

# Rotation and stability of neutrons stars with strong phase transitions

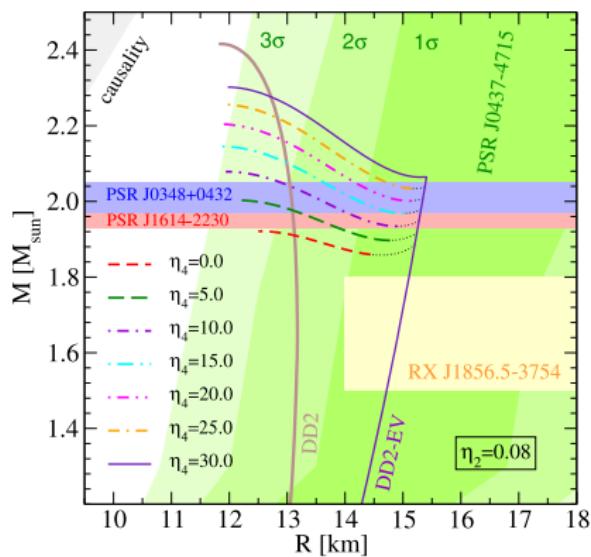
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Annual NewCompStar Conference 2015  
Budapest, 15.6.15

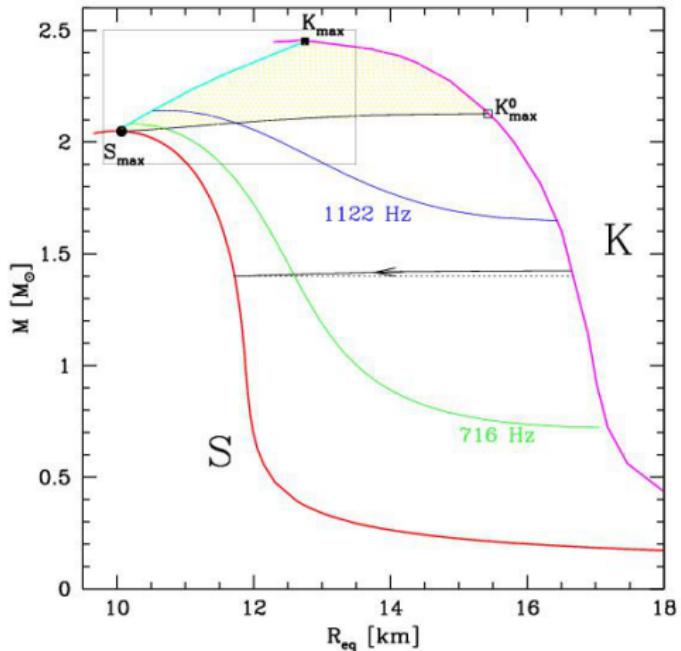


## Quark-core twins – rotating configurations and their stability

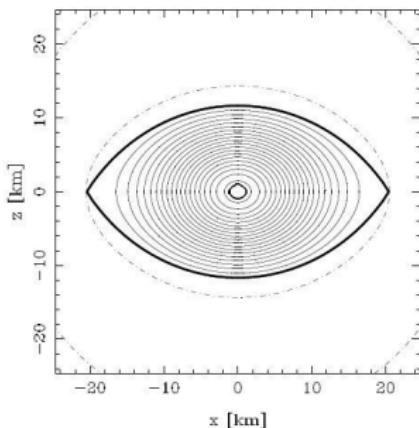


- ★ Since PSR J1614-2230 and PSR J0348+0432, the discussion about exotic (beyond  $npe\mu$ ) dense matter is really interesting
  
- ★ „*A new quark-hadron hybrid equation of state for astrophysics - I. High-mass twin compact stars*”, Benić et al. (2015)  
[arXiv:1411.2856](https://arxiv.org/abs/1411.2856)
  - Exotic quark phase is related to massive NSs.
  
- ★ Here - remarks about the stability of rotating configurations with relation to astrophysics (using DD2-EV  $\eta_2 = 0.12$ ,  $\eta_4 = 5$  EOS)
- ★ results from LORENE/rotstar.

