Hagedorn States Mix

Sequential 2-body decays
of Glueball-Hagedorn
States can well explain
the observed hadron
yield ratios.

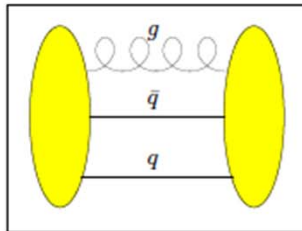
Glueballs !?

Beyond standard quark configurations

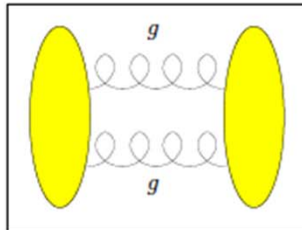
- QCD allows much more than what we have observed:



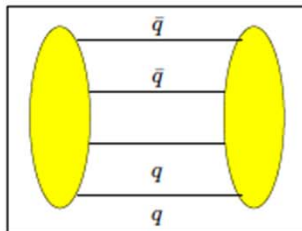
Exotica



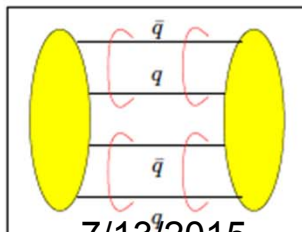
hybrid:
with gluon excitation



glueball:
pure gluon state



4 quark state:
compact 4-quark state

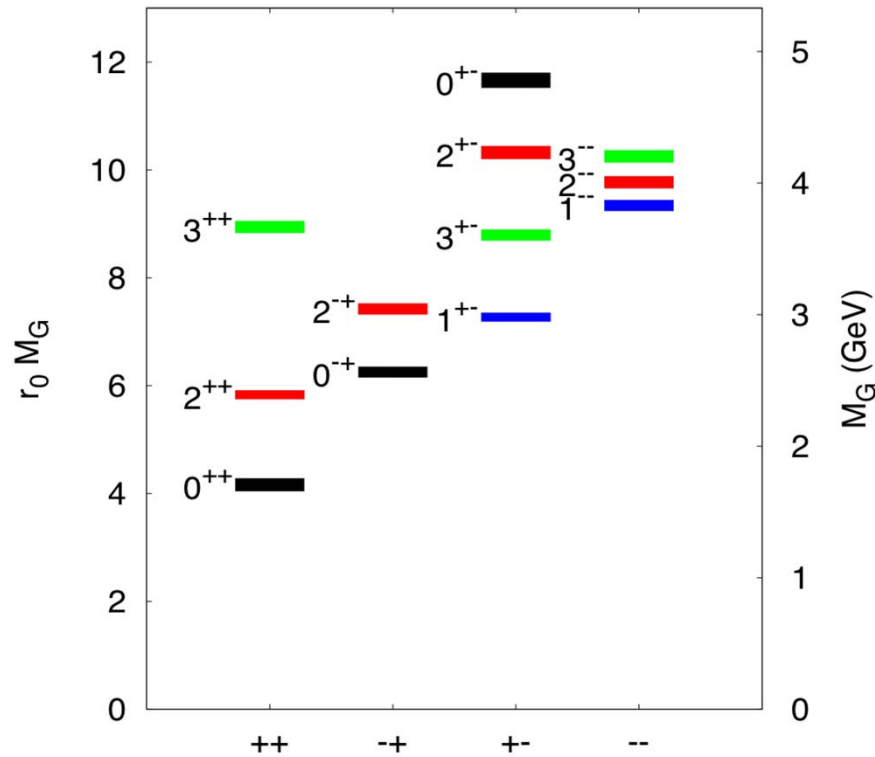


hadronic molecule:
bound state of two mesons

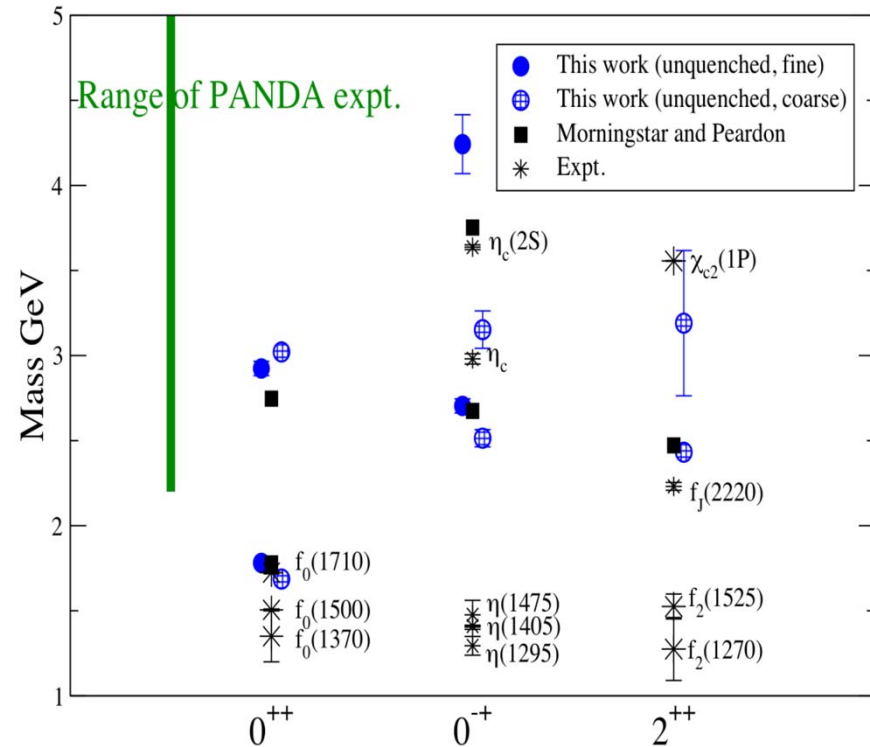
Mesons

} may have J^{PC}
not allowed for qq

Glueball spectrum



Quenched results:
Morningstar-Peardon
Phys.Rev. D73 014516 ('06)



First unquenched results:
pion mass 360 MeV
UKQCD coll. PRD82 ('10) 34501

GlueBall-Matter at RHIC, LHC, FCC

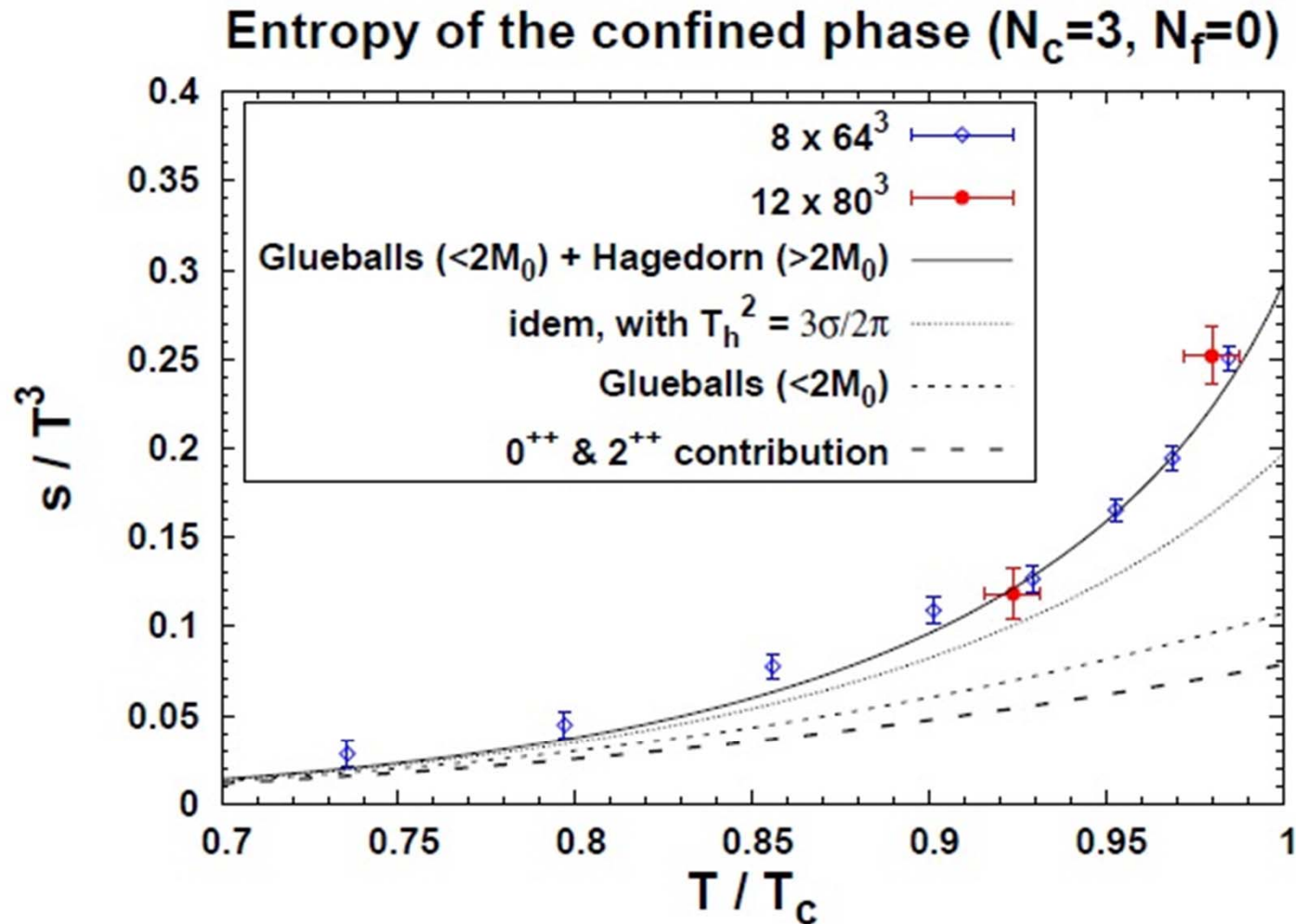
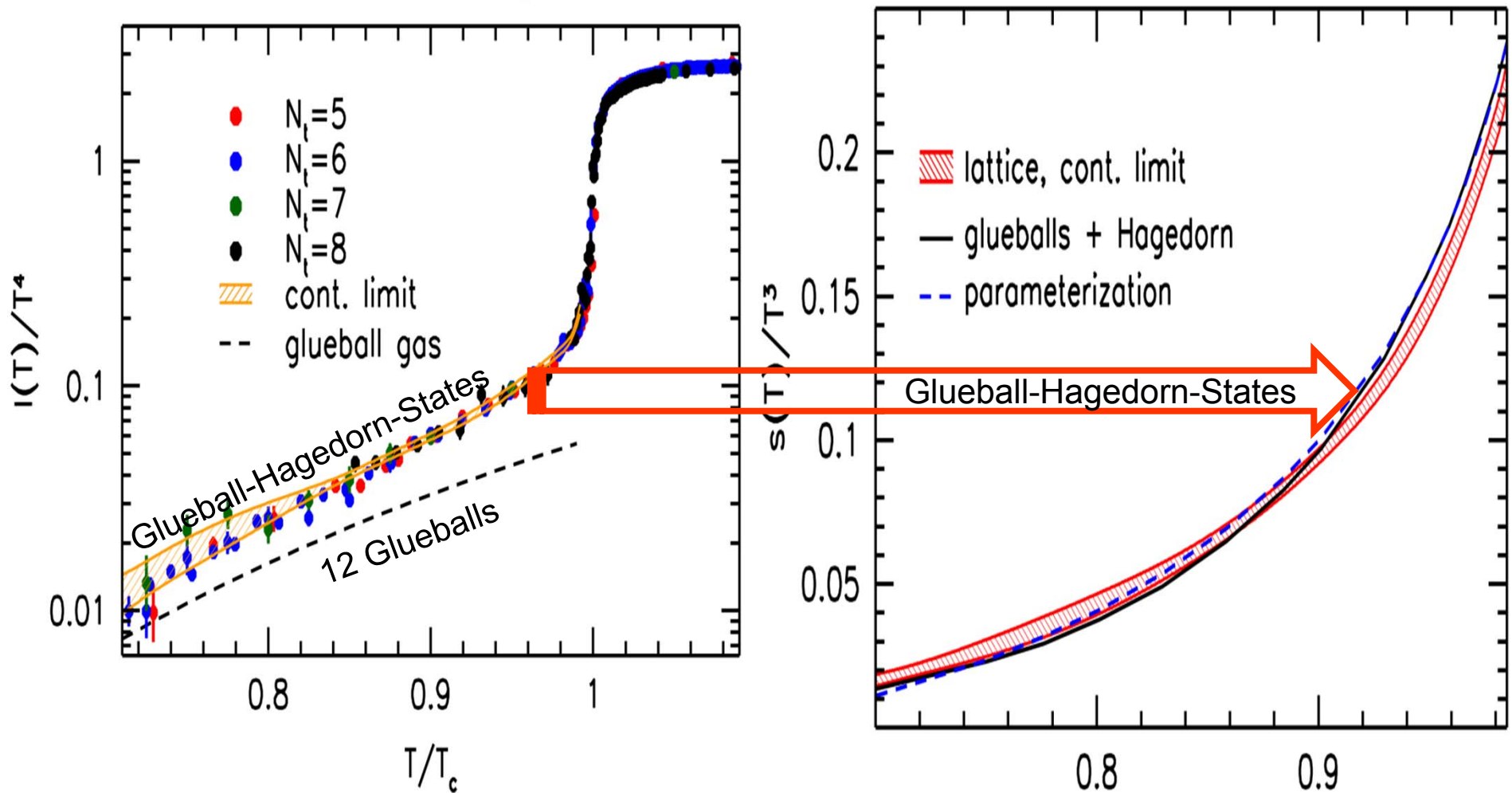


FIG. 3: The entropy density in units of T^3 for $LT = 8$. We applied a (modest) volume-correction to the $N_t = 12$ data.

Thermodynamics of the GlueBall fluids



Wuppertal-Budapest (W.-B.) Collaboration: JHEP 1207 56 ('12)
 High precision continuum result for the quenched equation of state. T/T_c

The low temperature behavior up to the transition point
 can be described by the glueball spectrum.

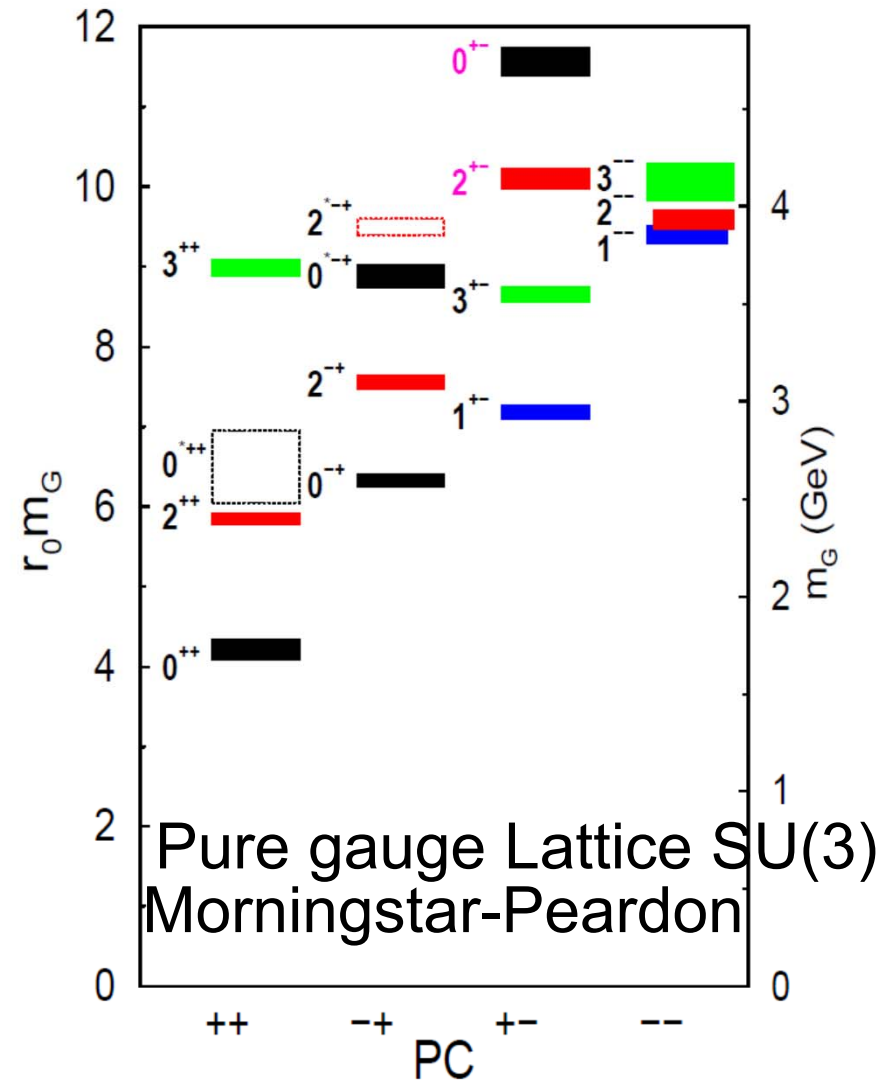
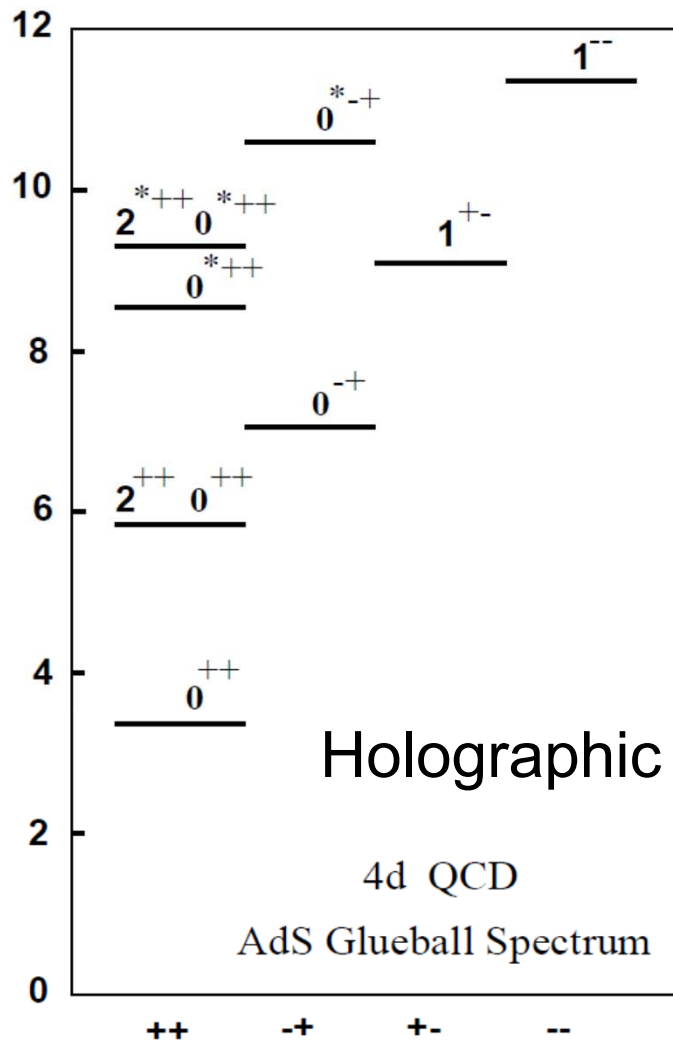
W.-B. used 12 glueball states from Morningstar-Pearson
 plus a Hagedorn particle tower (as proposed by Harvey Meyer).