## Rotation on the $M(R)$ diagram



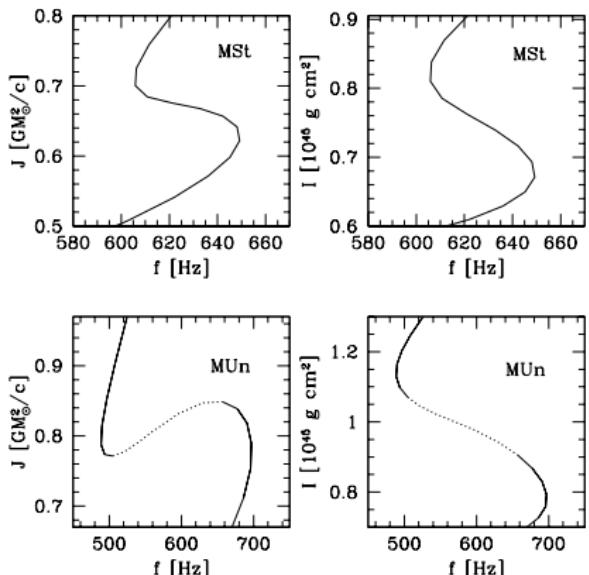
- ★ S: static configurations (TOV),
- ★ K: "Keplerian" (mass-shedding) configuration - maximally-rotating, rigid stars at a given mass,



- ★ in cyan: the instability line (star loses stability w.r.t. axisymmetric oscillations) ★

## Stability indicators: $J$ and $M_b$

Sufficient condition for instability (turning-point criterion):  
Sorkin (1981, 1982), Friedman et al. (1988)★



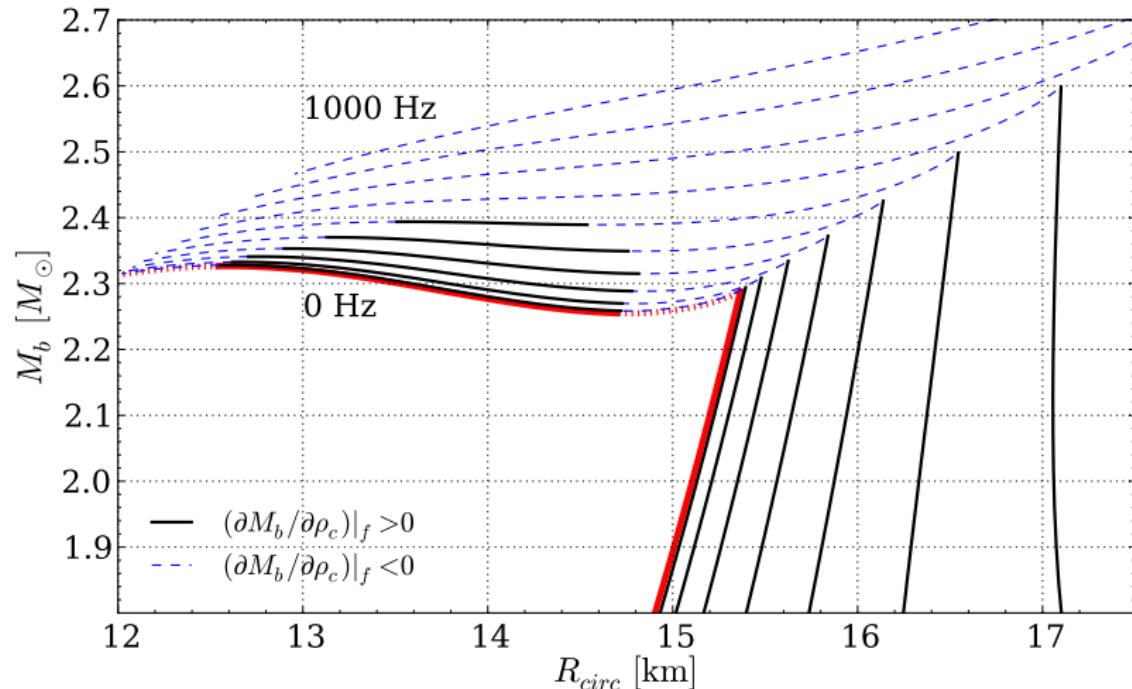
- ★ *Change in stability* corresponds to extremum of  $M$  or  $M_b$  at fixed  $J$ , or to extremum of  $J$  at fixed either  $M$  or  $M_b$ :