7/13/2015

Holographic vs. lattice glueball spectra
Seiji Terashima, YITP, Kyoto,
Koji Hashimoto, Riken, Chung-I Tan, Brown

Holographic vs. lattice glueball spectra

Seiji Terashima, YITP, Kyoto, Koji Hashimoto, Riken, Chung-I Tan, Brown, arXiv:0709.2208



Brower-Mathur-Tan, 2000
 $P_\tau = -1$ dropped

Adding quarks in AdS/CFT: holographic QCD

Terashima et al

- Adding N_f flavors → adding another kind of D-branes as probe. Karch-Katz
Myers et.al.
Sakai-Sugimoto
- Here, we add N_f pairs of **D8-brane and anti-D8-brane**.
This model has spontaneously broken chiral symmetry,
so there is **massless pion**.

Let us consider **gravity dual**, i.e. the **D8-branes in the Witten's background**.
(D8-brane and anti-D8-brane are connected and
become smooth curved D8-branes as a result of the curved background.)

The D8-brane action is

$$S_{D8} = -(2\pi\alpha')^2 \mathcal{T}_{D8} \text{Tr} \int d^9x e^{-\Phi} \sqrt{-\det \tilde{g}} \frac{1}{4} \tilde{g}^{PR} \tilde{g}^{QS} F_{PQ} F_{RS} + S_{\text{Chern-Simons}}$$

where F is the field strength of the 9-dim. gauge fields on the \mathbb{R}^9

Generic feature of **holographic glueball decay**

Terashima et al

- Glueballs are obviously flavor-blind. Thus couplings to mesons are universal against flavors.
- From the D8-brane action,

$$S_{D8} = -(2\pi\alpha')^2 \mathcal{T}_{D8} \text{Tr} \int d^9x e^{-\Phi} \sqrt{-\det \tilde{g}} \frac{1}{4} \tilde{g}^{PR} \tilde{g}^{QS} F_{PQ} F_{RS} + S_{\text{Chern-Simons}}$$

we see that

- (1) No glueball interaction involving more than two pions. because π appears in A_z but there are no $(A_z)^n$ terms with $n > 2$

Decay of any glueball to $4\pi_0$ is suppressed. Prediction of the holographic QCD!

- (2) Direct couplings of a glueball with more than five meson are suppressed. (implies “vector meson dominance”): No A^5 term

These are from “Holographic gauge” choice

But no mixing between **lightest glueball** and meson

Terashima et al

- Scalar mesons = transverse scalar of D8-branes, denoted by y , which is essentially τ .
- Terms linear in y in the D8-action is:

$$\begin{aligned} g_{\nu y}|_{y=0} \partial_\mu y(z, x^\mu), & \quad g_{\nu y}|_{y=0} \partial_z y(z, x^\mu), \\ y[\partial_y g_{\tau\tau, rr, \mu r, \mu\nu}]_{y=0}, & \quad y[\partial_y \phi]_{y=0}, \\ g_{zy}|_{y=0} \partial_\mu y(z, x^\mu), & \quad g_{zy}|_{y=0} \partial_z y(z, x^\mu), \end{aligned}$$

All of these vanish for the lightest glueball.

No mixing with mesons at order $1/\sqrt{N_c}$

This is very important to distinguish the glueball and meson.

Decay of lightest scalar glueball

Terashima et al

Lightest glueball mass is $M = \sqrt{7.31/9}M_{KK}$

ρ meson mass is $m_\rho = \sqrt{\lambda_1}M_{KK} = \sqrt{0.669}M_{KK}$

We have $m_\rho < M < 2m_\rho$. Thus no 2 ρ -meson decay
in holographic QCD

(In the experiment, $M=1507\text{MeV}$, $m_\rho=775\text{MeV}$)

We will use

$$\lambda N_c / 108\pi^3 = 7.45 \times 10^{-3}$$

$$N_c = 3$$

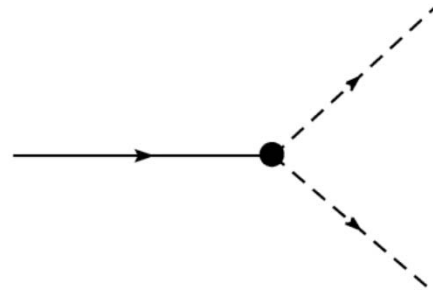
Possible decay process (from kinematics)

(a) $G \rightarrow \pi\pi$ (figure 1)

(b) $G \rightarrow \rho\pi\pi$, $G \rightarrow \rho\rho \rightarrow \rho\pi\pi$ (figure 2)

(c) $G \rightarrow \rho\pi\pi \rightarrow \pi\pi\pi\pi$, $G \rightarrow \rho\rho \rightarrow \pi\pi\pi\pi$ (figure 3)

(d) $G \rightarrow \eta'\eta'$ (figure 1)



Branching ratio for $f_0(1500)$:

(a) 35%

(b)+(c) 49%

(d) 7 %

Figure 1: A glueball G decaying to two pions π .

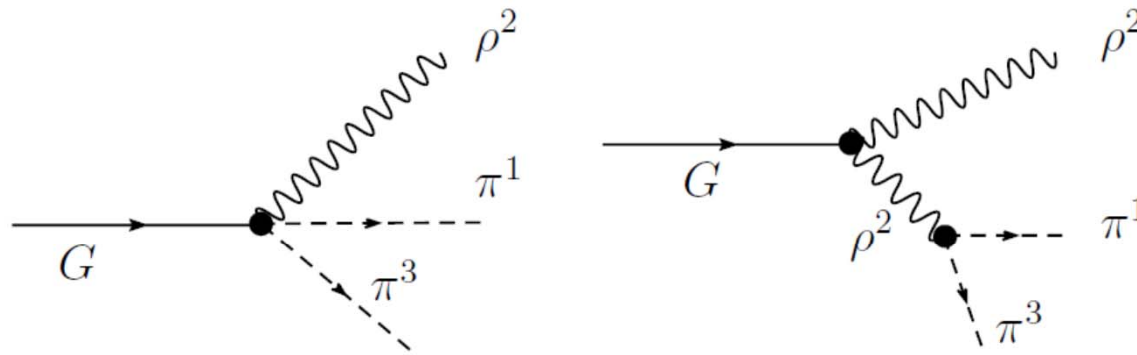


Figure 2: A glueball G decaying to two pions π and a single ρ . There are two graphs, the decay with a single vertex (Left) and the decay with two vertices (Right).