$$\left( \frac{\partial M_b}{\partial \lambda_c} \right)_J = 0, \quad \left( \frac{\partial J}{\partial \lambda_c} \right)_M = 0,$$

- ★ *Back-bending* is related to the existence of a minimum of  $M_b$  along  $f = \text{const.}$  sequence,
- ★ **Conjecture:** character of stability persists for all rotation rates (A&A **450**, 2006, 747)

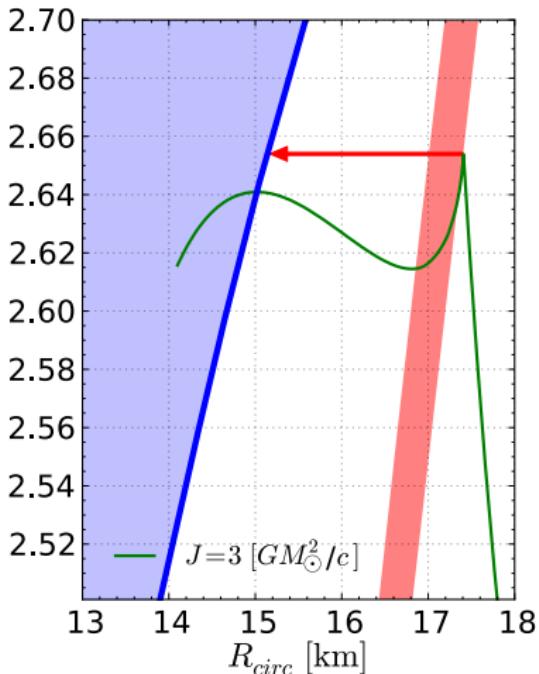
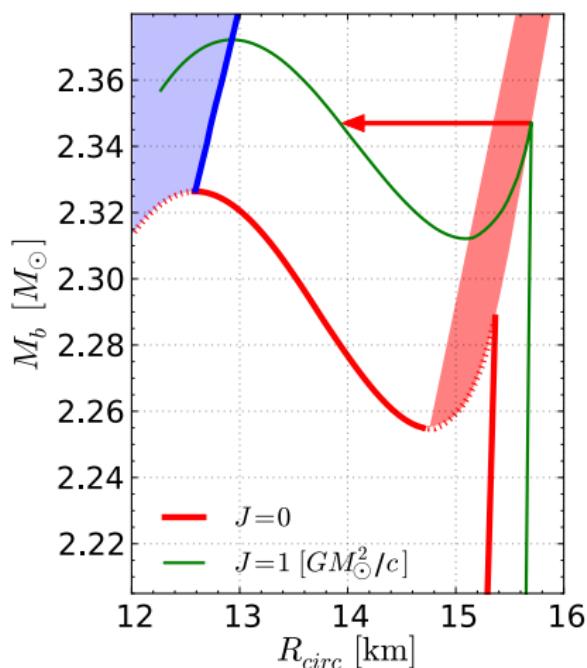
★ However, see Takami et al. (2011) for comparison with dynamical calculations