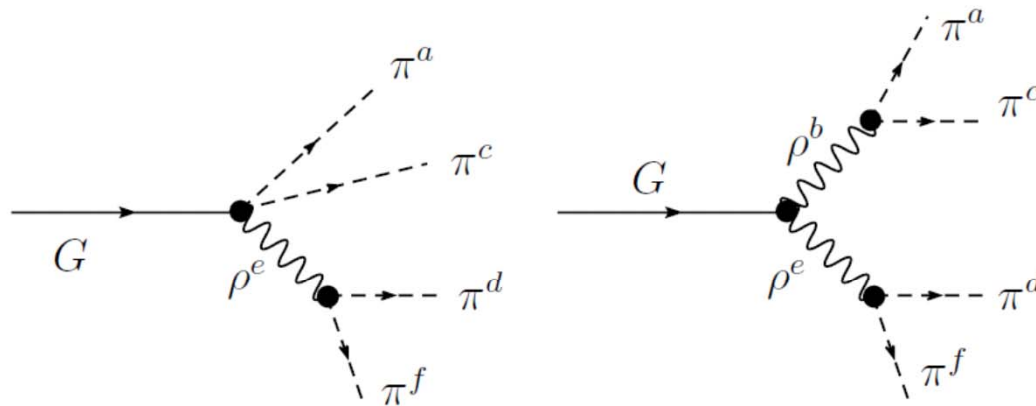


Figure 3: A glueball G decaying to four pions π . There are two graphs, the decay with two vertices (Left) and the decay with three vertices (Right).

From the effective action we have, we can compute the decay width.

For $G \rightarrow \pi\pi$ $\frac{\Gamma_{G \rightarrow \pi\pi}}{M} = 0.040.$

Experimentally, $\frac{\Gamma_{G \rightarrow \pi\pi}^{(\text{ex})}}{M} = \frac{109}{1507} \times 34.9\% = 0.0252.$

Good agreement.

$$G \rightarrow \rho\pi\pi \quad \text{and} \quad G \rightarrow 4\pi$$

$$\frac{\Gamma_{G \rightarrow \rho\pi\pi}}{M} \sim 1.3 \times 10^{-6} \quad \frac{\Gamma_{G \rightarrow 4\pi}}{M} \sim 2.2 \times 10^{-5}$$

This is too small, but if we set M/m_ρ to the experimental value by hand, we have

$$\frac{\Gamma_{G \rightarrow \rho\pi\pi}}{M} = 0.096 \quad \frac{\Gamma_{G \rightarrow 4\pi}}{M} \sim 0.0087$$

Thus
$$\frac{\Gamma_{G \rightarrow 4\pi} + \Gamma_{G \rightarrow \rho\pi\pi}}{M} \sim 0.105$$

Experimentally,
$$\frac{\Gamma_{G \rightarrow 4\pi}^{(\text{ex})}}{M} = \frac{109}{1507} \times 49.5\% = 0.0358$$

Consistent

(In particular, taking into account the masslessness of the pions)

Terashima et al: First attempt in computing decays of glueballs to mesons using a holographic QCD (Sakai-Sugimoto model).

The holographic QCD is, in principle, equivalent to QCD.

We therefore expect that the holographic approach should provide interesting information on strong coupling physics of QCD.

Explicit couplings between the lightest glueball and the mesons are given, and the associated decay products/widths are calculated.

Our results are consistent with the experimental data of the decay for the $f_0(1500)$ which is thought to be the best candidate of a glueball in the hadronic spectrum.

We have shown that there is no mixing with the mesons at the leading order.

Decay of any glueball to $4\pi_0$ is suppressed.

This is a prediction of the holographic QCD!

Decay of Hagedorn state glueballs

Beitel, Gallmeister, Carsten Greiner

Bootstrap (courtesy Max Beitel, Kai Gallmeister, Carsten Greiner)

cf. S. Frautschi, PRD 3 (1971) 2821

C. Hamer, S. Frautschi, PRD 4 (1971) 2125

■ Assumption: only 2-body (detailed balance!)

$$\vec{C} = (B, S, Q)$$

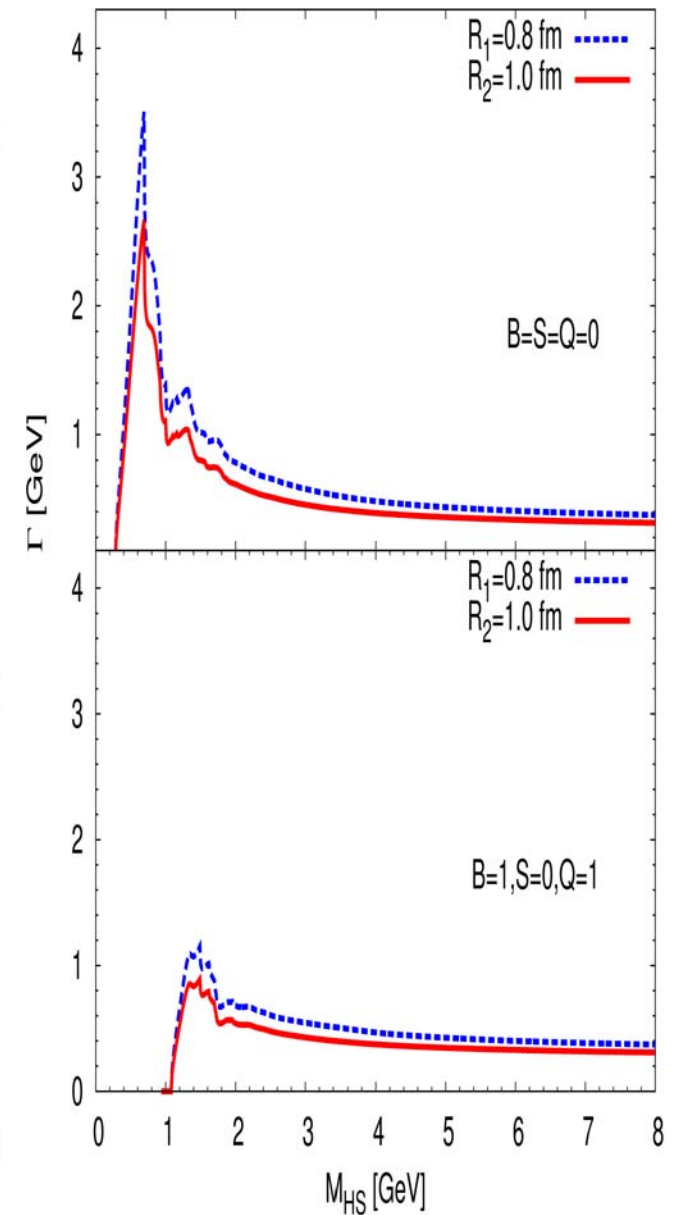
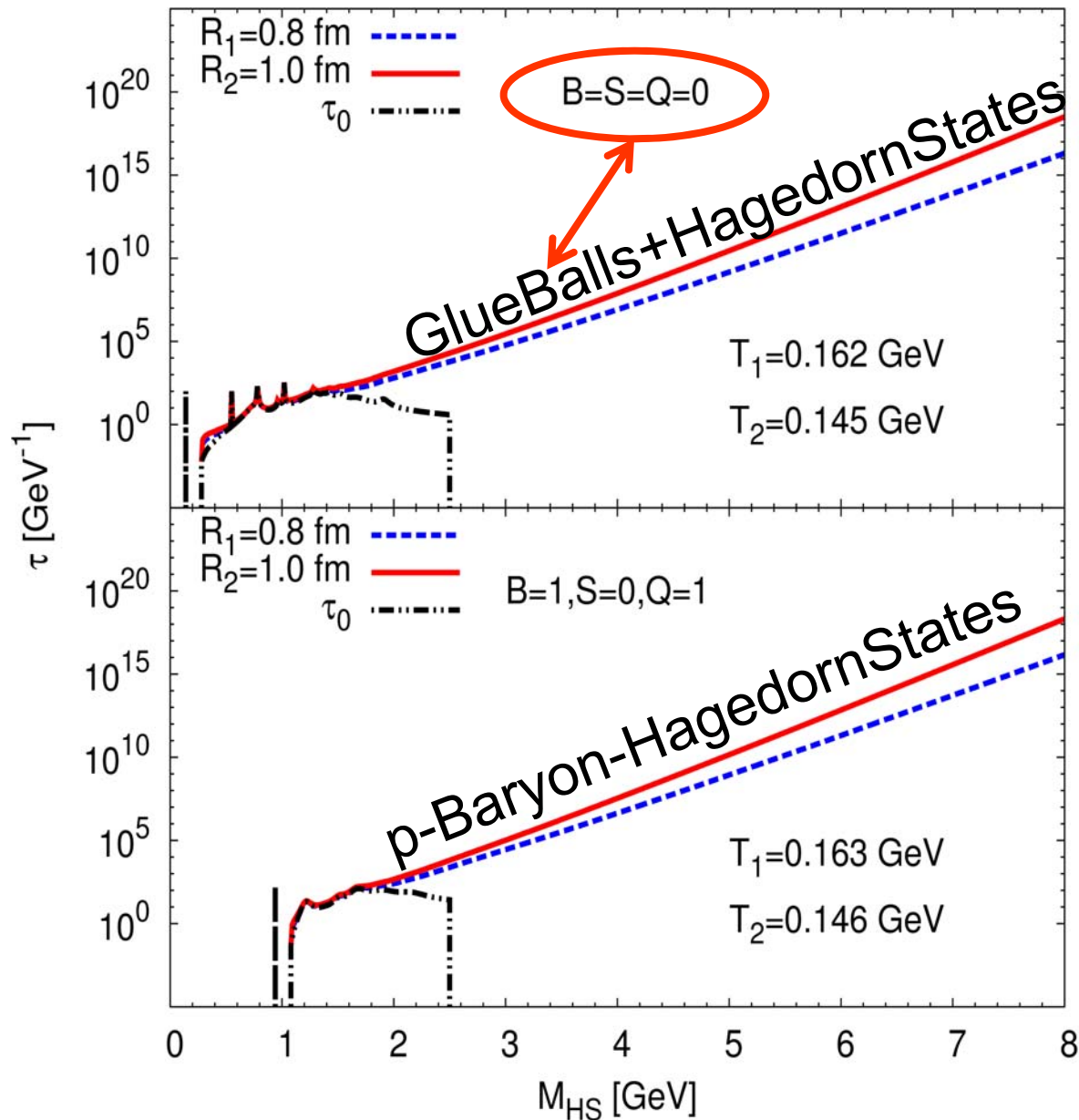
■ Bootstrap equation

$$\begin{aligned} \tau_{\vec{C}}(m) &= \frac{R^3}{3\pi m} \sum_{\vec{C}_1, \vec{C}_2} \iint dm_1 dm_2 m_1 \tau_{\vec{C}_1}(m_1) m_2 \tau_{\vec{C}_2}(m_2) \\ &\quad \times p_{\text{cm}}(m, m_1, m_2) \delta(\vec{C} - \vec{C}_1 - \vec{C}_2) \end{aligned}$$

■ Total decay width (via detailed balance)

$$\begin{aligned} \Gamma_{\vec{C}}(m) &= \frac{\sigma}{2\pi^2 \tau_{\vec{C}}(m)} \sum_{\vec{C}_1, \vec{C}_2} \iint dm_1 dm_2 \tau_{\vec{C}_1}(m_1) \tau_{\vec{C}_2}(m_2) \\ &\quad \times p_{\text{cm}}^2(m, m_1, m_2) \delta(\vec{C} - \vec{C}_1 - \vec{C}_2) \end{aligned}$$

GlueBalls & Hagedorn-States: exponentially increasing Mass-Spectra, Width



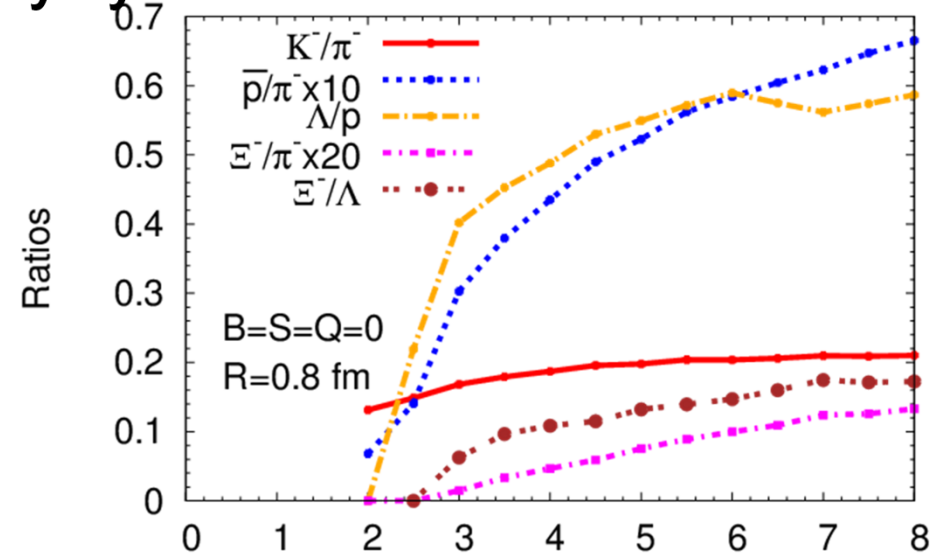
T quite independent of charges

Single HS cascading decay: yield ratios vs ALICE

data: ALICE @

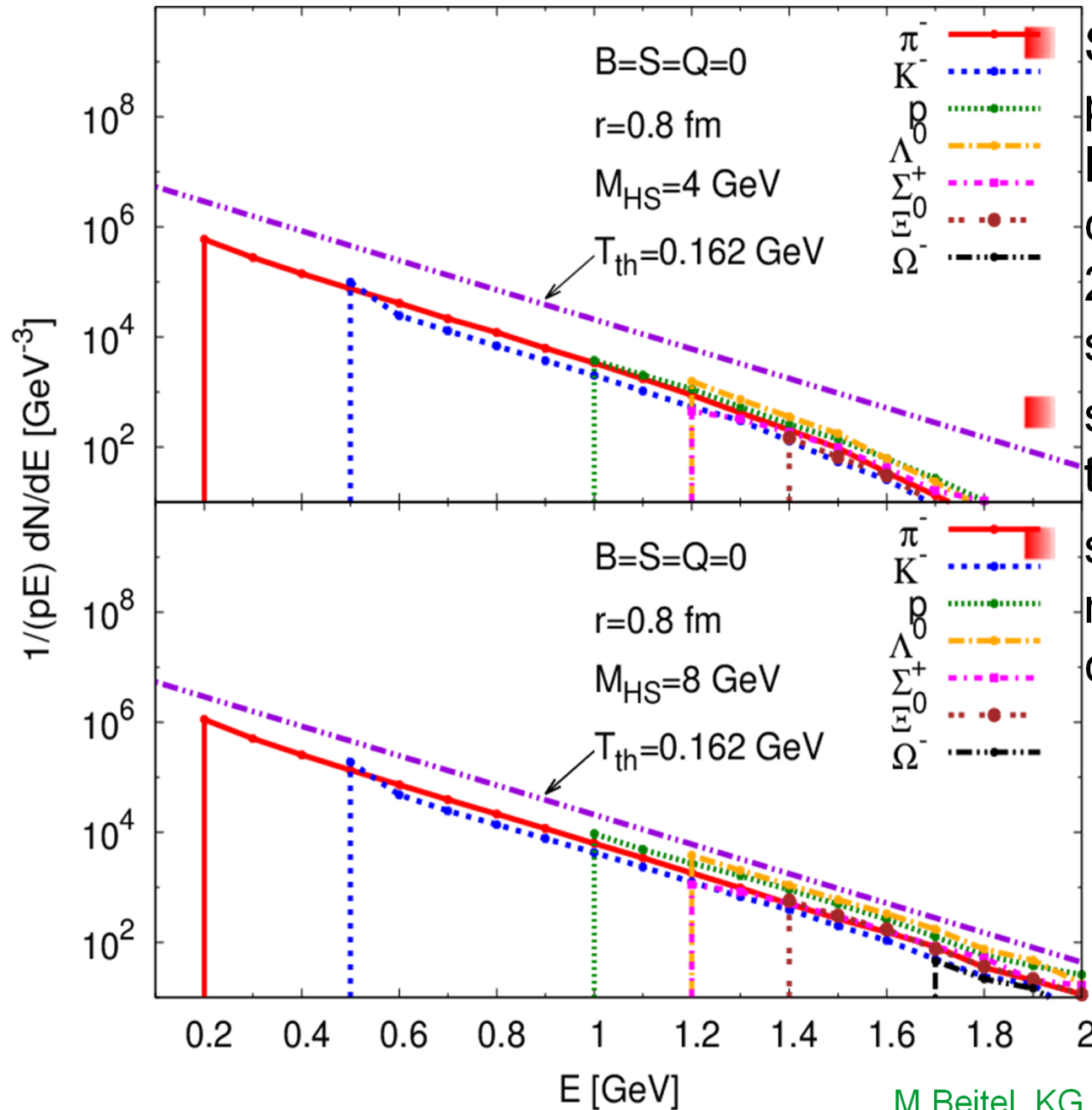
LHC p - p : $\sqrt{s_{NN}} = 0.9 \text{ TeV}$