$f = \text{const.}$  curves on  $M_b(R)$  plane



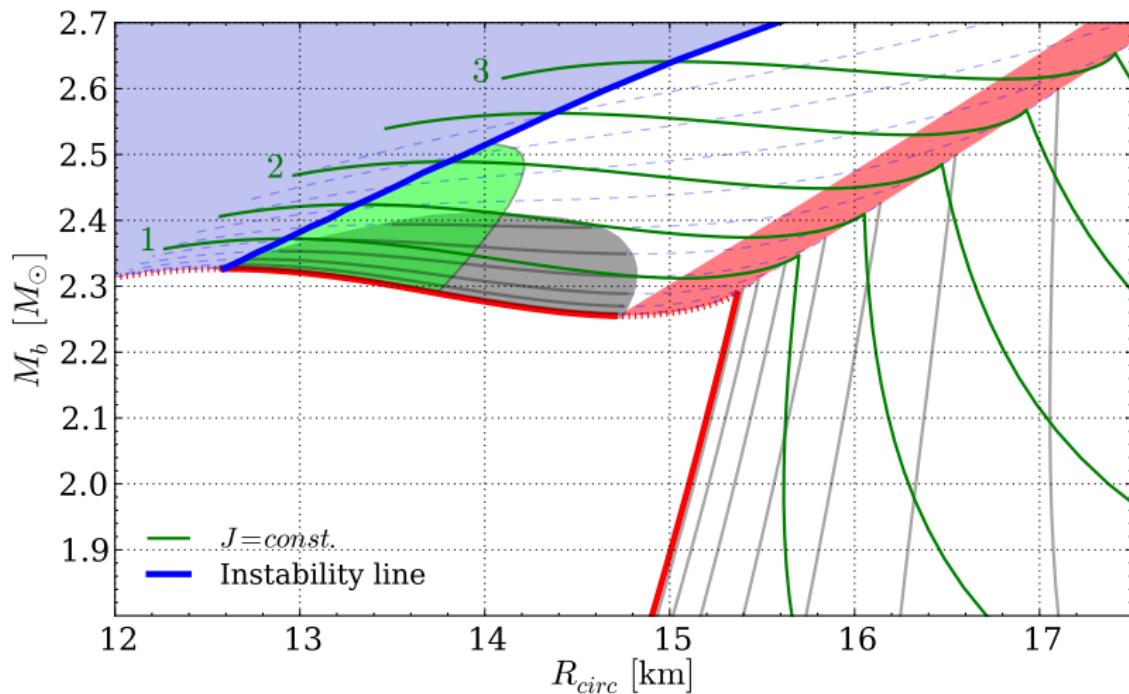
→ Dashed lines - *back-bending* is present (NS spins-up while monotonically losing angular momentum)

$J = \text{const.}$  curves, loss of stability and critical angular momentum  $J$



Analysis of  $J = \text{const.}$  sequences: stars with too much angular momentum (e.g., spun-up by accretion) end up in the instability.

## $J = \text{const.}$ curves on $M_b(R)$ plane



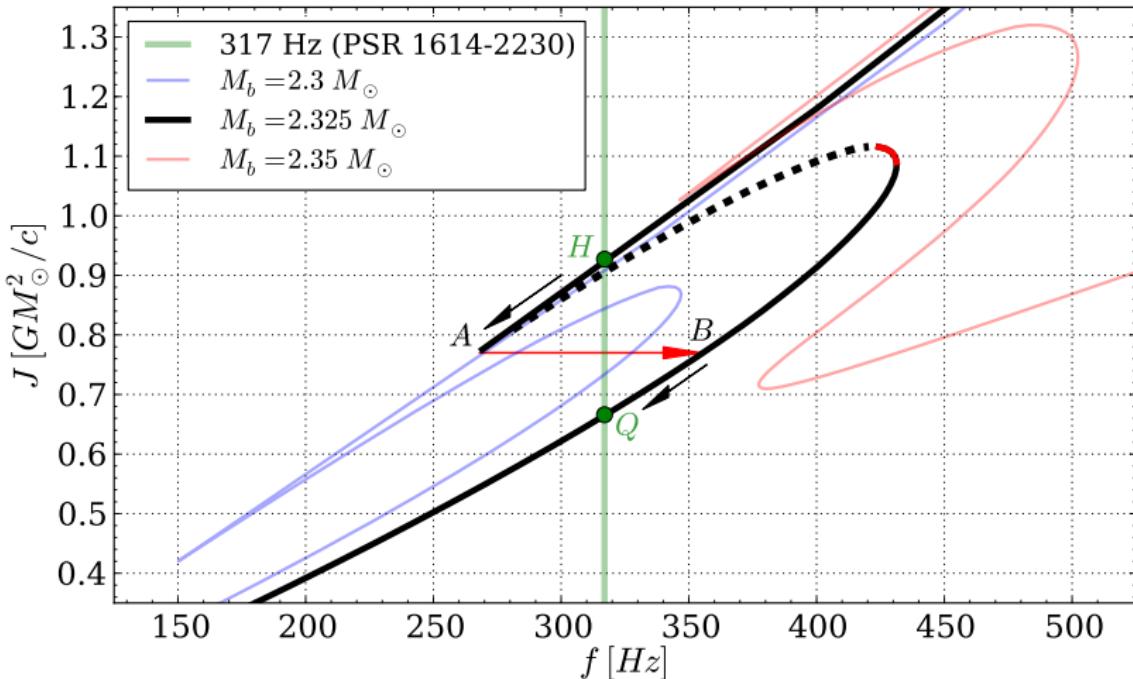
**Red region** - strong phase-transition instability,