Pb - Pb : $\sqrt{s_{NN}} = 2.8 \text{ TeV}$



	p-p	Pb-Pb	4 GeV	8 GeV
K^-/π^-	0.123(14)	0.149(16)	0.187	0.210
\bar{p}/π^-	0.053(6)	0.045(5)	0.043	0.066
Λ/π^-	0.032(4)	0.036(5)	0.021	0.038
Λ/\bar{p}	0.608(88)	0.78(12)	0.494	0.579
Ξ^-/π^-	0.003(1)	0.0050(6)	0.0023	0.0066
$\Omega^-/\pi^- \cdot 10^{-3}$	—	0.87(17)	0.086	0.560

Slope of Single 4-GeV GlueBall-like Hagedorn State seq. 2-body decay cascade



Spectra/slopes of decay products of each single Hagedorn State cascading a sequential 2-body decay chain: slopes look **thermal !!!**
 slopes equal Hagedorn temperature !

slope independent of mass, radius, charges of Hagedorn State

Dileptons and Photons from pure glue scenario
VoloGorenstein, Satarov, Mishustin, Csernai et al.

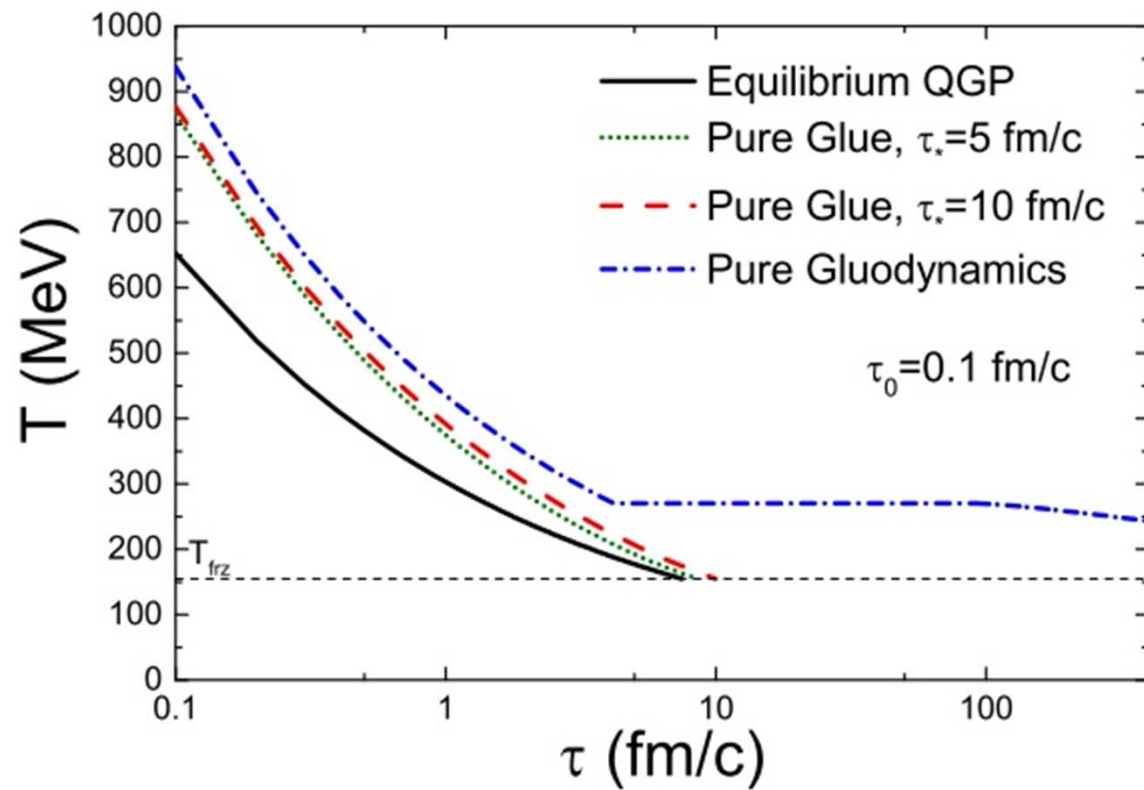
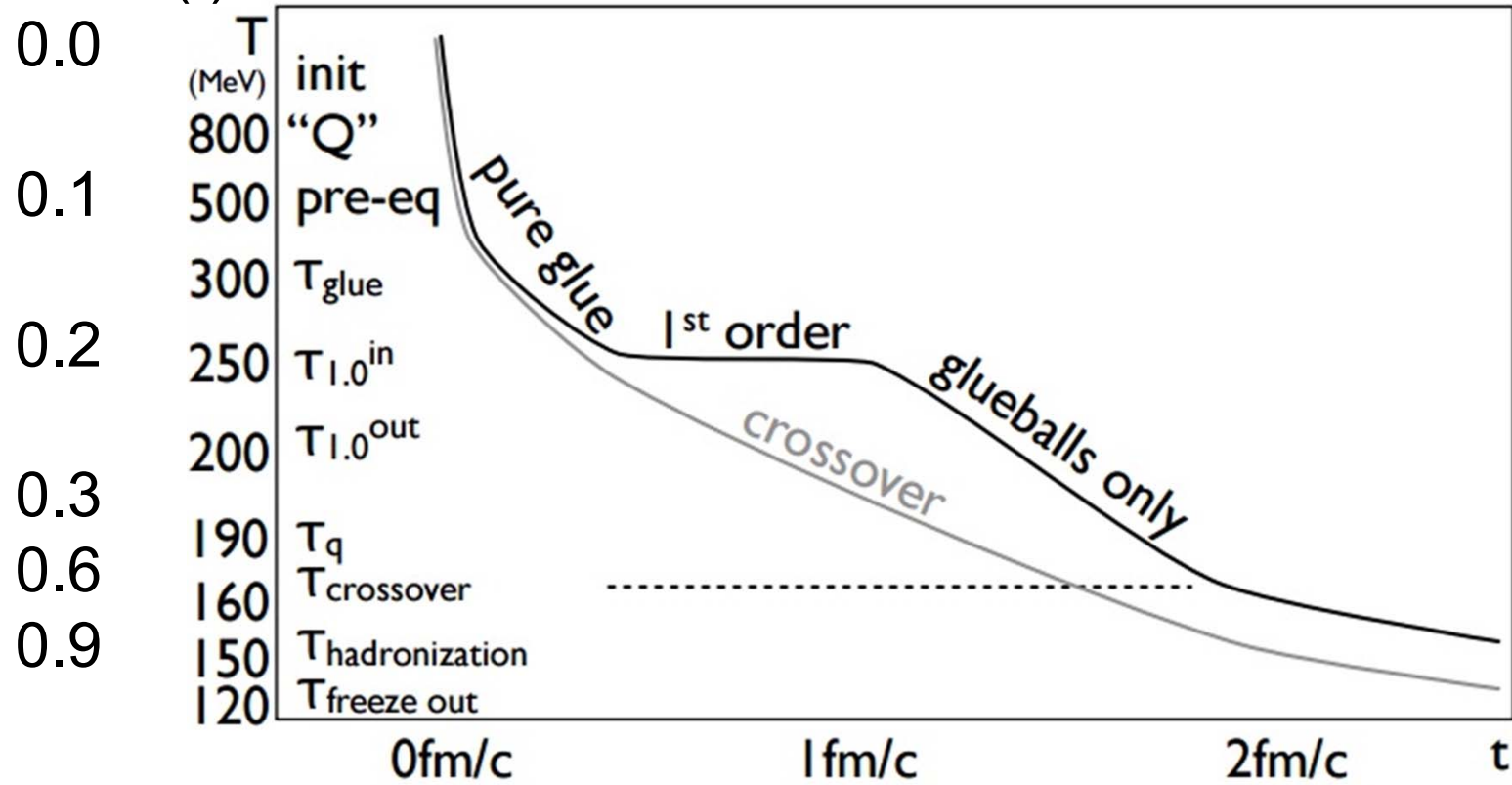


FIG. 6: Dependence of the temperature on the proper time τ for three different system evolution scenarios with $\tau_0 = 0.1$ fm/c, $\tau_* = 5$ fm/c and 10 fm/c.

Eff.Nf(t)



Eff.Nf(t): 0.0 0.1 0.2 0.3 0.6 0.9

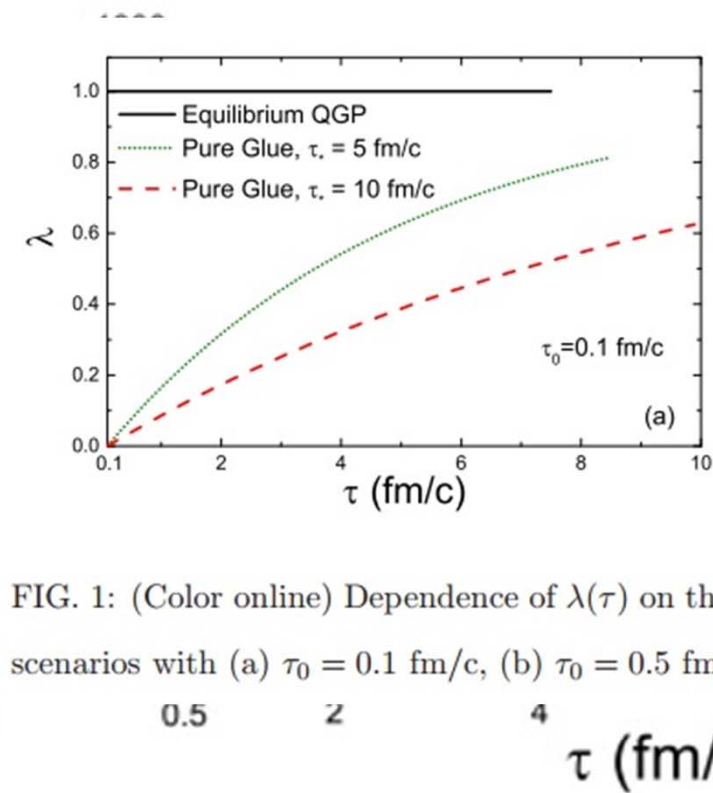
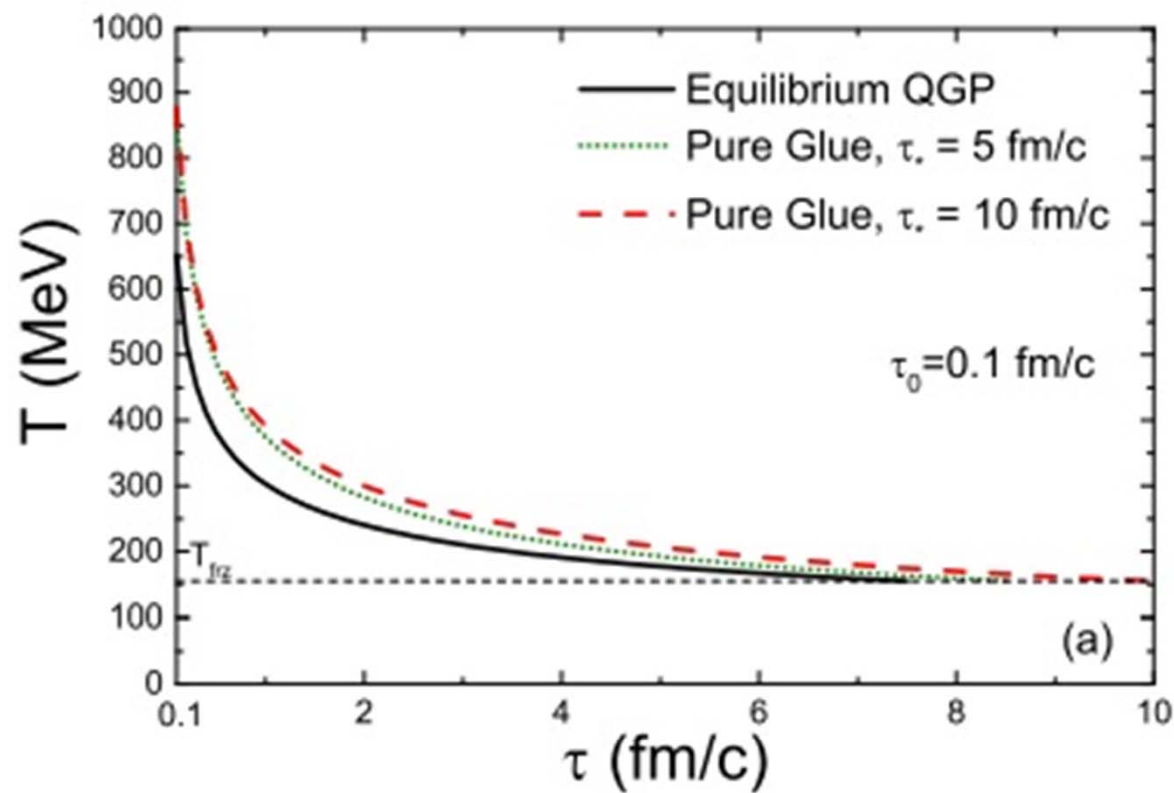


FIG. 1: (Color online) Dependence of $\lambda(\tau)$ on the scenarios with (a) $\tau_0 = 0.1$ fm/c, (b) $\tau_0 = 0.5$ fm

FIG. 2: (Color online) Dependence $T(\tau)$ of the temperature on the proper time system evolution scenarios with (a) $\tau_0 = 0.1$ fm/c, (b) $\tau_0 = 0.5$ fm/c, and $\tau_* = 5$

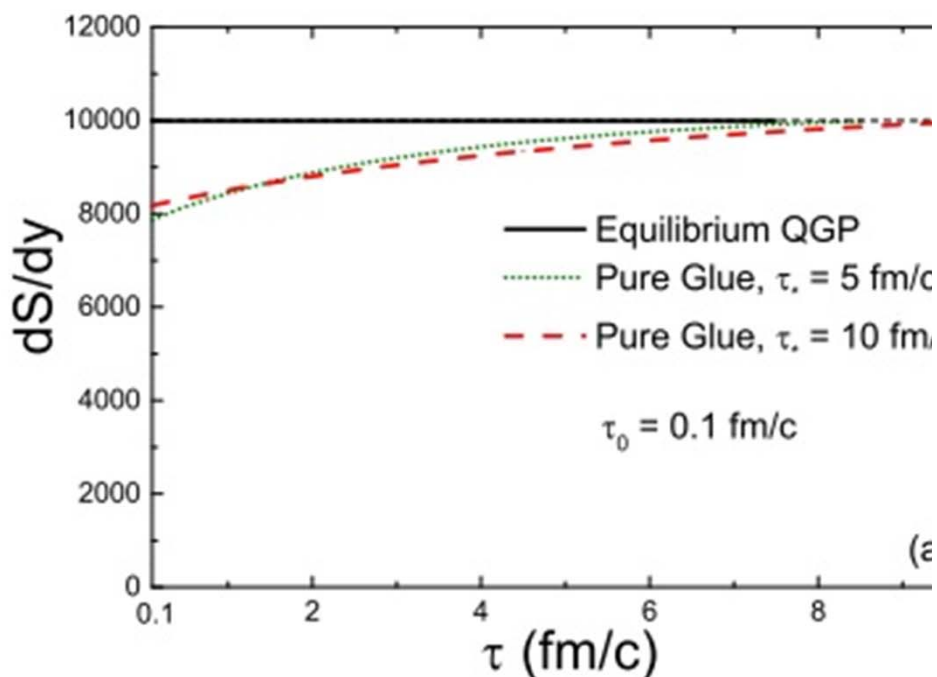
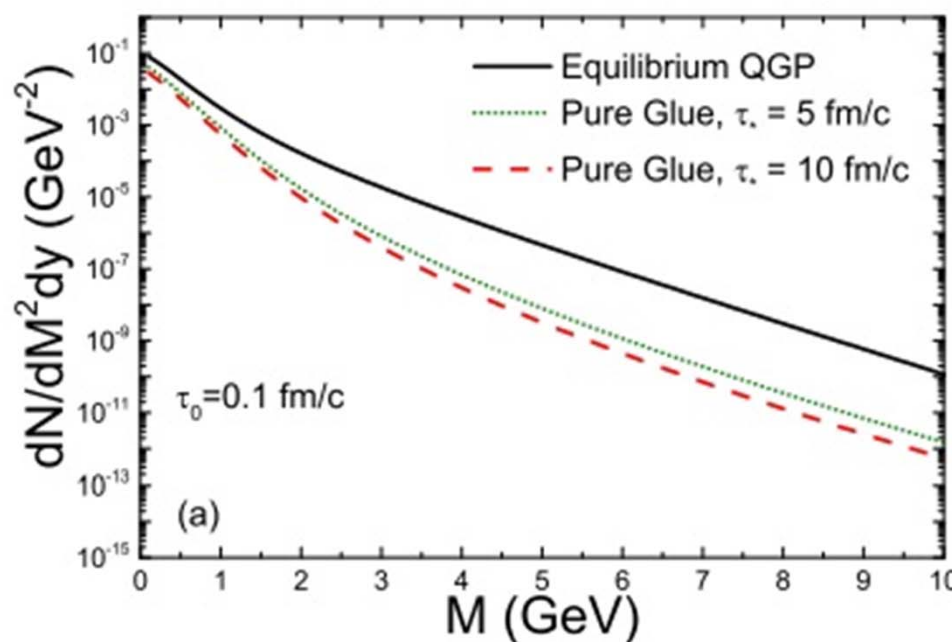