**Blue region** - unstable w.r.t axisymmetric oscillations,

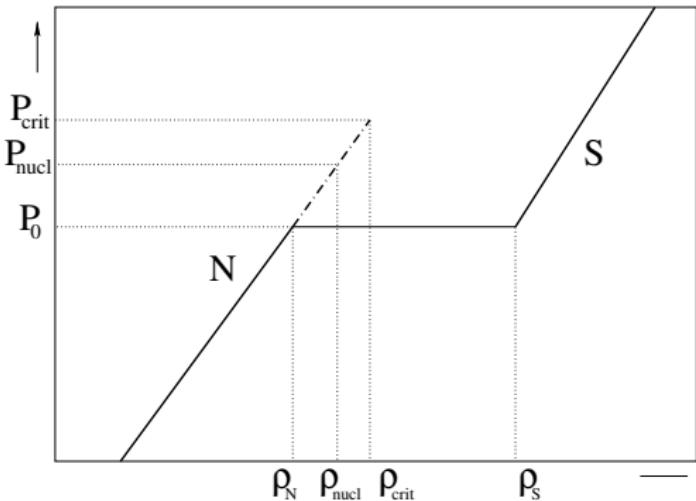
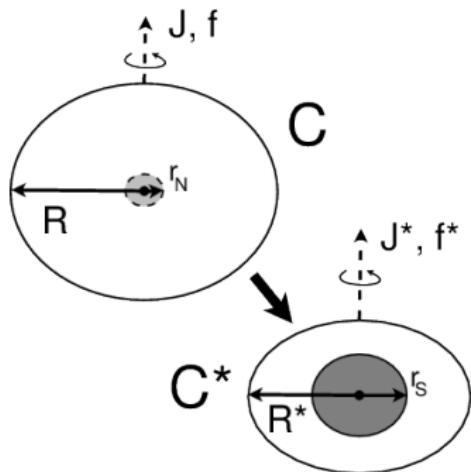
**Grey region** - no back-bending,

**Green region** - stable twin branch reached after the mini-collapse from the tip of  $J = \text{const.}$  curve, along  $M_b = \text{const.}$

$M_b = \text{const.}$  curves on  $J(f)$  plane

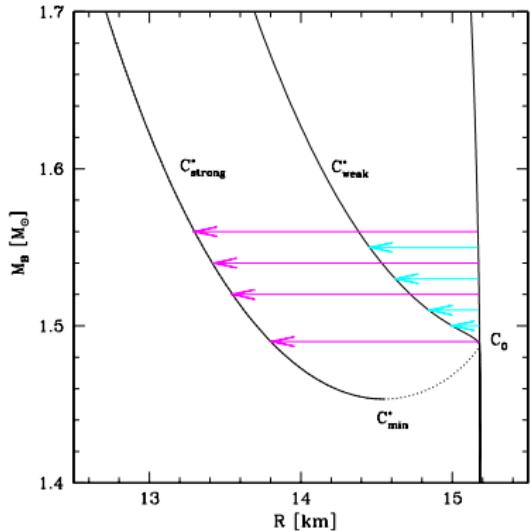


For NSs with measured gravitational mass  $M$  and frequency - possibility to put limits on  $M_b$ ,  $J$ , moment of inertia  $I$ , core EOS composition etc.