FIG. 3: The τ -dependence of entropy per unit volume evolution scenarios with (a) $\tau_0 = 0.1$ fm/c, (b)

FIG. 4: The thermal dilepton emission rate per invariant mass squared M^2 and unit rapidity calculated for two different system evolution scenarios with (a) $\tau_0 = 0.1$ fm/c, (b) $\tau_0 = 0.5$ fm/c and $\tau_* = 5$ fm/c and 10 fm/c.

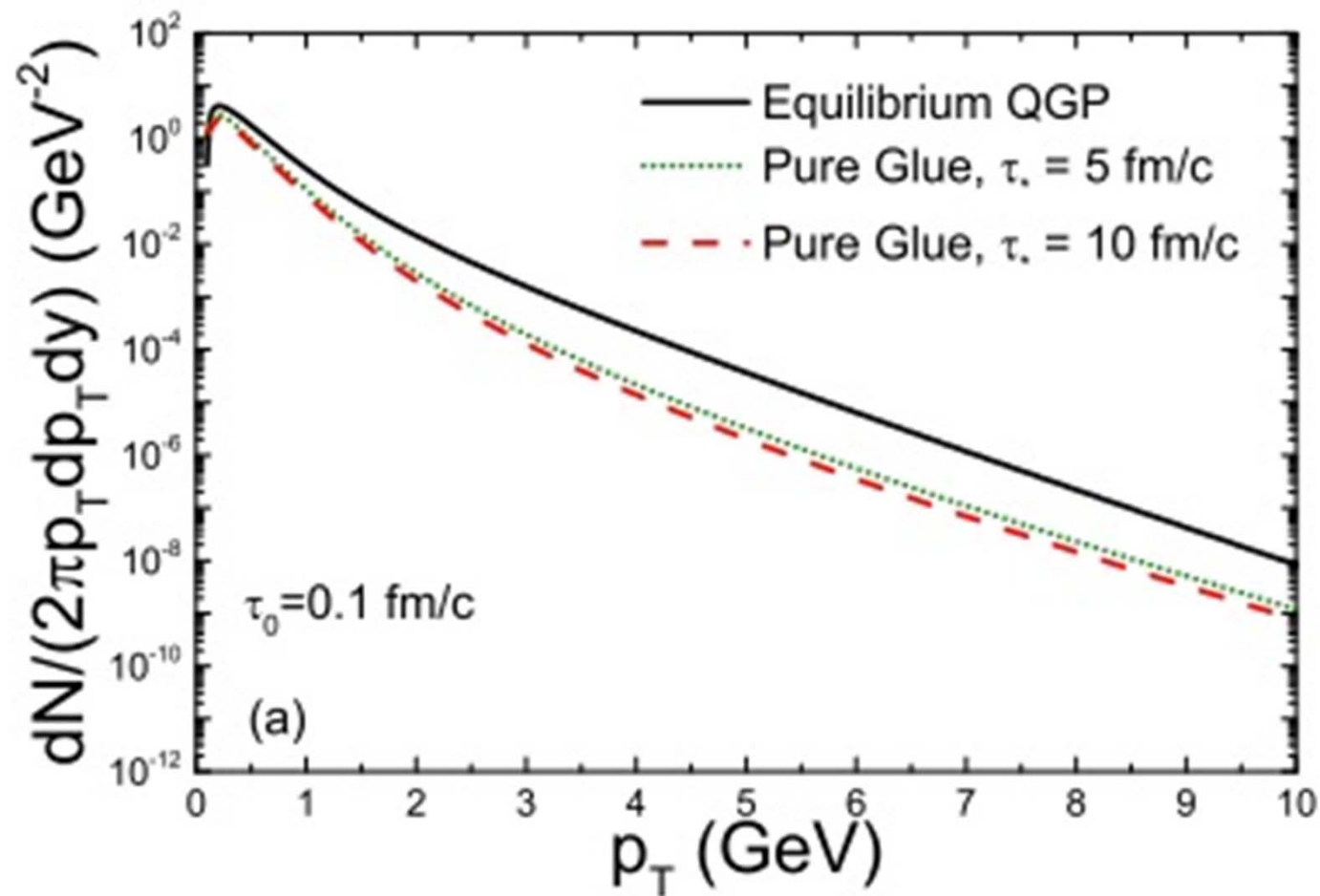


FIG. 5: The transverse distribution of the thermal photons formed with (a) $\tau_0 = 0.1 \text{ fm/c}$, (b) $\tau_0 = 0.5 \text{ fm/c}$

Signatures for **pure glue->glueball** scenario:

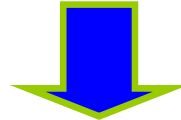
New event-class in **high multiplicity pp & pA**
at RHIC and LHC

time dependence in Columbia plot **LHC – the Glueball Factory...**

- violent **pp** (& AA) collisions
- initial state at LHC:
- Color Glass Condensate
- $t=0.1\text{fm}/c$: glue thermalizes
- **pure glue-plasma created**
- Quenched Lattice $SU(3)_c$:
- **$T_c = 270\text{MeV}$**
- glue plasma -> **GlueBall fluid**
- **1. Order Phase Transition**
- Expansion to critical point
- **$T_{cp} = 240\text{ MeV}$** $t \sim 1-2\text{ fm}/c$
- **GlueBalls** + Hagedorn States Mix
- more and more quarks produced: **$T_{co} = 155\text{MeV}$** crossover transition
- **Observables** from Columbia plot
- $T > T_{cp}$: **Zero e.m. radiation**
- Measure Dilepton intermed. mass
- T_c : **Flow collapse** as barometer
- T_{cp} : **Critical Scattering (MG, WG)**,
- **Kurtosis** , # fluctuations
- $T_c \sim 2 * T_{co} \Rightarrow$
- $P_t(pp) \sim 2 * p_t(AA)$
- $M_{\text{GlueBalls}} < 2\text{GeV}$: „**No**“ Baryons
- **$p/\pi = 0$** : Yield $p + p\text{Bar} \ll$ mesons
- Lightest GlueBall decays:
- - No decays to 2 Omega no 2 Rho
- Glue Flavor blind !
- **$K/\pi = 1$** Yields: Kaons \sim pions

Outlook: Alternative Class of High M events in pp, pA @ LHC – AA?

Initial Color Glass Condensate \longrightarrow Glasma thermalizes
fast equilibration of gluons, **slow** equil. of quarks
high pressure, entropy in **gluon** plasma
 \longrightarrow **fast** hydrodynamic expansion of **gluon** plasma.



1. Order Phase Transition at $T_c = 270$ MeV of flavorless QCD.



Transition from glue plasma in GlueBall fluid



**Glueballs' Hagedorn states decay directly into Hadrons
Comparison of theory with the experiments tests our
understanding of QCD matter.**

Wholehearted Congratulations, **from all of us**, Miklos!

Many thanks, for Your Splendid Hospitality,
to the Wigner Institute

- from the Wuhan Faculty !