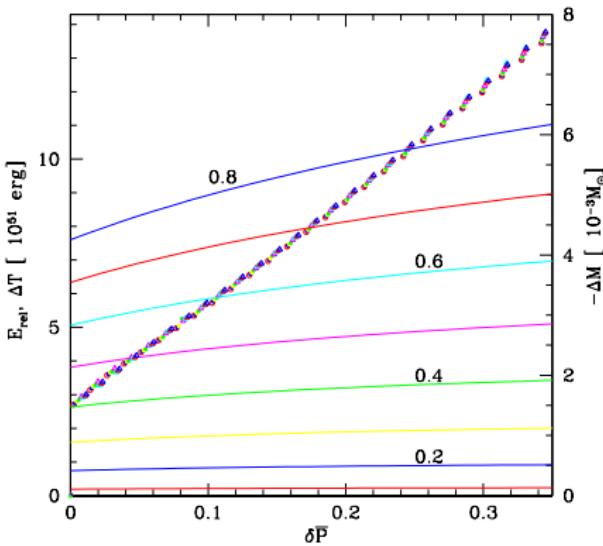


**Strong** phase transition if  
 $\rho_s / \rho_N > \frac{3}{2} (1 + P_0 / \rho_N c^2)$

# Energy release (A&A 479, 2008, 515)

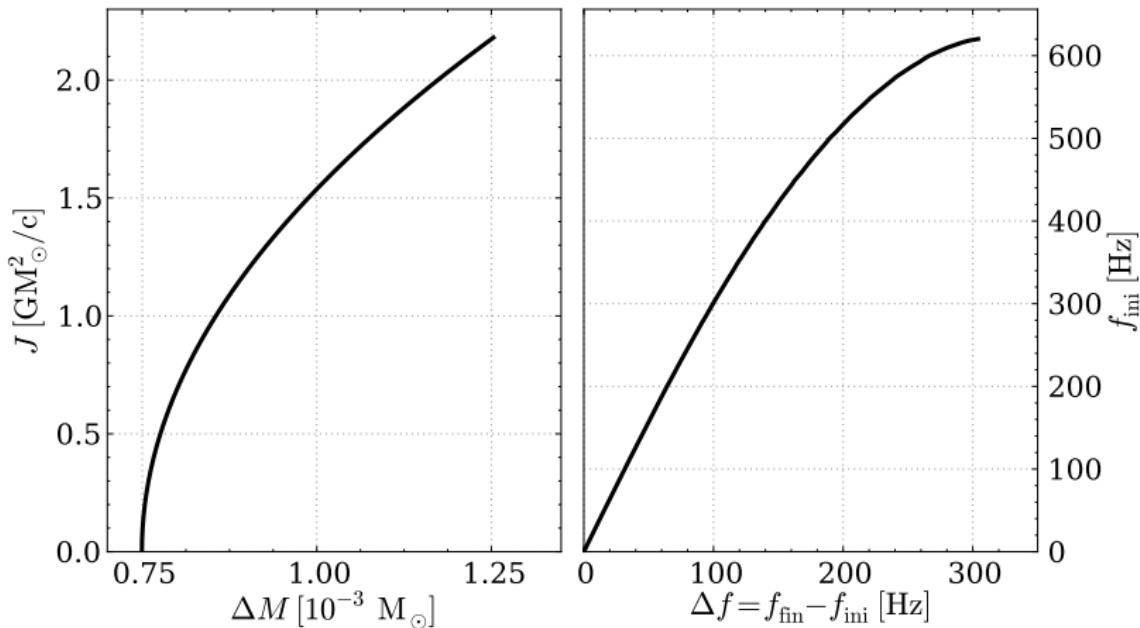


**Strong** phase transition if  
 $\rho_s / \rho_N > \frac{3}{2}(1 + P_0 / \rho_N c^2)$



Angular momentum  
 $J = 0.1, \dots, 0.8 \times GM_\odot^2/c$ ,  
 Energy release  $E_{\text{rel}} = (M - M^*)c^2$ ,  
 Kinetic energy  $\Delta T = T^* - T$ .

## Energy release in case of DD2-EV $\eta_2 = 0.12$ , $\eta_4 = 5$ EOS

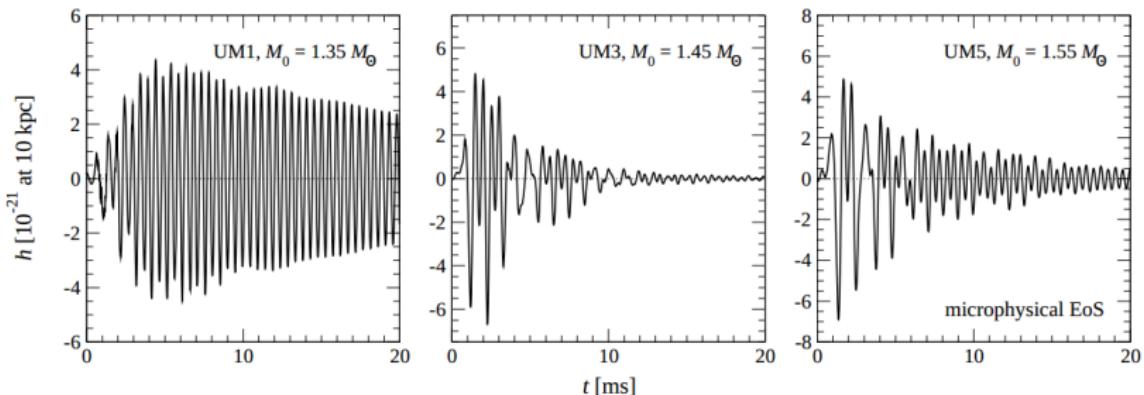
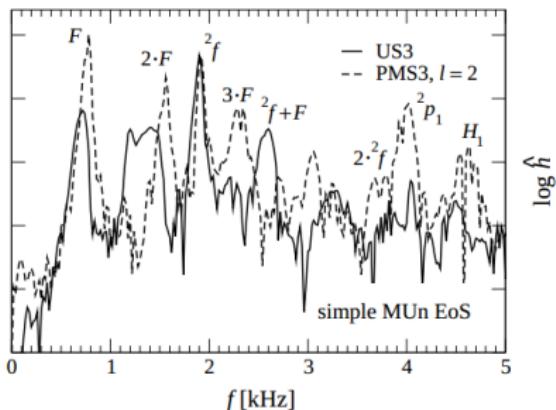


**Left panel:** energy release (difference in the gravitational mass) vs  $J$  of the configuration entering the strong phase-transition instability.

**Right panel:** spin-up  $\Delta f$  (difference between the final and initial spin frequency) against the spin frequency of the initial configuration.

# Burst-like GW emission (MNRAS 502, 2009, 605)

Time evolution of a dynamical mini-collapse induced by a phase transition (simulations with the CoCoNuT code)



## Summary/outlook

### Instability in the EOS

- ★ bypasses back-bending regions,
- ★ provides a "natural" spin frequency cut-off at some moderate (but  $> 716$  Hz) frequency,
- ★ resembles Fast Radio Burst 'blitzar' engine (Falcke & Rezzolla 2014):
  - ★ catastrophic mini-collapse to the second branch (or to a black hole),
  - ★ massive rearrangement of the magnetic field → energy emission.

### Other astrophysically-interesting questions:

- ★ Way to constraint on  $M_b$ ,  $J$ ,  $I$ , core EOS etc.,
- ★ Specific shape of NS-BH mass function (no mass gap?)
- population of massive, low B-field NSs (radio-dead?),
- population of massive, high B-field NSs (collapse enhances the field?),
- ★ Characteristic burst-like signature in GW emission during the mini-collapse.